Truth table for 4 inputs and 7 outputs. The output values in the bottom 6 rows (decimal input values 10 - 15) are marked 'd' because it does not matter what the output is for these inputs.

Z	У	Х	W	а	b	С	d	е	f	g
0	0	0	0	1	1	1	1	1	1	0
0	0	0	1	0	1	1	0	0	0	0
0	0	1	0	1	1	0	1	1	0	1
0	0	1	1	1	1	1	1	0	0	1
0	1	0	0	0	1	1	0	0	1	1
0	1	0	1	1	0	1	1	0	1	1
0	1	1	0	1	0	1	1	1	1	1
0	1	1	1	1	1	1	0	0	0	0
1	0	0	0	1	1	1	1	1	1	1
1	0	0	1	1	1	1	1	0	1	1
1	0	1	0	d	d	d	d	d	d	d
1	0	1	1	d	d	d	d	d	d	d
1	1	0	0	d	d	d	d	d	d	d
1	1	0	1	d	d	d	d	d	d	d
1	1	1	0	d	d	d	d	d	d	d
1	1	1	1	d	d	d	d	d	d	d

Karnaugh maps for each of the outputs:

а	XW					
		0	0	1	1	
		0	1	1	0	
z	0			T		
У	0					
	0		$\overline{1}$	1	1	
	1		l	l J	J	
	1	d	d	d	d	
	1				J	
	1	1	1	d	d	
	0					

$$a = x + z + y \cdot w + \overline{w} \cdot \overline{y}$$

b	XW				
		0	0	1	1
		0	1	1	U
Z	0		1	\Box	1
z y	00				
	0	1		1	
	1				
		d	d	d	d
	1				
	1	1	1	d	d
	0				

$$b = \overline{z} \cdot \overline{y} + \overline{x} \cdot \overline{w} + z + x \cdot w$$

Mark Bellingham - 140320986 G4Z1002 CSF Assignment

	С			xw		
			0	0	1	1
			0	1	1	0
	Z	0	$\overline{1}$			
	У	0				
		0	1	1	1	1
		1				
		1	d	d	ď	d
		1				
		1 0	1	1	d	d
Į		0				

$$c = \overline{x} + w + y$$

d			XW		
		0	0	1	1
		0	1	1	0
Z	0			$\boxed{1}$	1
z y	0				
	0				1
	1				
	1	d	d	d	d
	1				
	1		1	d	d
	0				

 $d = z + x \cdot \overline{w} + \overline{z} \cdot \overline{y} \cdot x + \overline{y} \cdot \overline{w} + \overline{x} \cdot w \cdot y$

е	XW					
		0 0	0	1	1 0	
		0	1	1	0	
Z	0 0				1	
z y	0					
	0 1				1	
	1					
	1	d	d	d	d	
	1					
	1			d	d	
	0					

 $e = \overline{y} \cdot \overline{w} + z \cdot \overline{x} \cdot \overline{w} + x \cdot \overline{w}$

f	XW				
		0	0	1	1 0
		0	1	1	0
Z	0 0	1			
У					
	0	1	\Box		1
	1				
	1	d	d	d	d
	1				
	1	1	1	d	d
	0				

 $f = z + \overline{x} \cdot \overline{w} + y \cdot \overline{w} + \overline{x} \cdot y$

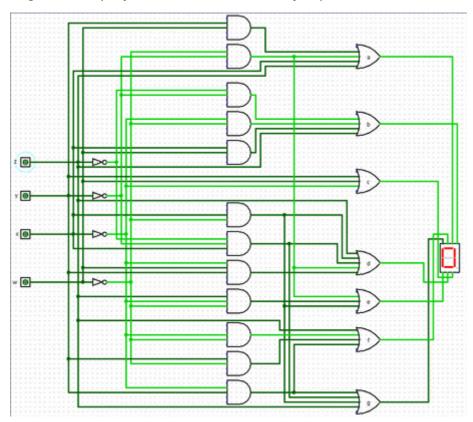
g	XW				
		0	0	1	1
		0	1	1	0
Z	0			1	
У	0				
	0	$\overline{\Box}$	U		1
	1	l	J		
	1	d	d	d	d
	1				
	1	1	1	d	d
	0				

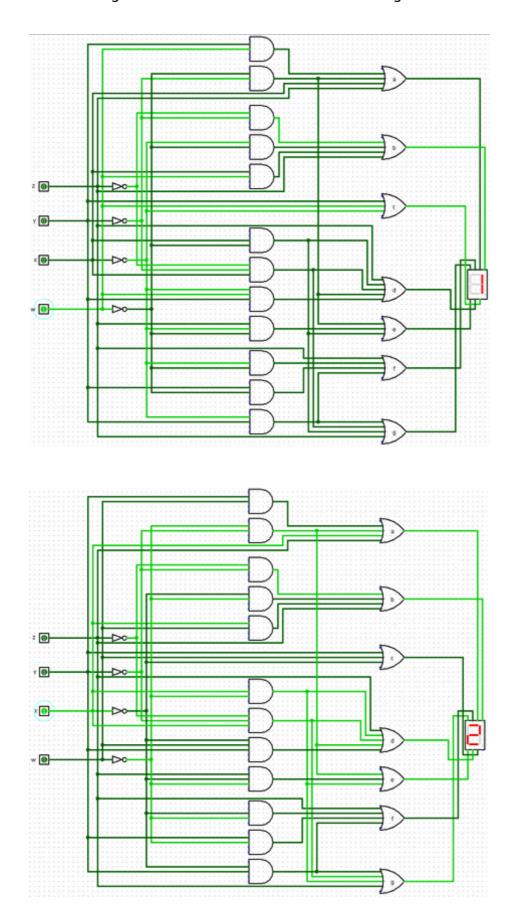
$$g = z + \overline{x} \cdot y + \overline{z} \cdot \overline{y} \cdot x + x \cdot \overline{w}$$

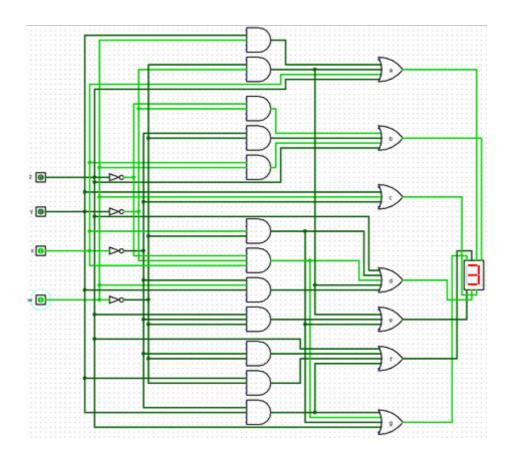
AND gates which are repeated and can therefore be reused in the circuit:

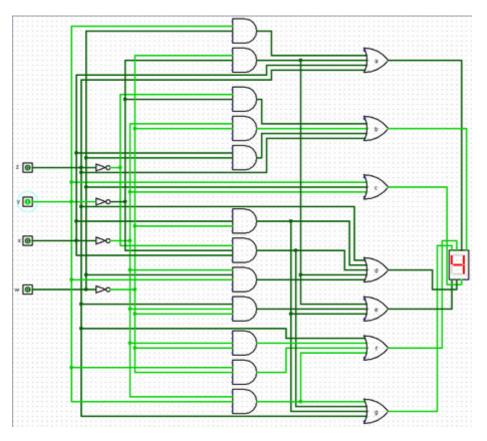
\overline{w} . \overline{y}	$X.\overline{W}$	\overline{z} . \overline{y} . x	\overline{x} . y
a, d, e	d, e, g	d, g	f, g

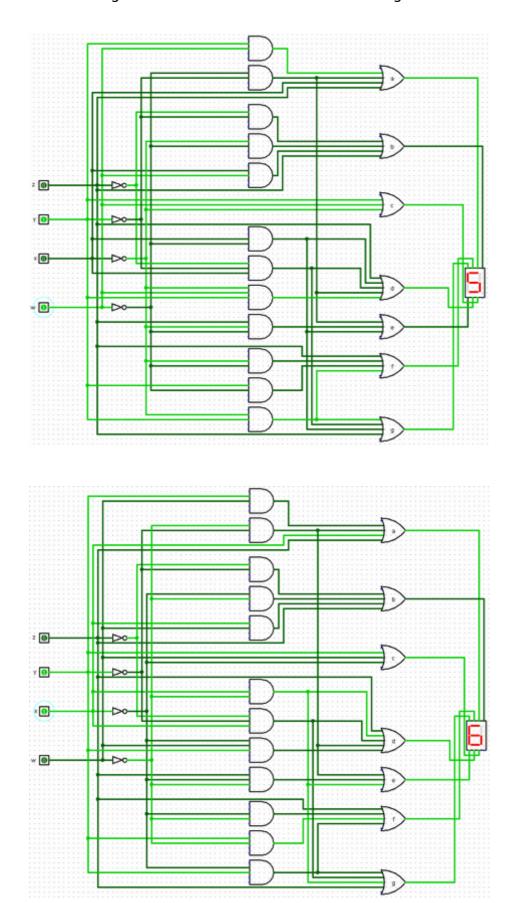
Screen-prints of the circuit showing each of the 10 decimal digits on the 7-segment display for the relevant binary input.

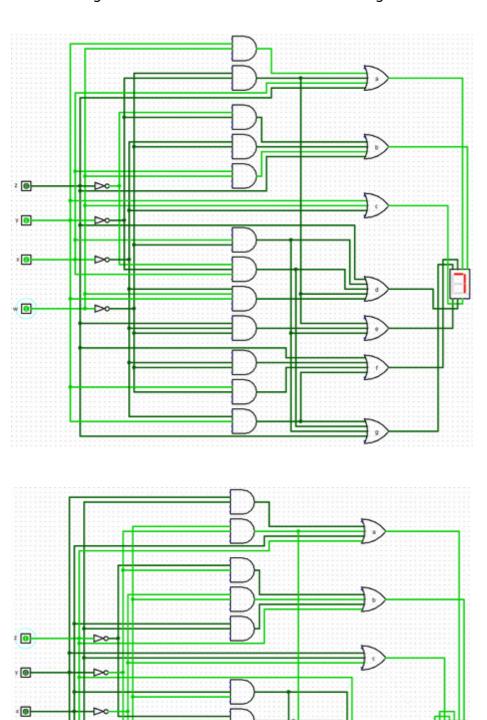












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