## Factoring using Mixed Methods

A. Factor completely the given polynomial expressions.

1) 
$$36x^4 - 13x^2 + 1$$

2) 
$$9x^5 - 4x^3 - 9x^2 + 4$$

Factored Form: (2x-1)(2x+1)(3x-1)(3x+1)

Factored Form: 
$$(x-1)(3x-2)(3x+2)(x^2+x+1)$$

## Remainder Theorem

B. Give the remainder of each of the following expressions using remainder theorem.

1) 
$$(2x^3 + 3x^2 - 8x - 12) \div (2 - x)$$

2) 
$$(-2x^3 + 2x^2 + 2x - 2) \div (-2x - 2)$$

Remainder: 45

Remainder: 0

## Factor Theorem

C. State if the given binomial is a factor of the given polynomial.

1) 
$$(2x^4 + x^3 - 6x^2 + x + 2) \div (2 - 2x)$$

2) 
$$(2x^3 + 7x^2 + 2x - 3) \div (2x + 2)$$

Answer: Factor

Answer: Factor

## **Rational Root Theorem**

D. Identify the nature of the roots (table of variations), the number of roots (FTA), possible roots, actual roots and the factored form of the given polynomial.

1) 
$$f(x) = x^3 + 3x^2 - x - 3$$

2) 
$$f(x) = x^4 + 5x^3 + x^2 - 21x - 18$$

FTA: Atmost 3

Factored form: (x-1)(x+1)(x+3)

Actual roots: -3, -1, 1

FTA: Atmost 4

Factored form:  $(x-2)(x+1)(x+3)^2$ Actual roots: -3 mul. 2, -1, 2