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```
% TTK4135 - Helicopter lab
% Hints/template for problem 2.
% Updated spring 2018, Andreas L. Flåten
```

## Initialization and model definition

```
close
clear

init_simulator; % Change this to the init file corresponding to your
helicopter

% Discretize model
% Discrete time system model. x = [lambda r p p_dot]'
delta_t = 0.25; % sampling time

Ac = [0 1 0 0;
      0 0 -K_2 0;
      0 0 0 1;
      0 0 -K_1*K_pp -K_1*K_pd];

Bc = [0; 0; 0; K_1*K_pp];

A1 = eye(4)+delta_t*Ac;
B1 = delta_t*Bc;

% A1 = [1 0.25 0 0;
%       0 0.9925 -0.0975 0;
%       0 0 1 0.25;
%       0 0 -1.7825 0.1];
% B1 = [0; 0; 0; 1.685];

Number of states and inputs

mx = size(A1,2); % Number of states (number of columns in A)
mu = size(B1,2); % Number of inputs(number of columns in B)

% Initial values
x1_0 = pi; % Lambda
x2_0 = 0; % r
x3_0 = 0; % p
x4_0 = 0; % p_dot
```

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```

x0 = [x1_0 x2_0 x3_0 x4_0]'; % Initial values

% Time horizon and initialization
N = 100; % Time horizon for states
M = N; % Time horizon for inputs
z = zeros(N*mx+M*mu,1); % Initialize z for the whole
horizon
z0 = z; % Initial value for
optimization

% Bounds
ul = -pi/6; % Lower bound on control
uu = pi/6; % Upper bound on control

xl = -Inf*ones(mx,1); % Lower bound on states (no
bound)
xu = Inf*ones(mx,1); % Upper bound on states (no
bound)
xl(3) = ul; % Lower bound on state x3
xu(3) = uu; % Upper bound on state x3

% Generate constraints on measurements and inputs
[vlb,vub] = gen_constraints(N,M,xl,xu,ul,uu); % hint:
gen_constraints
vlb(N*mx+M*mu) = 0; % We want the last input to be
zero
vub(N*mx+M*mu) = 0; % We want the last input to be
zero

% Generate the matrix Q and the vector c (objective function weights
in the QP problem)
Q1 = zeros(mx,mx);
Q1(1,1) = 1; % Weight on state x1
Q1(2,2) = 0; % Weight on state x2
Q1(3,3) = 0; % Weight on state x3
Q1(4,4) = 0; % Weight on state x4
P1 = 10; % Weight on input
Q = gen_q(Q1,P1,N,M); % Generate Q, hint: gen_q
c = 0; % Generate c, this is the
linear constant term in the QP

```

## Generate system matrixes for linear model

```

Aeq = gen_aeq(A1,B1,N,mx,mu); % Generate A, hint: gen_aeq
beq = zeros(size(Aeq,1),1); % Generate b
beq(1) = pi;

```

## Solve QP problem with linear model

```

tic
[z,lambda] = quadprog(Q,[],[],[],Aeq,beq,vlb,vub); % hint: quadprog.
Type 'doc quadprog' for more info
t1=toc;

```

---

```

% Calculate objective value
phil = 0.0;
PhiOut = zeros(N*mx+M*mu,1);
for i=1:N*mx+M*mu
    phil=phil+Q(i,i)*z(i)*z(i);
    PhiOut(i) = phil;
end

```

## Extract control inputs and states

```

u = [z(N*mx+1:N*mx+M*mu);z(N*mx+M*mu)]; % Control input from solution

x1 = [x0(1);z(1:mx:N*mx)]; % State x1 from solution
x2 = [x0(2);z(2:mx:N*mx)]; % State x2 from solution
x3 = [x0(3);z(3:mx:N*mx)]; % State x3 from solution
x4 = [x0(4);z(4:mx:N*mx)]; % State x4 from solution

num_variables = 5/delta_t;
zero_padding = zeros(num_variables,1);
unit_padding = ones(num_variables,1);

u = [zero_padding; u; zero_padding];

x1 = [pi*unit_padding; x1; zero_padding];
x2 = [zero_padding; x2; zero_padding];
x3 = [zero_padding; x3; zero_padding];
x4 = [zero_padding; x4; zero_padding];

```

## Plotting

```

t = 0:delta_t:delta_t*(length(u)-1);

u = [t' u];

figure(2)
subplot(511)
stairs(t,u),grid
ylabel('u')
subplot(512)
plot(t,x1,'m',t,x1,'mo'),grid
ylabel('lambda')
subplot(513)
plot(t,x2,'m',t,x2,'mo'),grid
ylabel('r')
subplot(514)
plot(t,x3,'m',t,x3,'mo'),grid
ylabel('p')
subplot(515)
plot(t,x4,'m',t,x4,'mo'),grid
xlabel('tid (s)'),ylabel('pdot')

```

