

Question 1

- Sketch the energy level (Grotrian) diagram for a hydrogen atom. Use it to explain the atomic spectrum that is observed for hydrogen.
- What is meant by the term radial distribution function when discussing atomic orbitals? Sketch the radial distribution functions of the 2s and 2p orbitals of lithium.
- The principal series of lines in the emission spectrum of atomic lithium arise from the $np \rightarrow 2s$ transitions, where n is the principal quantum number. The first five lines in the series are observed at wavenumbers of 14 908, 30 935, 36 479, 39 024, and 40 399 cm^{-1} . Use a graphical method to estimate the ionization energy (expressed as a wavenumber, in cm^{-1}) of the 2s electron in lithium.
- In fact, under higher resolution, the $2p \rightarrow 2s$ transition in b) is split into a doublet separated by 0.3 cm^{-1} . Explain this observation.

Question 2

- Write down the Rydberg equation and explain briefly its value in analysis of atomic spectra of hydrogenic atoms. The lowest energy electronic transition in ground state hydrogen atoms occurs at a wavelength of 121.8nm, and the lowest energy transition in ground state helium occurs at a wavelength of 58.43 nm. Calculate the ratio of the Rydberg constants for hydrogen and helium.
- What is meant by a radial probability distribution function for an electron in an atom? In what way is it different from the radial wavefunction? Outline how a knowledge of the radial wavefunction can help explain the energy ordering of the s, p, and d orbitals in an atom.
- If helium gas is excited in an electrical discharge, an emission spectrum showing a large number of spectral lines is observed. Many of these lines are absent from the absorption spectrum of helium. Explain this observation as fully as possible.
- What is the Uncertainty Principle? Describe one experiment that provides evidence for the Uncertainty Principle.

Question 3

- Write notes on the following topics:
 - Principal quantum number, n
 - Orbital angular momentum quantum number, l
 - Spin quantum number, s
 - Magnetic quantum number, m_l
- The wavefunction for a $2p_z$ electron in a hydrogenic atom of atomic number Z is

$$\psi = Nr \cos \theta e^{-\frac{Zr}{2a_0}}$$

where a_0 is the Bohr radius and N is a normalisation constant.

- i. Normalise this wavefunction. For this step, you will need the integrals.

$$\int_0^{\infty} r^n e^{-ar} dr = \frac{n!}{a^{n+1}} \quad \int_0^{\pi} \cos^2 \theta \sin \theta d\theta = \frac{2}{3} \quad \int_0^{2\pi} d\phi = 2\pi$$

- ii. Evaluate the most probable distance of the electron from the nucleus.
 iii. Identify the most probable location of the electron in terms of r and θ .

Question 4

- a. Explain what is meant by the terms eigenfunction, eigenvalue and normalization constant.
- b. Show that: i) e^{ibt} ; and ii) $a \cos(bt + c)$; in which a , b and c are constants, are eigenfunctions of the operator $\frac{d^2}{dt^2}$. and in each case determine the associated eigenvalue.
- c. A simple model for the molecule β -carotene (whose structure is shown below) treats the π electrons as though they were confined to a one-dimensional box with infinitely high potential walls. The electrons can then be described according to the “particle-in-a-box” model, with each energy level able to accommodate a maximum of two electrons.
- What value must the wavefunction for the electrons in the box have at each end of the box? Why?
 - β -carotene is orange; in what region of the visible spectrum does it absorb light?
 - It is possible to synthesize molecules of structure similar to β -carotene, in which the length of the conjugated π system is greater than that in β -carotene. The energy of electrons confined to a one-dimensional box is given by what equation? How would the wavelength of the light absorbed by the π electrons be affected if the length of the conjugated system were increased? Justify your answer.

