# A modular ADC system for power data acquisition utilising coreless PCB transformers for power and signal isolation

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Abstract-Although current industrial energy meters offer high accuracy and reliability, they are typically expensive and low-bandwidth, making them poorly suited to a multi-sensor data collection scheme. As a result, this paper proposes the concept of a measurement device that is highly modular and extendible, in addition to being accurate, compact and low-cost. To minimise cost, the proposed measurement device will make use of planar coreless PCB trnasformer in order to provide galvanically isolated outputs. The network of measurement devices would then be consolidated by a central processing device (for example, an FPGA) before integration with existing control systems and computer consoles. This paper focusses primarily on the practical use of planar coreless PCB transformers, which will facilitate the module's isolated power, clock and data signal transfer. The paper presents calculations necessary to design coreless PCB transformers, and shows circuits designed for the transformer's practical application in the measurement module. The coreless PCB transformer and each associated application circuit is experimentally verified, with test data and conclusions made applicable to coreless PCB transformers in general.

#### I. Introduction

Currently, industrial energy users are limited to the use of generally expensive and low-bandwidth energy usage data collection devices. Although such metering devices are well suited to high-accuracy, high-energy systems, they are poorly suited to highly modular, multi-sensor data collection schemes. To facilitate industrial process refinement, fault detection and energy usage analysis, the Queensland University of Technology researchers are currently developing a galvanically isolated, low-cost, high-bandwidth data acquisition module (herein referred to as a DAQM). Data from the network of distributed measurement modules will be consolidated by a central processor (such as an FPGA), with a microcontroller facilitating the data logging and integration into existing control systems and computer consoles.

Conventionally, a galvanically isolated power supply is designed using a transformer with magnetic core to provide isolation in one of several DC-DC conversion topologies. Although a proven, reliable technology capable of high power and high efficiency, the transformer can be an expensive and bulky component. Additionally, in an application with a very low output power requirement ( $<\frac{1}{4}W$ ), the transformer, and possibly the entire DC-DC converter design, may be excessively over-engineered for the low-power application

unnecessarily increasing the system size and cost.

For isolated data transfer, opto-couplers are a popular solution for many low- to moderate-frequency signal transfer. For high-frequency applications (such as high-speed ADC data transfer), opto-couplers capable of reliable operation at several megahertz are expensive. A relatively new method of signal isolation, the digital isolator, can operate at up to many tens of megahertz, however with a typical price of several dollars per two-channel unit (in 1ku quantities), their application in a low-cost device (such is the data acquisition module) is limited. Planar coreless PCB transformers are not a new idea, and considerable work has been published on their use in isolated gate drive circuits for switch-mode power converters [1][2][3][4]. Although wireless charging systems for consumer electronics use a very similar concept, coreless PCB transformers have not seen significant use as a power and signal transfer device within commercial electronics. Since a coreless PCB transformer's only cost is the PCB area it consumes, they are well suited for low-cost applications, and the use of standard PCB manufacturing processes makes their construction predictable and repeatable.

This paper will focus primarily on the practical application of planar coreless PCB transformers as used for the module's isolated power, clock and data signal transfer. Calculations necessary to design the coreless PCB transformers are presented, and practical circuits designed for the DAQM application but applicable to coreless PCB transformers in general, are included. The experimental validation section demonstrates the viability of the use of a coreless PCB transformer in the DAQM application. Test results for the transformer itself and each associated application circuit is shown, with the test data and conclusions applicable to coreless PCB transformer-based designs in general.

#### II. PROPOSED MODULAR DATA ACQUISITION SYSTEM

The complete data acquisition system (1) comprises of one or more data acquisition modules (DAQMs), a data consolidation FPGA, and a microcontroller attached to a PC, display or storage device. The DAQM's data conversion device is a commercial dual-input sigma-delta IC, with appropriate signal conditioning to facilitate voltage measurement via a resistor divider, and current measurement via a resistive shunt or current transformer (CT). This paper will refer to the data conversion side of the DAQM as the "secondary" side. The

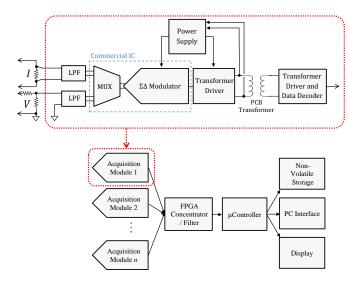


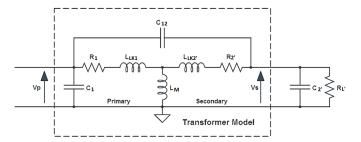
Fig. 1. Modular isolated power measurement system.

primary side of the DAOM consists of the coreless PCB transformer driver, clock encoding and data recovery circuitry. To power the sigma-delta converter (secondary side) and to provide it with a clock signal from the host, a single planar coreless PCB transformer is used. This is teamed with a smaller, much higher frequency coreless PCB transformer in order to transfer data from the sigma-delta modulator back to the host. For the selected sigma-delta converter, the clock frequency is approximately 8MHz, resulting in a data rate of  $f_{clock}/4$  (voltage and current share one data stream) with the maximum input sampling rate of  $f_{clock}/12$ . Whilst considerable work has been presented regarding the use of planar coreless PCB transformers in power transfer and isolated gate drive circuits, such papers do not discuss a high-frequency data and power transfer application [1][2][3][4]. The planar coreless PCB transformer, along with the methods used to transfer power, clock and data signals, will be the focus of this paper.

### III. PLANAR CORELESS PCB TRANSFORMERS

The fundamental design of a planar coreless PCB transformer involves two planar copper spirals - one etched onto either side of a regular two-layer PCB. The two windings are thus separated by the PCB's core, whose material properties and thickness determine, to some extent, the transformer's performance and primary-to-secondary isolation. This transformer's primary winding is then driven at high frequency, usually in the range of 2MHz to 20MHz in order to achieve either the maximum [input] impedance frequency (MIF useful in low power systems) or the maximum efficiency frequency (MEF - useful for high power systems)[1][2][3][4]. [1] has demonstrated that an external secondary load capacitor, in the order of 100pF to 1nF, plays a significant role in the determination of the transformer's resonant frequency. In conventional coreless PCB transformer applications, the output (ie: secondary winding) voltage is then rectified and filtered. Transformer efficiencies exceeding 90%, with power density of up to  $24W/cm^2$  have been demonstrated [1].

Planar coreless PCB transformers are very low cost and feature high power densities, no manufacturing restrictions



High-frequency transformer model [1].

due to core size or shape and are constructed using highly repeatable standard PCB manufacturing process.

A two-winding coreless PCB transformer may be described using the high-frequency transformer model in figure 2 [1], where:

 $R_1$ Primary winding resistance;

 $R_2'$ Secondary winding resistance, referred to primary;

Load resistance, referred to primary;

 $R_{L}^{2}$   $R_{L}^{\prime}$   $L_{LK1}$   $L_{LK2}^{\prime}$   $L_{M}$   $C_{12}$ Primary leakage inductance;

Secondary leakage inductance, referred to primary;

Mutual inductance;

Primary-to-secondary winding capacitance;

Sum of primary winding capacitance and primary driver output capacitance;

 $C_2'$ Sum of secondary winding capacitance and external

load capacitance, referred to primary; Turns ratio; n

Permeability of vacuum;  $\mu_0$ 

Inner radius of *i*th circular track filament;  $a_1$ 

Outer radius of ith circular track filament;  $a_2$ 

Height of ith circular track filament;  $h_1$ 

Inner radius of *j*th circular track filament;  $r_1$ 

Outer radius of jth circular track filament;  $r_2$ 

Height of *j*th circular track filament;

Separation distance between the circular tracks;

 $J_0(x)$ Bessel function of the first kind, order zero.

The self inductance of the planar winding is given by

$$L_p = \sum_{j=1}^{N_p} \sum_{i=1}^{N_p} M_{ij} \tag{1}$$

$$L_s = \sum_{j=1}^{N_s} \sum_{i=1}^{N_s} M_{ij} \tag{2}$$

And thus, the mutual inductance between the two planar windings may be represented as

$$M_{ps} = \sum_{i=1}^{N_p} \sum_{i=1}^{N_s} M_{ij} \tag{3}$$

where the mutual inductance,  $M_{ij}$ , has been reported in [5]

$$M_{ij} = \frac{\mu_0 \pi}{h_1 \ln(\frac{r_2}{r_1}) h_2 \ln(\frac{a_2}{a_1})} \int_0^\infty S(kr_2, kr_1) S(ka_2, ka_1)$$

$$Q(kh_1, kh_2) e^{-k|z|} dk$$
(4)

where

$$S(kx, ky) = \frac{J_0(kx) - J_0(ky)}{k}$$

$$Q(kx, ky) = \begin{cases} \frac{2}{k^2} \left[ \cosh k \frac{x+y}{2} - \cosh k \frac{x-y}{2} \right] & z > \frac{h_1 + h_2}{2} \\ \frac{2}{k} \left[ h + \frac{e^{-kh} - 1}{k} \right] & z = 0, x = y = h \end{cases}$$
(6)

To approximate the performance of the coreless PCB transformer, [1] gives the resonant frequency as

$$f_0 = \frac{1}{2\pi\sqrt{L_{eq}C_{eq}}};\tag{7}$$

and the s-domain voltage gain (8) and input impedance (9) as

$$\frac{V_s}{V_p} = G(s) = B = \frac{\frac{1}{X_1} + sC_{12}'Y_1}{nY};$$
(8)

$$Z_{in} = \frac{1}{sC'_{12}(1 - nB) + \frac{1 - A}{X_1} + sC'_1}.$$
 (9)

Although it is not of great concern to the DAQM application (due to the low secondary power requirements), the efficiency of the coreless PCB transformer may be calculated as follows

$$P_{out} = \frac{|G(s)|^2 \cdot |V_p|^2}{R_L};$$
(10)

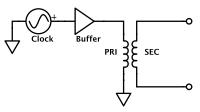
$$P_{in} = |V_p|^2 \cdot \Re\left[\frac{1}{Z_{in}}\right]; \tag{11}$$

and thus,

$$\eta = \frac{|G(s)|^2}{R_L \cdot \Re\left[\frac{1}{Z_{in}}\right]} \times 100\%. \tag{12}$$

where

$$\begin{split} L_{eq} &= L'_{LK2} + L_{LK1} || L_M \\ C_{eq} &= C'_2 + C'_{12} \\ R'_2 &= n^2 R_2 \\ L'_{LK2} &= n^2 L_{LK2} \\ C'_1 &= C_1 + \frac{n-1}{n} C_{12} \\ C'_2 &= \frac{1}{n^2} C_2 + \frac{1-n}{n^2} C_{12} \\ C'_{12} &= \frac{1}{n} C_{12} \\ X_1 &= R_1 + s L_{LK1} \\ X_2 &= R'_2 + s L'_{LK2} \\ Y_1 &= X_2 \left[ \frac{1}{X_1} + \frac{1}{s L_M} + 1 \right] \\ Y_2 &= \frac{1}{X_2} + s C'_{12} + s C'_2 + \frac{1}{n^2 R_L} \\ Y &= -\frac{1}{X_2} + Y_1 Y_2 \\ A &= \frac{s C'_{12} + \frac{X_2}{X_1} Y_2}{Y_1} \\ A &= \frac{s C'_{12} + \frac{X_2}{X_1} Y_2}{Y_2} \end{split}$$



a) Single-Ended Drive

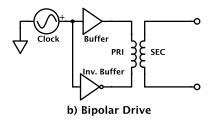


Fig. 3. Single-ended (a) and bipolar (b) transformer drive concept.

# IV. IMPLEMENTATION OF POWER AND SIGNAL ISOLATION USING PCB TRANSFORMERS

#### A. Power

The most basic use for a planar coreless PCB transformer is in an isolated power transfer application. Typically, this would be achieved by driving the transformer at its maximum efficiency frequency (MEF) for high power transfer applications, or, where it is desirable to minimise the quiescent power consumption of the transformer, the maximum impedance frequency (MIF). The MEF will tend to approach the MIF as the transformer's secondary load current decreases [1]. Due to the low secondary load current of the DAQM, approximately 6mA at 3.3V (20mW), the MEF of the module's coreless PCB transformer was initially assumed to be equal to the MIF. In most papers discussing planar coreless PCB transformers, the primary winding is driven in either a singleended or bipolar manner 3 with a relatively high supply voltage (12V being a popular choice for isolated gate drive circuits). Since the DAQM is to be a 3.3V supply capable device, the PCB transformer is driven in a bipolar manner to achieve an effective doubling of the primary drive voltage. The primary drive circuit uses a simple relaxation oscillator for the resonant frequency generation, and the transformer's winding is driven directly by the Schmitt-trigger's high-current (±32mA) pushpull outputs 4. On the transformer's secondary side, the output waveform may simply be rectified using a voltage-doubler rectifier topology 4, with a zener clamping diode to ensure the voltage regulator's maximum input voltage is not exceeded. The additional load capacitance, primarily due to the rectifier diode array D2 and coupling capacitor C4, can reduce the PCB transformer's resonant frequency by 5%-10%. When the regulator's input capacitor is much greater than each of the rectifier diode's junction capacitance, that is,  $C7 \gg C_D$ , the additional load capacitance may be estimated as

$$C_{extra} = C4//(C_{D2a} + CD2b)$$

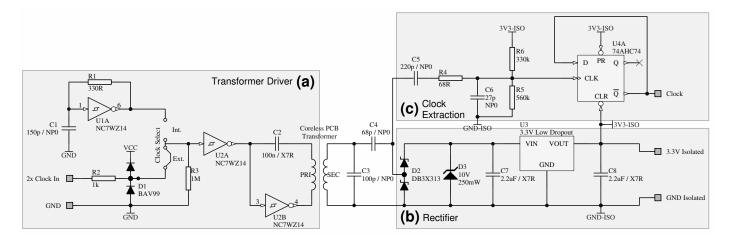


Fig. 4. Coreless PCB transformer driver (a) with power rectifier (b) and clock extraction circuitry (c) highlighted.

## B. Clock Generation and Recovery

In order to provide a clock signal of approximately 8MHz to the frontend ADC, a method of transferring this clock signal via the PCB transformer from the DAQM's primary side to the secondary side (where the sigma-delta data converter resides) was required. It is desirable to allow the sigma-delta modulator to be externally clocked as this allows for synchronisation in multi-module systems, thus simplifying the filtering and data consolidation process. Since a coreless PCB transformer's resonant frequency may be adjusted quickly and easily using the external load capacitance, it is possible to drive the transformer at any power-of-two multiple of the desired modulator clock frequency (provided the resulting drive frequency results in sufficient secondary output voltage). The clock signal may then extracted simply by rectifying, filtering and dividing the transformer's secondary voltage waveform. The resulting clock recovery circuit has been highlighted in FIGURE.

# C. Data Recovery

The sigma-delta data converter encodes both voltage and current information into a single Manchester-encoded bitstream at a rate equal to  $f_{clock}/4$  (typically 2MHz). To transfer this data back to the primary side of the data acquisition module, a second coreless PCB transformer may be used. Since the data signal is not periodic in the way that a clock signal may be, it is necessary to configure the data transformer for a very high resonant frequency. This ensures that only the high-frequency square wave transitions are sent over the coil. As the data frequency approaches the transformer's resonant frequency, the transformer's output voltage can be seen to 'ring' after the fundamental edge transition is transmitted - a benefit when maximum power transfer is required, but detrimental to the signal integrity of data transmissions. To achieve a very high resonant frequency, the EQUATIONS imply that either the number of primary and secondary turns (and thus the primary and secondary outer diameter) should be decreased, and/or the external load capacitor may be reduced or removed. FIGURE shows the signal transformer and data recovery circuit. On the signal transformer's secondary side (where the sigma-delta modulator is located), the data output of the modulator is capacitively coupled into the signal transformer, which is driven in a single-ended configuration. On

the primary side, the low-amplitude (50mV to 500mV may be expected) positive- and negative-going spikes, which represent the rising and falling edges of the data signal respectively, are first amplified by a bipolar junction transistor (BJT). The amplifier's output is then coupled into two more BJTs with necessary biasing to allow the discrimination of the positive-and negative-going transitions. The output of each of the 'edge transition detectors' is then fed into a set/reset latch constructed from a dual Schmitt-input NAND array. As an added benefit, the outputs of the two NAND gates are complementary and thus allow for differential signal driving back to the host FPGA (which may be located some distance away).

# V. EXPERIMENTAL VALIDATION

To validate the use of planar coreless PCB transformers in the data acquisition module design, a test PCB transformer was manufactured on a standard two-layer, 1.6mm PCB. The test transformer had 11 turns with identical primary and secondary windings. The track and spacing width was equal at  $203.2\mu m$  (8 mil), giving an outer diameter of 13.7mm.

# A. Power

To approximate the expected load of the sigma-delta modulator and associated secondary circuitry, a  $500\Omega$  load resistor was fitted after the rectifier. By sweeping the primary drive frequency over the range of 500kHz to 25MHz, the coreless PCB test transformer, with primary-side Schmitt trigger driver and secondary side rectifier could be analysed for input impedance- and output voltage- versus frequency (FIGURE). The figure shows a clear distinction between the MIF (13MHz) and MEF (15.5MHz), however the reasonably low quality factor of the MEF peak suggests that driving the transformer at a frequency of compromise between the MIF and MEF may be desirable. The data also demonstrate the effectiveness of driving the transformer in a bipolar manner, which has resulted in an output voltage approximately 1.6 times the 3.3V primary supply voltage - thus increasing the usable voltage range of the data acquisition module and simplifying the secondary voltage supply circuitry. FIGURE shows the coreless PCB test transformer's secondary rectified output power and voltage versus load current. It shows a maximum power point of

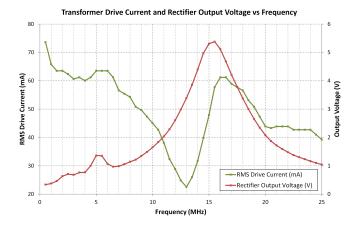


Fig. 5. Input impedance and output voltage versus frequency at 3.3V.

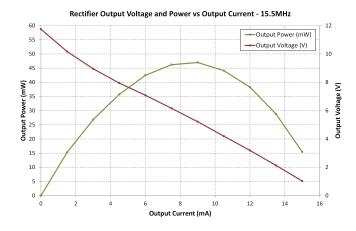


Fig. 6. Secondary output voltage and power versus load current at MEF (15.5MHz).

47mW, and that for a minimum pre-regulator voltage of 3.5V, the load current may be up to 11mA (about 40mW) twice the expected power required by the DAQM's secondary circuitry. As a compromise between the MIF (13MHz) and MEF (15.5MHz), the test transformer drive frequency was adjusted to 14MHz (see FIGURE). This data shows improved load regulation and a shift in the maximum power point toward greater load currents, as well as a slight reduction in maximum power (approximately 47mW max versus 40mW max). This suggests that transformer operation at a MEF-MIF compromise frequency (rather than at the MEF exactly) can have benefits for applications with greater secondary loads where the primary is driven by a current-limited source (such as the Schmitt trigger direct-drive circuit used herein). The recommended experimental frequency setting procedure is to configure the secondary circuit for maximum expected load, then adjust the primary driver frequency for maximum secondary output voltage.

#### B. Clock Generation and Recovery

Since the sigma-delta modulator's clock is derived from the drive frequency of the primary winding, it is necessary for the primary drive frequency to be an exact power-of-two multiple of the desired modulator frequency, which may vary from DC

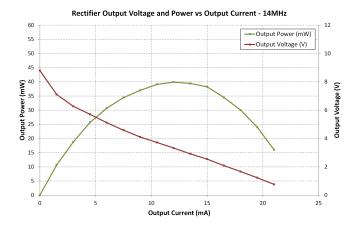


Fig. 7. Secondary output voltage and power versus load current at MIF-MEF compromise (14MHz).

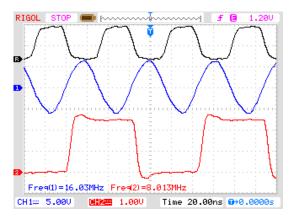


Fig. 8. 16MHz input clock signal (top); secondary output voltage (centre); 8MHz extracted clock signal (bottom).

to 8MHz. For the DAQM application, however, the external clock is necessary for multi-module synchronisation, and there is no desire to operate the sigma-delta modulator at a clock frequency other than 8MHz. The test coreless PCB transformer has been designed for a 16MHz resonant frequency, with prior figures showing this to be the case in practice. FIGURE shows the 16MHz clock signal (Reference - white), secondary output voltage (Channel 1 - yellow) and extracted clock signal (Channel 2 - cyan). The divide-by-two clock extraction method appears effective, even with a varying secondary load, and further testing showed the simple circuit was able to accurately output a clock signal over the transformer drive frequency range of 11MHz to 16MHz. The figures show no reason why a higher order division (divide by 4, for example) could not be used if desired.

# C. Data Recovery

To test the data recovery circuit, a second PCB transformer was obtained with physical specifications identical to the unit discussed prior. This second test transformer, however, had its load capacitor (which was 100pF in the prior unit) removed, such that its resonant frequency (now estimated to be >80MHz) was much greater than the expected data frequency - a key requirement of the data detection circuit. Driving the transformer in a single-ended configuration was achieved by

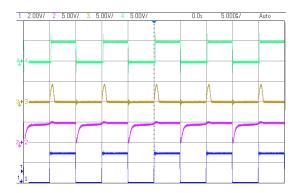


Fig. 9. Data into transformer (CH1, bottom); output of negative edge amplifier (CH2); output of positive edge amplifier (CH3); recovered data signal at output of transformer (CH4, top).

grounding one terminal and connecting the other, via a small capacitor, to a signal generator simulating the sigma-delta modulator's data output. Due to hardware availability issues, the high-speed ( $t_d \le 10ns$ ) Schmitt NAND gate specified in the circuit was substituted for an ordinary-speed ( $t_d \approx 250ns$ ) Schmitt NAND gate, which resulted in poor performance above about 500kHz (due to the fast impulses generated by the edge detection circuit). FIGURE shows the data recovery circuit operating at 100kHz, where Channel 1 (bottom) is the 2MHz simulated data into the transformer; Channel 2 is the output of the negative edge amplifier (node 'Neg Edge' in FIGURE); Channel 3 is the output of the positive edge amplifier (node 'Pos Edge' in FIGURE); and Channel 4 (top) is the recovered 2MHz data signal. Since the data recovery circuit was capable of reliable operation with edge spikes of an amplitude as low as about 100mV, the 11-turn transformer was found to be excessive for the data signal transfer. By cutting the PCB copper tracks on the primary and secondary side of the transformer, the performance of the data recovery circuit was tested for a transformer consisting of five turns and three turns. The test showed that for a 3.3V square wave input, the five-turn and three-turn transformer yielded edge spikes of amplitude approximately 170mV and 50mV respectively. FIGURE shows the positive and negative edge spikes at the secondary of the five-turn coreless PCB transformer with a 3.3V, 2MHz primary signal applied (via a small capacitor). Testing has demonstrated that the data recovery circuit is effective over a range of data rates and duty cycles, and that a coreless PCB transformer with as few as four to five turns can be expected to yield reliable performance.

# VI. FUTURE WORK

The development of the coreless PCB transformer for use in the data acquisition module has yielded two key further research opportunities. With each module's coreless PCB transformer operating at 16MHz, significant electromagnetic interference (EMI), both radiated and conducted, may be expected. Whilst informal experimentation has shown that crosstalk between planarly separated modules is much less than when the modules are axially separated, a thorough analysis has not yet been performed and thus the extent and effect of inter-module interference is not yet known. [6] demonstrates that relatively thin (0.4mm) ferrite sheets can provide effective EMI shielding - up to a shielding effectiveness of 40dB for

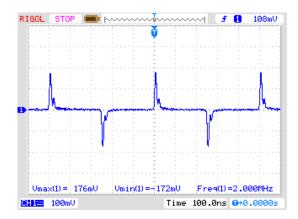


Fig. 10. Positive and negative edge spikes at secondary of 5-turn transformer (3.3V primary signal).

a bare ferrite sheet, or up to 60dB for the same sheet but with copper backing. Cost analysis has shown that such a ferrite sheet may increase the module cost by 10-20%, which, considering the low initial cost of the device, may represent a worthwhile inclusion.

Other methods for EMI reduction include driving the coreless PCB transformer with a sinusoidal waveform rather than the square waveform used currently, and the possibility of using a spread-spectrum driver in order to reduce the amplitude of the fundamental drive frequency.

The second area of research interest involves the transmission of the 2MHz (typical) data signal from the module's secondary side to the primary side, using the same coreless PCB transformer used to transfer the clock signal (16MHz ÷ 2 typical) and provide isolated secondary power. This single-transformer concept is the ultimate goal of the DAQM's coreless PCB transformer design, with the original intention being that the data signal would be load- or resonant frequency-modulated at the secondary, which could be detected by monitoring the transformer's primary-side drive current. Such disturbance detection is performed in commercial RFID systems, where the receiver modulates its antenna's resonant frequency to allow the transmitter to identify the receiving device [7].

In practice, even 100% load- or resonant frequency-modulation, which also reduces the average output voltage below the minimum requirement, yielded a primary current change of less than ten milliamperes. This small amplitude distinction, coupled with the limited spectral separation of the data (2MHz) and carrier (16MHz) frequencies, loss of adequate secondary voltage, and the expense of high-speed comparators and op-amps, has proved primary-side data detection to be challenging, particularly with the tight cost constraints imposed by the application.

#### VII. CONCLUSION

The use of planar coreless PCB transformers has received some interest due to the advent of wireless inductive charging systems; however, such transformers they have not seen significant use as a power and signal transfer device in commercial electronics. This paper presented the concept of a isolated, lowcost, modular data acquisition module designed for use in a distributed multi-sensor, single-host environment. Specifically,

planar coreless PCB transformers were introduced and typical design processes and calculations were presented. The paper experimentally verified the viability of the use of the coreless transformers for the module's isolated power, clock and data signals. The experimental data presented is considered to be typical of a two-winding coreless PCB transformer, and the calculations and models may be used to represent any such coreless PCB transformer design.

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