

Chapter 5 (draft): Data Grammar

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1 Grammar

path var,			fomalize?
x_p			
pattern,			
$patc$	$::=$	x	y
		$(\overline{dpatc} :: x_p)$	
cast expressions,			
a, b, A, B, L	$::=$	x	y
		$a :: L$	cast ym
		\star	ym
		$(x : A) \rightarrow B$	y
		$\text{fun } f x \Rightarrow b$	y
		$b a$	y
		D_Δ	type cons.
		d_Δ	data cons.
		$\text{case } \overline{a}, \left\{ \overline{ patc \Rightarrow b patc'_\ell} \right\}$	data elim.
		$!_L$	force blame
		$\{\overline{a},\}_L$	connected expressions ym
		$a \sim_{\ell,o}^L b$	assertion y (without ℓ)m
		x_p	
		$Arg L$	y
		$Bod_a L$	y
		$App_a L$	y
		$TCon_i L$	
		$DCon_i L$	
observations,			
o	$::=$	$.$	
		$o.Arg$	
		$o.App_a$	
		$o.Bod_a$	application
		$o.TCon_i$	type cons. arg.
		$o.DCon_i$	data cons. arg.
		$inEx_{\overline{patc}}[\overline{a}]$	in-exhaustive pattern match
contexts,			
Γ	$::=$	$.$	y
		$x : A$	y
		$x_p : A \approx B$	
		$\Gamma, \text{data } D : \Delta \rightarrow \star \left\{ \overline{ d : \Theta \rightarrow D\overline{a} } \right\}$	data definition
		$\Gamma, \text{data } D : \Delta \rightarrow \star$	abstract data

2 Judgment Forms

Main judgments

$\Gamma \vdash a \sqsupseteq a' : A'$ a has endpoint a' at type A'

Γ **Empty** type context only contains data defs

$a \rightsquigarrow b$ a steps to b

a **Val** value

a **Blame** $_{\ell,o}$ a contains contradiction is observable at o induced at source location ℓ

Derived Judgment

$\Gamma \vdash a : A$ $\Gamma \vdash a \sqsupseteq a : A$, type

Internal judgments

$\Gamma \vdash a \equiv a' : A$ definitional equivalence

$\bar{a} \rightsquigarrow \bar{b}$ a steps to b

\bar{a} **Val** values