

Truth table for 4 inputs and 7 outputs. The output values in the bottom 6 rows (decimal input values 10 - 15) are marked 'd' because it does not matter what the output is for these inputs.

z	y	x	w	a	b	c	d	e	f	g
0	0	0	0	1	1	1	1	1	1	0
0	0	0	1	0	1	1	0	0	0	0
0	0	1	0	1	1	0	1	1	0	1
0	0	1	1	1	1	1	1	0	0	1
0	1	0	0	0	1	1	0	0	1	1
0	1	0	1	1	0	1	1	0	1	1
0	1	1	0	1	0	1	1	1	1	1
0	1	1	1	1	1	1	0	0	0	0
1	0	0	0	1	1	1	1	1	1	1
1	0	0	1	1	1	1	1	0	1	1
1	0	1	0	d	d	d	d	d	d	d
1	0	1	1	d	d	d	d	d	d	d
1	1	0	0	d	d	d	d	d	d	d
1	1	0	1	d	d	d	d	d	d	d
1	1	1	0	d	d	d	d	d	d	d
1	1	1	1	d	d	d	d	d	d	d

Karnaugh maps for each of the outputs:

a		xw			
z y		0	0	1	1
		0	1	1	0
	0	1		1	1
	0				
	1		1	1	1
	1	d	d	d	d
	1	1	1	d	d

$$a = x + z + y \cdot w + \bar{w} \cdot \bar{y}$$

b		xw			
z y		0	0	1	1
		0	1	1	0
	0	1	1	1	1
	0				
	1	1		1	
	1	d	d	d	d
	1	1	1	d	d

$$b = \bar{z} \cdot \bar{y} + \bar{x} \cdot \bar{w} + z + x \cdot w$$

c		xw			
z y		0	0	1	1
		0	1	1	0
	0	1	1	1	
	0				
	0	1	1	1	1
	1	d	d	d	d
	1				
	1	1	1	d	d
	0				

$$c = \bar{x} + w + y$$

d		xw			
z y		0	0	1	1
		0	1	1	0
	0	1		1	1
	0				
	0		1		1
	1	d	d	d	d
	1				
	1	1	1	d	d
	0				

$$d = z + x \cdot \bar{w} + \bar{z} \cdot y \cdot x + \bar{y} \cdot \bar{w} + \bar{x} \cdot w \cdot y$$

e		xw			
z y		0	0	1	1
		0	1	1	0
	0	1			1
	0				
	0				1
	1	d	d	d	d
	1				
	1	1		d	d
	0				

$$e = \bar{y} \cdot \bar{w} + z \cdot \bar{x} \cdot \bar{w} + x \cdot \bar{w}$$

f		xw			
z y		0	0	1	1
		0	1	1	0
	0	1			
	0				
	0	1	1		1
	1	d	d	d	d
	1				
	1	1	1	d	d
	0				

$$f = z + \bar{x} \cdot \bar{w} + y \cdot \bar{w} + \bar{x} \cdot y$$

g		xw			
z y		0	0	1	1
		0	1	1	0
	0			1	1
	0				
	1	1	1		1
	1	d	d	d	d
	1	d	d	d	d
	0	1	1	d	d

$$g = z + \bar{x}.y + \bar{z}.\bar{y}.x + x.\bar{w}$$

AND gates which are repeated and can therefore be reused in the circuit:

$\bar{w}.\bar{y}$	$x.\bar{w}$	$\bar{z}.\bar{y}.x$	$\bar{x}.y$
a, d, e	d, e, g	d, g	f, g

Screen-prints of the circuit showing each of the 10 decimal digits on the 7-segment display for the relevant binary input.











