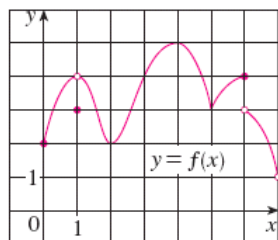


# Q1

Wednesday, October 7, 2020

7:12 PM

Use the graph to state the absolute and local maximum and minimum values of the function. (Assume each point lies on the gridlines. Enter your answers as a comma-separated list. If an answer does not exist, enter DNE.)



absolute maximum value

5



absolute minimum value

DNE



local maximum value(s)

4,5



local minimum value(s)

2,3



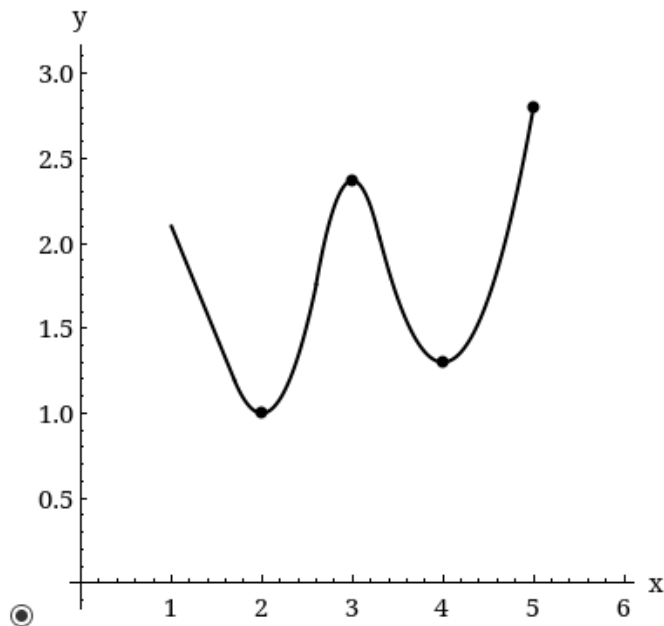
## Q2

Wednesday, October 7, 2020

7:18 PM

Sketch the graph of a function  $f$  that is continuous on  $[1, 5]$  and has the given properties.

Absolute maximum at 5, absolute minimum at 2, local maximum at 3, local minima at 2 and 4

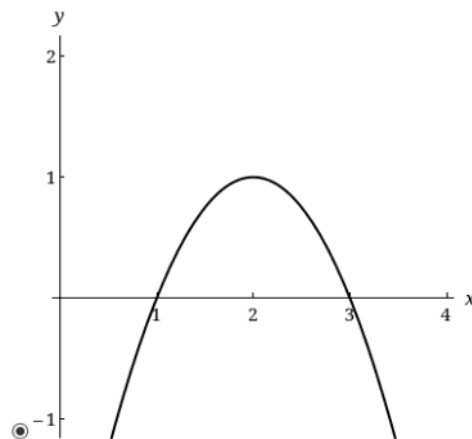


# Q3

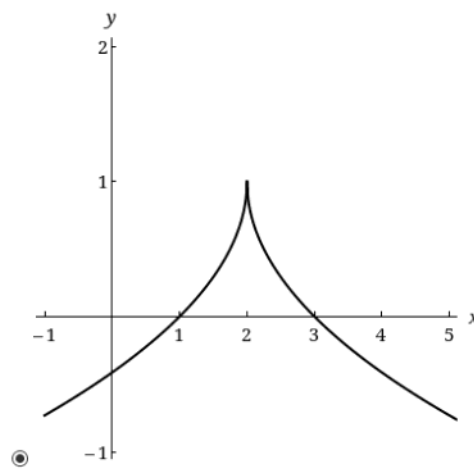
Wednesday, October 7, 2020

7:20 PM

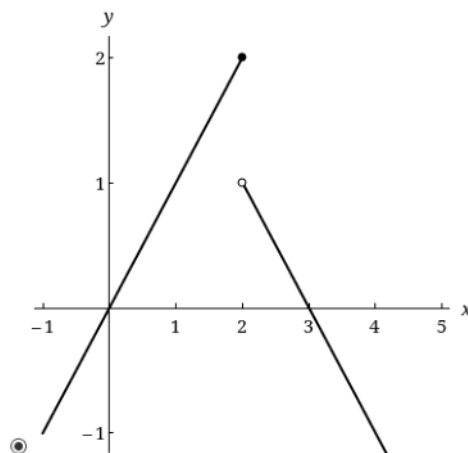
(a) Sketch the graph of a function that has a local maximum at 2 and is differentiable at 2.



(b) Sketch the graph of a function that has a local maximum at 2 and is continuous but not differentiable at 2.



(c) Sketch the graph of a function that has a local maximum at 2 and is not continuous at 2.

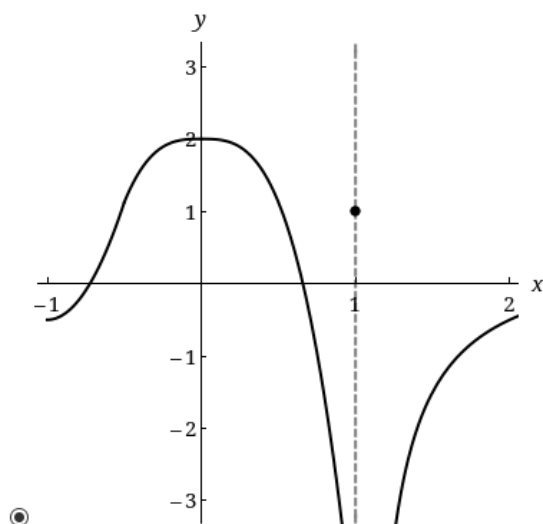


# Q4

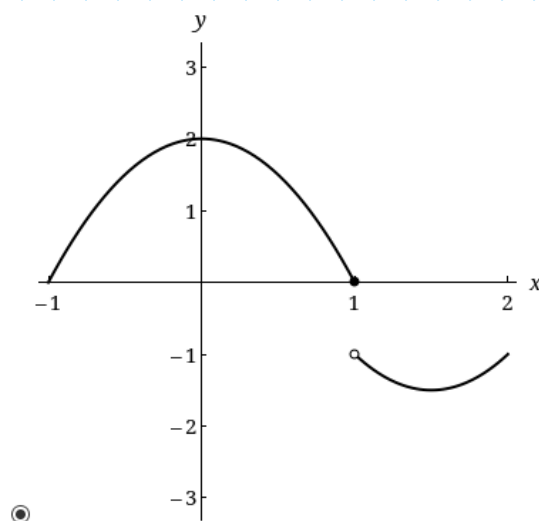
Wednesday, October 7, 2020

7:23 PM

(a) Sketch the graph of a function on  $[-1, 2]$  that has an absolute maximum but no absolute minimum.



(b) Sketch the graph of a function on  $[-1, 2]$  that is discontinuous but has both an absolute maximum and an absolute minimum.



## Q5

Wednesday, October 7, 2020 7:29 PM

Sketch the graph of  $f$  by hand and use your sketch to find the absolute and local maximum and minimum values of  $f$ . (Enter your answers as a comma-separated list. If an answer does not exist, enter DNE.)

$$f(x) = \frac{1}{2}(5x - 1), \quad x \leq 3$$

absolute maximum value

7



absolute minimum value

DNE



local maximum value(s)

DNE

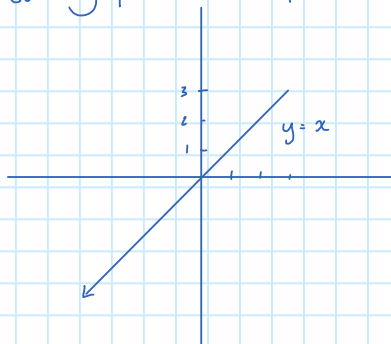


local minimum value(s)

DNE

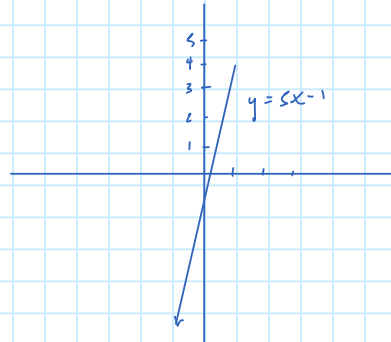
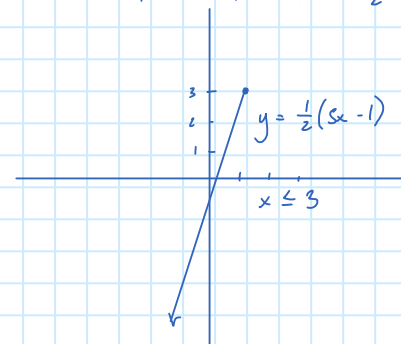


$$f(x) = \frac{1}{2}(5x - 1), \quad x \leq 3$$

starting point with slope of  $x$ 

$\frac{5}{1}$  rise over run  
shift down 1

with slope of  $5x - 1$

with slope of  $\frac{1}{2}(5x - 1)$  or  $\frac{5}{2}x - \frac{1}{2}$ 

Absolute Maximum

$$\begin{aligned} x = 3 \quad y &= f(3) \\ &= f(3) = \frac{1}{2}(5(3) - 1) \\ &= \frac{1}{2}(15 - 1) \\ &= \frac{1}{2}(14) \\ y &= 7 \end{aligned}$$

= 7

Since the function of  $f$  is linear for  $x \leq 3$ 

Absolute Minimum

= DNE

Local maximum

= DNE

Local minimum

= DNE

# Q6

Thursday, October 8, 2020 4:27 PM

Sketch the graph of  $f$  by hand and use your sketch to find the absolute and local maximum and minimum values of  $f$ . (Enter your answers as a comma-separated list. If an answer does not exist, enter DNE.)

$$f(x) = \frac{2}{x}, \quad x \geq 2$$

absolute maximum value	<input type="text" value="1"/>	✓
absolute minimum value	<input type="text" value="DNE"/>	✓
local maximum value(s)	<input type="text" value="DNE"/>	✓
local minimum value(s)	<input type="text" value="DNE"/>	✓

Absolute maximum

$$f(x) = \frac{2}{x}, \quad x \geq 2$$

$$f(2) = \frac{2}{2} = 1$$

$$= 1$$

Since the function of  $f$  is linear for  $x \geq 2$

Absolute Minimum

$$= \text{DNE}$$

Local maximum

$$= \text{DNE}$$

Local minimum

$$= \text{DNE}$$

## Q7

Thursday, October 8, 2020 4:34 PM

Sketch the graph of  $f$  by hand and use your sketch to find the absolute and local maximum and minimum values of  $f$ . (Enter your answers as a comma-separated list. If an answer does not exist, enter DNE.)

$$f(x) = \sin(x), \quad 0 \leq x < \frac{\pi}{2}$$

absolute maximum value  ✓

absolute minimum value  ✓

local maximum value(s)  ✓

local minimum value(s)  ✓

Absolute maximum for  $0 \leq x < \frac{\pi}{2}$

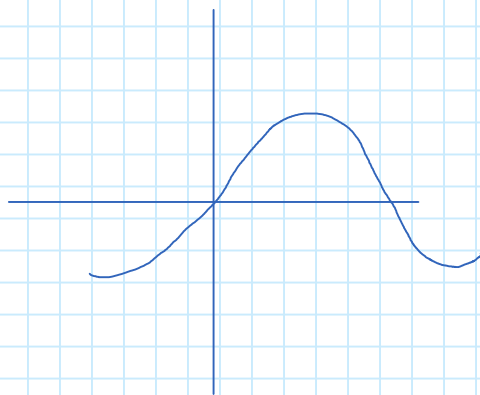
$x$  is ONLY less than  $\frac{\pi}{2}$ , not including  $\frac{\pi}{2}$ . So, the absolute maximum is infinite as  $x$  approaches  $\frac{\pi}{2}$ .

$\therefore$  Absolute maximum

Absolute minimum for  $0 \leq x < \frac{\pi}{2}$

$$\begin{aligned} y &= f(x) \\ f(0) &= \sin(x) \\ &= \sin(0) \\ &= 0 \end{aligned}$$

Graph of  $\sin(x)$



$\therefore$  Local maximum   
and  
Local minimum

## Q8

Thursday, October 8, 2020 4:44 PM



$$y = \cos(x)$$

$$f(t) = 2\cos(t), \quad -\frac{3\pi}{2} \leq t \leq \frac{3\pi}{2}$$

Abs &amp; Local max

$$= 1(2)$$

$$= \boxed{2}$$

Abs &amp; Local min

$$= -1(2)$$

$$= \boxed{-2}$$



## Q9

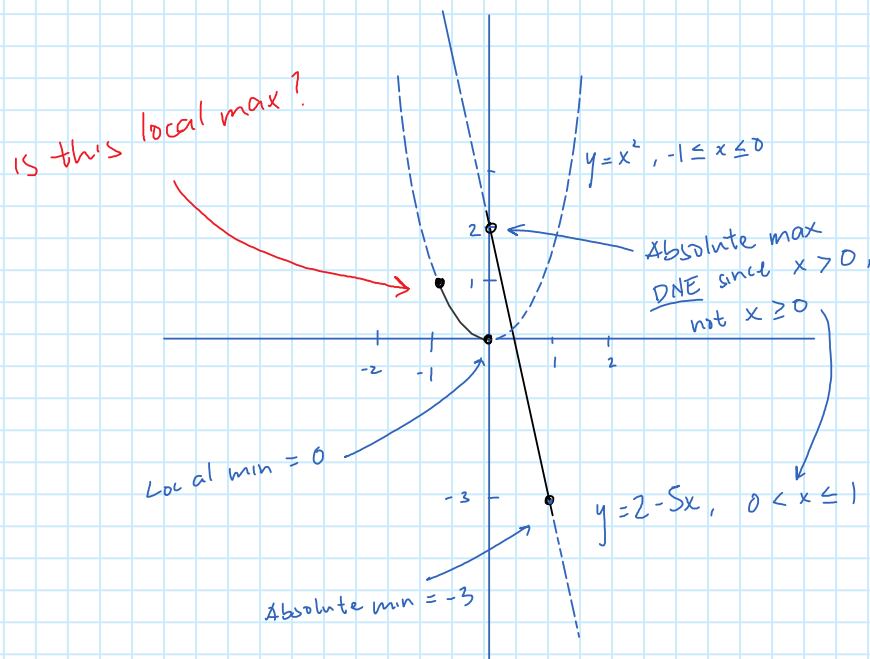
Thursday, October 8, 2020 8:54 PM

Sketch the graph of  $f$  by hand and use your sketch to find the absolute and local maximum and minimum values of  $f$ . (Enter your answers as a comma-separated list. If an answer does not exist, enter DNE.)

$$f(x) = \begin{cases} x^2 & \text{if } -1 \leq x \leq 0 \\ 2 - 5x & \text{if } 0 < x \leq 1 \end{cases}$$

absolute maximum value absolute minimum value local maximum value(s) local minimum value(s) 

Professor Wayne  
isn't convinced with  
this as well



Absolute max

$$y = f(x)$$

$$\begin{aligned} f(1) &= 2 - 5x \\ &= 2 - 5(1) \\ &= -3 \end{aligned}$$

Absolute min

= DNE

Local max

= DNE

Local min

$$y = f(0)$$

$$\begin{aligned} f(0) &= x^2 \\ &= 0^2 \\ &= 0 \end{aligned}$$

# Q10

Thursday, October 8, 2020 9:24 PM

Find the critical numbers of the function. (Enter your answers as a comma-separated list. If an answer does not exist, enter DNE.)

$$f(x) = 4 + \frac{1}{3}x - \frac{1}{2}x^2$$

$$x = \frac{1}{3}$$



$$f(x) = 4 + \frac{1}{3}x - \frac{1}{2}x^2$$

$$m = f'(x)$$

critical numbers of a function  
are where slope = 0 or undefined

$$f'(x) = \frac{d}{dx} \left( 4 + \frac{1}{3}x - \frac{1}{2}x^2 \right)$$

$$= 0 + \frac{1}{3} - (2) \frac{1}{2}x$$

$$f'(x) = \frac{1}{3} - x$$

$$\frac{1}{3} - x = 0$$

$$x = \frac{1}{3}$$

# Q11

Thursday, October 8, 2020 9:47 PM

Find the critical numbers of the function. (Enter your answers as a comma-separated list. If an answer does not exist, enter DNE.)

$$f(x) = 2x^3 - 3x^2 - 12x$$

$$x = 2, -1$$



$$f(x) = 2x^3 - 3x^2 - 12x$$

$$m = f'(x)$$

$$f'(x) = \frac{d}{dx}(2x^3 - 3x^2 - 12x)$$

$$= (3)2x^2 - (2)3x - 12$$

$$f'(x) = 6x^2 - 6x - 12$$

critical numbers of a function  
are where slope = 0 or undefined

$$6x^2 - 6x - 12 = 0$$

$$6(x^2 - x - 2) = 0$$

$$6(x-2)(x+1) = 0$$

$$\begin{array}{l} \swarrow \quad \searrow \\ x-2=0 \quad x+1=0 \end{array}$$

$$x = 2$$

$$x = -1$$

# Q12

Thursday, October 8, 2020 10:00 PM

Find the critical numbers of the function. (Enter your answers as a comma-separated list. If an answer does not exist, enter DNE.)

$$g(y) = \frac{y-1}{y^2-3y+3}$$

$$y = 0, 2$$

critical numbers of a function  
are where slope = 0 or undefined

$$g(y) = \frac{y-1}{y^2-3y+3}$$

$$m = g'(y)$$

$$g'(y) = \frac{d}{dy} \left( \frac{y-1}{y^2-3y+3} \right)$$

$$= \frac{(y^2-3y+3) \frac{d}{dy}(y-1) - (y-1) \frac{d}{dy}(y^2-3y+3)}{(y^2-3y+3)^2}$$

$$= \frac{(y^2-3y+3)(1) - (y-1)(2y-3)}{(y^2-3y+3)^2}$$

$$= \frac{y^2-3y+3 - (2y^2-5y+3)}{(y^2-3y+3)^2}$$

$$= \frac{y^2-3y+3-2y^2+5y-3}{(y^2-3y+3)^2}$$

$$g'(y) = \frac{-y^2+2y}{(y^2-3y+3)^2}$$

$$\frac{-y^2+2y}{(y^2-3y+3)^2} = 0 \longrightarrow \text{only way a fraction equals to 0 is if the numerator equals to 0}$$

$$-y^2+2y = 0$$

$$-y(y-2) = 0$$

$$\begin{array}{l} \swarrow \quad \searrow \\ \boxed{y=0} \quad y+2=0 \\ \quad \quad \quad \boxed{y=-2} \end{array}$$

The Quotient Rule

$$\frac{d}{dx} \left[ \frac{f(x)}{g(x)} \right] = \frac{g(x) \frac{d}{dx}[f(x)] - f(x) \frac{d}{dx}[g(x)]}{[g(x)]^2}$$

## Q13

Thursday, October 8, 2020 10:25 PM

Find the critical numbers of the function. (Enter your answers as a comma-separated list. Use  $n$  to denote any arbitrary integer values. If an answer does not exist, enter DNE.)

$$f(\theta) = 4 \cos(\theta) + 2 \sin^2(\theta)$$

$$\theta = k\pi$$



$$f(\theta) = 4 \cos(\theta) + 2 \sin^2(\theta)$$

$$m = f'(\theta)$$

$$f'(\theta) = \frac{d}{dx} [4 \cos(\theta) + 2 \sin^2(\theta)]$$

$$= 4 \frac{d}{dx} [\cos(\theta)] + 2 \frac{d}{dx} [(\sin(\theta))^2]$$

$$= 4(-\sin(\theta)) + 2 \frac{dy}{du} (u^2) \frac{du}{dx} (u)$$

$$= -4 \sin(\theta) + 2 [2 \sin(\theta)] \frac{d}{dx} [\sin(\theta)]$$

$$= -4 \sin(\theta) + 4 \sin(\theta) \cos(\theta)$$

$$f'(\theta) = 4 \sin(\theta) [-1 + \cos(\theta)]$$

$$4 \sin(\theta) [-1 + \cos(\theta)] = 0$$



$$\sin(\theta) = 0$$

$$0, \pi, 2\pi, \dots$$



$$-1 + \cos(\theta) = 0$$

$$\cos(\theta) = 1$$

$$0, 2\pi, 4\pi, \dots$$

$$\theta = k\pi$$

critical numbers of a function  
are where slope = 0 or undefined

chain rule

$$u = \sin(\theta)$$

$$f(u) = u^2 = y$$

$$\frac{dy}{du} \quad \frac{du}{dx}$$

## Q14

Thursday, October 8, 2020 10:43 PM

Find the absolute maximum and absolute minimum values of  $f$  on the given interval.

$$f(x) = 12 + 2x - x^2, \quad [0, 5]$$

absolute minimum value

-3



absolute maximum value

13



$$f(x) = 12 + 2x - x^2, \quad [0, 5]$$

Get all critical numbers

$$f'(x) = \frac{d}{dx}(12 + 2x - x^2)$$

$$= 0 + 2 - 2x$$

$$f'(x) = 2 - 2x$$

$$2 - 2x = 0$$

$$-2x = -2$$

$$x = 1$$

critical numbers of a function  
are where slope = 0 or undefined

$$f(5) = 12 + 2(5) - (5)^2$$

$$= 12 + 10 - 25$$

$$= 22 - 25$$

$$= -3 = \text{absolute min}$$

$$f(0) = 12 + 2(0) - (0)^2$$

$$= 12$$

$$f(1) = 12 + 2(1) - (1)^2$$

$$= 12 + 2 - 1$$

$$= 13 = \text{absolute max}$$

## Q15

Thursday, October 8, 2020 10:53 PM

Find the absolute maximum and absolute minimum values of  $f$  on the given interval.

$$f(x) = 2x^3 - 6x^2 - 18x + 3, \quad [-2, 4]$$

absolute minimum value

-51



absolute maximum value

13



$$f(x) = 2x^3 - 6x^2 - 18x + 3, \quad [-2, 4]$$

Get all critical numbers

critical numbers of a function are where slope = 0 or undefined

$$\begin{aligned} f'(x) &= \frac{d}{dx}(2x^3 - 6x^2 - 18x + 3) \\ &= (3)2x^2 - (2)6x - 18 + 0 \\ f'(x) &= 6x^2 - 12x - 18 \end{aligned}$$

$$\begin{aligned} f(4) &= 2x^3 - 6x^2 - 18x + 3 \\ &= 2(4)^3 - 6(4)^2 - 18(4) + 3 \\ &= -37 \end{aligned}$$

$$6x^2 - 12x - 18 = 0$$

$$6(x^2 - 2x - 3) = 0$$

$$6(x-3)(x+1) = 0$$

$$\begin{array}{cc} \downarrow & \downarrow \\ x-3=0 & x+1=0 \\ \underline{x=3} & \underline{x=-1} \end{array}$$

$$\begin{aligned} f(-2) &= 2x^3 - 6x^2 - 18x + 3 \\ &= 2(-2)^3 - 6(-2)^2 - 18(-2) - 3 \\ &= -1 \end{aligned}$$

$$\begin{aligned} f(-1) &= 2x^3 - 6x^2 - 18x + 3 \\ &= 2(-1)^3 - 6(-1)^2 - 18(-1) - 3 \\ &= 13 \rightarrow \text{Absolute max} \end{aligned}$$

$$\begin{aligned} f(3) &= 2x^3 - 6x^2 - 18x + 3 \\ &= 2(3)^3 - 6(3)^2 - 18(3) + 3 \\ &= -51 \rightarrow \text{Absolute min} \end{aligned}$$

## Q16

Friday, October 9, 2020

6:13 PM

$$f(x) = x + \frac{1}{x}, [0.2, 4]$$

critical numbers of a function  
are where slope = 0 or undefined

Get all critical numbers

$$\begin{aligned} f'(x) &= \frac{d}{dx} \left( x + \frac{1}{x} \right) \\ &= \frac{d}{dx} \left( x + x^{-1} \right) \\ &= 1 + (-x^{-2}) \end{aligned}$$

$$f'(x) = 1 - x^{-2}$$

$$1 - x^{-2} = 0$$

$$1 - \frac{1}{x^2} = 0$$

$$(-x^2) \cdot \frac{1}{x^2} = -1(-x^2)$$

$$1 = x^2$$

$$x = \sqrt{1}$$

$$x = \pm 1$$

Domain of  $f$  is  $[0.2, 4]$

$\therefore x = 1$  is the only  
critical point

$$\begin{aligned} f(4) &= x + \frac{1}{x} \\ &= (4) + \frac{1}{(4)} \\ &= \frac{17}{4} = 4.25 \end{aligned}$$

$$\begin{aligned} f(0.2) &= x + \frac{1}{x} \\ &= (0.2) + \frac{1}{(0.2)} \\ &= 5.2 \rightarrow \text{Absolute max} \end{aligned}$$

$$\begin{aligned} f(1) &= x + \frac{1}{x} \\ &= (1) + \frac{1}{(1)} \\ &= 2 \rightarrow \text{Absolute min} \end{aligned}$$



# Q17

Friday, October 9, 2020 6:53 PM

After the consumption of an alcoholic beverage, the concentration of alcohol in the bloodstream (blood alcohol concentration, or BAC) surges as the alcohol is absorbed, followed by a gradual decline as the alcohol is metabolized. The function

$$C(t) = 1.35te^{-2.802t}$$

models the average BAC, measured in mg/mL, of a group of eight male subjects  $t$  hours after rapid consumption of 15 mL of ethanol (corresponding to one alcoholic drink). What is the maximum average BAC during the first 2 hours? (Round your answer to three decimal places.)

0.177 ✓ mg/mL

When does it occur? (Round your answer to two decimal places.)

0.36 ✓ h

Domain of  $C(t)$  in hours

$C(t) = 1.35te^{-2.802t}$ ,  $[0, 2]$

Get all critical numbers

$C'(t) = \frac{d}{dx}(1.35te^{-2.802t})$

$$= 1.35 \frac{d}{dx}(te^{-2.802t})$$

$$= 1.35 \left[ t \frac{d}{dx}(e^{-2.802t}) + e^{-2.802t} \frac{d}{dx}(t) \right]$$

$$= 1.35 \left[ t(e^{-2.802t}) \frac{d}{dx}(-2.802t) + e^{-2.802t}(1) \right]$$

$$= 1.35 \left( te^{-2.802t}(-2.802) + e^{-2.802t} \right)$$

$$= 1.35(-2.802te^{-2.802t} + e^{-2.802t})$$

$$C'(t) = 1.35(e^{-2.802t})(-2.802t + 1)$$

this will never be zero for any value of  $t$

this can be made zero

$$-2.802t + 1 = 0$$

$$-2.802t = -1$$

$$t = \frac{1}{2.802}$$

$t \approx 0.357h$

$f(2) = 1.35te^{-2.802t}$

$$= 1.35(2)e^{-2.802(2)}$$

$$\approx 0.009$$

$f(0) = 1.35te^{-2.802t}$

$$= 1.35(0)e^{-2.802(0)}$$

$$= 0$$

$f(0.357) = 1.35te^{-2.802t}$

$$= 1.35(0.357)e^{-2.802(0.357)}$$

$$\approx 0.177 \rightarrow \text{Absolute max within 2 hours}$$