

## CS 3120 Exam 2

This packet contains exam 1. This **cover sheet** is here to provide instructions, and to cover the questions until the quiz begins. **do not open this quiz packet** until your proctor instructs you to do so.

You will have 1 hour and 45 minutes to complete this exam. Each quiz is two pages (front and back of one sheet of paper) worth of questions. Make sure to **write your name and computing id at the top of each individual page**.

When you are finished, simply submit this packet at the front of the classroom.

This quiz is CLOSED text book, closed-notes, closed-calculator, closed-cell phone, closed-computer, closed-neighbor, etc. Questions are worth different amounts, so be sure to look over all the questions and plan your time accordingly. Please sign the honor pledge below.

*A crash reduces  
Your expensive computer  
To a simple stone.*

**Module 3: Context-Free Grammars****Name** \_\_\_\_\_

1. [6 points] Answer the following True/False questions.

<i>PDA</i> s are allowed to use <i>non-determinism</i>	<b>True</b>	<b>False</b>
It is possible for a <i>context-free grammar</i> to generate only the empty string.	<b>True</b>	<b>False</b>
It is possible to write a working <i>context-free grammar</i> for the language $\Sigma^*$	<b>True</b>	<b>False</b>
$a^x b^y c^y d^x$ is a <i>context-free language</i>	<b>True</b>	<b>False</b>
A <i>PDA</i> 's stack can overflow, and in this case the machine always <i>rejects</i>	<b>True</b>	<b>False</b>
A <i>PDA</i> that has access to a <i>queue</i> is computationally equivalent to a <i>PDA</i> that has access to a <i>stack</i>	<b>True</b>	<b>False</b>

2. [2 points] Draw a *PDA* for the following language:  $C = \{ww^R \mid w \in \Sigma^*\}$

3. [2 points] Write out a *context-free grammar* for the following language:  $D = 1^*0^n1^n0^*$

**Module 4: Turing Machines****Name** \_\_\_\_\_

4. [6 points] Answer the following True/False questions.

A <i>Turing Machine</i> with a two-dimensional (infinite in both dimensions) tape is computationally more powerful than a <i>single-tape Turing Machine</i>	<b>True</b>	<b>False</b>
Some <i>recognizers</i> never <i>halt and reject</i> on any input	<b>True</b>	<b>False</b>
If a language $A$ is <i>decidable</i> , then the complement $\bar{A}$ is also <i>decidable</i>	<b>True</b>	<b>False</b>
$a^n b^n c^n$ is <i>turing-decidable</i>	<b>True</b>	<b>False</b>
<i>Turing Machines</i> can be run (simulated) on other <i>Turing Machines</i> to see how they behave on various input strings	<b>True</b>	<b>False</b>
The <i>turing-recognizable</i> languages are closed under <i>complement</i>	<b>True</b>	<b>False</b>

5. [2 points] Suppose you have a *recognizer* for the problem  $A$  (call it  $R$ ) and a *recognizer* for the complement  $\bar{A}$  (call it  $R'$ ). Describe an algorithm that *decides*  $A$ .6. [2 points] In your own words, explain how we were able to reduce  $A_{TM}$  to the *Halting Problem*. Describe the reduction informally (or formally if you prefer) in your answer.

**Miscellaneous**

7. [3 points] In class, we discussed how *detecting properties of Turing Machines* was often undecidable (e.g., emptiness testing) but *detecting properties of DFAs* was always decidable. At an intuitive level, why is this the case?
8. [3 points] Suppose I have a *grammar* for a language  $A$  with a start variable  $S_A$  and another grammar for a language  $B$  with a start variable  $S_B$ . Describe how I can combine these grammars by adding one new variable and one new rule to create the grammar for  $C = AB$  (that's  $A$  concatenated with  $B$ ). *HINT: your one new variable will be the start variable of the new union language.*
9. [3 points] Show that  $a^n b^n c^n$  is not context-free. You can use any technique you would like.