Problem Set 1

Applied Stats/Quant Methods 1

Due: October 1, 2021

Instructions

- Please show your work! You may lose points by simply writing in the answer. If the problem requires you to execute commands in R, please include the code you used to get your answers. Please also include the .R file that contains your code. If you are not sure if work needs to be shown for a particular problem, please ask.
- Your homework should be submitted electronically on GitHub in .pdf form.
- This problem set is due before 8:00 on Friday October 1, 2021. No late assignments will be accepted.
- Total available points for this homework is 100.

Question 1 (50 points): Education

A school counselor was curious about the average of IQ of the students in her school and took a random sample of 25 students' IQ scores. The following is the data set:

- 1. Find a 90% confidence interval for the average student IQ in the school.
- 2. Next, the school counselor was curious whether the average student IQ in her school is higher than the average IQ score (100) among all the schools in the country.

Using the same sample, conduct the appropriate hypothesis test with $\alpha = 0.05$.

Problem 1 - My Answer (R code)

```
2 # Problem 1 = My Answer
_{5} # Because the sample or n < 30 a t-distribution can be used as opposed to a
     normal distribution
6 # t-distribution is a type of probability distribution. used where the sample
      size is small.
8 # The sample size is 25
y \leftarrow c(105, 69, 86, 100, 82, 111, 104, 110, 87, 108, 87, 90, 94, 113, 112, 98,
      80, 97, 95, 111, 114, 89, 95, 126, 98)
# get the sample mean (x bar) of y which is 98.44
_{12} n \leftarrow length (y)
13 # sample mean
_{14} mean (y)
15 # standard deviation
16 sd (y)
(sd(y)/sqrt(n))
18 # CI of 90%
19 # From tables look for Degree of Freedom or DF of 24 and alpha level of 0.05
_{20} # this gives 1.71 or a t-score of 1.71
_{21} \# 1. 25 - 1 = 24
22 \# 2. 1 - .90 = .05 or the alpha level
_{23} # use alpha level of 0.05
c90 \leftarrow qt(.05, 24, lower.tail = FALSE)
25 c90
26 # CI tells us to take the mean of 98.44 and plus or minus 4.4778
lower \leftarrow mean(y) - c90*(sd(y)/sqrt(n))
upper \leftarrow \text{mean}(y) + c90*(sd(y)/sqrt(n))
29 # get the s or standard deviation of y which is 13.09287
30 #sd(y)
_{31} # Using a 90% confidence level and need to find the confidence interval
32 # Confidence Level or CI is the margin of error and written as
33 # CI is to do with how reliable the estimation is
34 \# 1.71 * 13.09287 / square root of 25 = 4.4778
35 \# 98.44 - 4.778 = 93.96 is the lower level
36 \# 98.44 + 4.778 = 102.92 is the upper level
37 c(lower, upper)
40 # t test can be used for small samples
t.test(y)
```

Problem 1 - My Answer - R console output

```
_2 > \# The sample size is 25
3 > y < -c(105, 69, 86, 100, 82, 111, 104, 110, 87, 108, 87, 90, 94, 113, 112,
     98, 80, 97, 95, 111, 114, 89, 95, 126, 98)
4 >
_{5} > \# get the sample mean (x bar) of y which is 98.44
6 > n \leftarrow length(y)
7 > \# sample mean
8 > mean(y)
9 [1] 98.44
10 > # standard deviation
11 > sd(y)
12 [1] 13.09287
solution 13 > (sd(y)/sqrt(n))
14 [1] 2.618575
_{15} > \# \text{ CI of } 90\%
_{16}> \# From tables look for Degree of Freedom or DF of 24 and alpha level of 0.05
_{17} > \# this gives 1.71 or a t-score of 1.71
18 > \# 1. \ 25 - 1 = 24
_{19} > \# \ 2. \ 1 - .90 = .05 or the alpha level
_{20} > \# use alpha level of 0.05
c90 \leftarrow qt(.05, 24, lower.tail = FALSE)
22 > c90
23 [1] 1.710882
_{24} > \# CI tells us to take the mean of 98.44 and plus or minus 4.4778
lower_lvl \leftarrow mean(y) - c90*(sd(y)/sqrt(n))
26 > upper_lvl \leftarrow mean(y) + c90*(sd(y)/sqrt(n))
_{27} > # get the s or standard deviation of y which is 13.09287
28 > \# sd(y)
29 > # Using a 90% confidence level and need to find the confidence interval
30 > # Confidence Level or CI is the margin of error and written as
31 > # CI is to do with how reliable the estimation is
_{32} > \# 1.71 * 13.09287 / square root of 25 = 4.4778
_{33} > \# 98.44 - 4.778 = 93.96 is the lower level
34 > \# 98.44 + 4.778 = 102.92 is the upper level
35 > c(lower_lvl, upper_lvl)
36 [1] 93.95993 102.92007
_{37} > \# t test can be used for small samples
38 > t.test(y)
    One Sample t-test
40 data: y
t = 37.593, df = 24, p-value < 2.2e-16
42 alternative hypothesis: true mean is not equal to 0
43 95 percent confidence interval:
    93.03553\ 103.84447
45 sample estimates:
46 mean of x
98.44
```

Question 2 (50 points): Political Economy

Researchers are curious about what affects the amount of money communities spend on addressing homelessness. The following variables constitute our data set about social welfare expenditures in the USA.

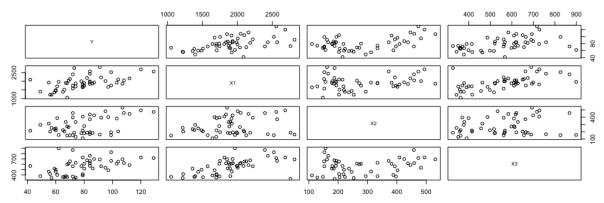
Explore the expenditure data set and import data into R.

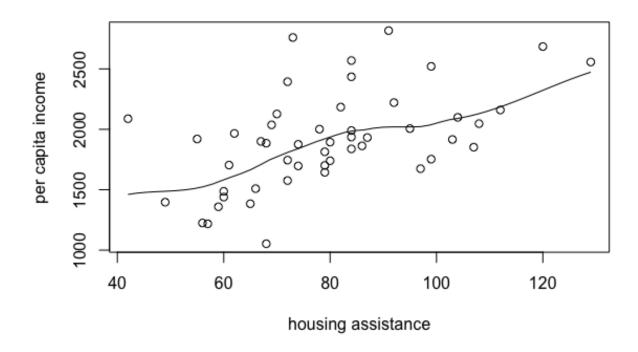
- Please plot the relationships among Y, X1, X2, and X3? What are the correlations among them (you just need to describe the graph and the relationships among them)?
- Please plot the relationship between Y and Region? On average, which region has the highest per capita expenditure on housing assistance?
- Please plot the relationship between Y and X1? Describe this graph and the relationship. Reproduce the above graph including one more variable Region and display different regions with different types of symbols and colors.

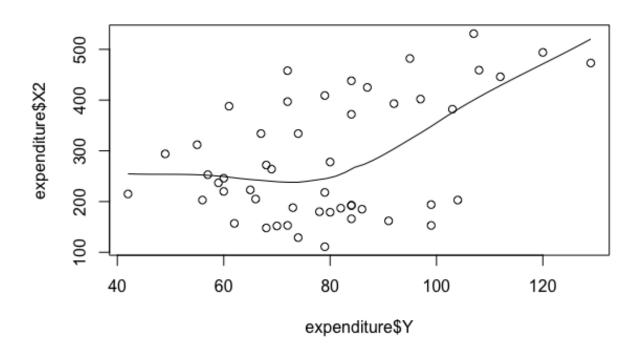
Problem 2 - My Answer (R code)

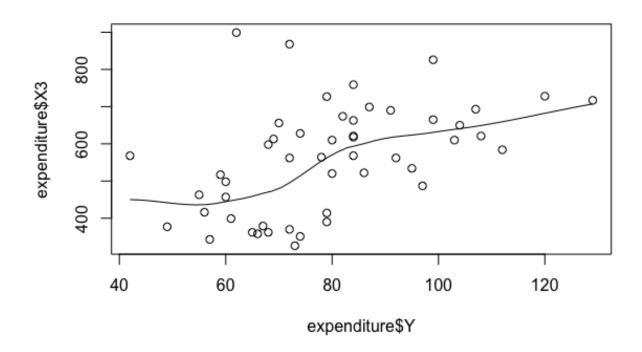
```
з # Problem 2 = My Answer
expenditure <- read.table("https://raw.githubusercontent.com/ASDS-TCD/StatsI_
     Fall2021/main/datasets/expenditure.txt", header=T)
7 str (expenditure)
8 # rows and columns 2 to 5
9 expenditure [2:5]
11 # This plots the relationships among Y, X1, X2, and X3
12 # using pairs() a matrix of scatter plots is produced
pairs (expenditure [2:5], main = "Correlation Matrix shown as a scatter plot")
14 # This shows that it is not correlated and is random
16 # Housing assistance and per capita expenditure / income
scatter.smooth(expenditure $Y, expenditure $X1, ylab="per capita income", xlab =
      "housing assistance")
18 # cor function calculates correlation among the vectors
19 # Region X1
20 # has the highest per capita on housing assistance
21 cor (expenditure $Y, expenditure $X1)
scatter.smooth(expenditure $Y, expenditure $X2)
23 # regions X2
24 cor (expenditure $Y, expenditure $X2)
scatter.smooth(expenditure$Y, expenditure$X3)
26 # Region X3
27 cor (expenditure $Y, expenditure $X3)
scatter.smooth(expenditure $X1, expenditure $X2)
```

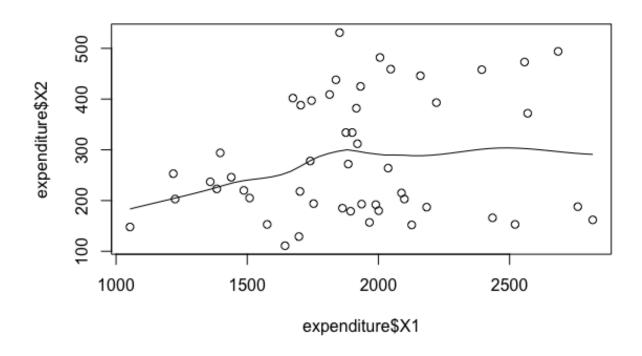
Correlation Matrix shown as a scatter plot











Problem 2 - My Answer - R console output

```
2 > expenditure <- read.table("https://raw.githubusercontent.com/ASDS-TCD/StatsI
       _{\rm L}Fall2021/main/datasets/expenditure.txt", header=T)
3 > str(expenditure)
  'data.frame': 50 obs. of
                                 6 variables:
                     "ME" "NH" "VT" "MA"
   $ STATE : chr
   $ Y
             : int
                     61 \ 68 \ 72 \ 72 \ 62 \ 91 \ 120 \ 99 \ 70 \ 82 \ \dots
   $ X1
                     1704 \ 1885 \ 1745 \ 2394 \ 1966 \ 2817 \ 2685 \ 2521 \ 2127 \ 2184 \ \dots
             : int
   $ X2
             : int
                     388\ \ 272\ \ 397\ \ 458\ \ 157\ \ 162\ \ 494\ \ 153\ \ 152\ \ 187\ \ \dots
   $ X3
             : int
                     399 \ 598 \ 370 \ 868 \ 899 \ 690 \ 728 \ 826 \ 656 \ 674 \ \dots
                     1 1 1 1 1 1 1 1 1 2 ...
   $ Region: int
_{11} > \# rows and columns 2 to 5
12 > expenditure [2:5]
        Y
             X1 X2
       61 1704 388 399
14 1
       68 1885 272 598
15
       72 1745 397 370
  3
17 4
       72 2394 458 868
       62 1966 157 899
  5
  6
       91 2817 162 690
19
      120 2685 494 728
  7
21 8
       99 \ 2521 \ 153 \ 826
       70 2127 152
  9
                     656
23 10
       82 2184 187
                     674
24 11
       84 1990 192 568
25 12
       84 2435 166 759
  13 104 2099 203 650
27 14
       84 1936 193 621
28 15 103 1916 382 610
29 16
       86 1863 185 522
  17
       69 2037 264 613
       74 1697 129 351
  18
32 19
       79 1644 111 390
  20
       80 1894 179 520
  21
       78 2001 180 564
  22
       73 2760 188 326
  23
       92 2221 393 562
  24
       97 1674 402 487
  25
       66 1509 205 358
  26
       65 \ 1384 \ 223 \ 362
40 27
       57 \ 1218 \ 253 \ 343
  28
       60 1487 220 498
  29
       74 1876 334 628
  30
       49 1397 294 377
44 31
       60 1439 246 457
       59 1359 237 517
  32
       68 1053 148 362
  33
47 34
       56 1225 203 416
48 35
       72 1576 153 562
```

```
49 36
      80 1740 278 610
50 37
      79 1814 409 727
  38
      55 1920 312 463
      79 1701 218 414
52 39
53 40
      42 \ 2088 \ 215 \ 568
54 41 108 2047 459 621
  42
      84 1838 438 618
56 43
      87 1932 425 699
  44
      99 1753 194 665
      84 2569 372 663
  45
59 46 112 2160 446 584
60 47
      95 2006 482 534
61 48 129 2557 473 717
62 49 67 1900 334 379
63 50 107 1852 531 693
64 >
65 > # This plots the relationships among Y, X1, X2, and X3
66 > # using pairs() a matrix of scatter plots is produced
67 > pairs (expenditure [2:5], main = "Correlation Matrix shown as a scatter plot")
68 > # This shows that it is not correlated and is random
69 >
70 > # Housing assistance and per capita expenditure / income
71 > scatter.smooth(expenditure$Y, expenditure$X1, ylab="per capita income", xlab
      = "housing assistance")
72 > # cor function calculates correlation among the vectors
73 > # Region X1
74 > # has the highest per capita on housing assistance
_{75} > cor(expenditure $Y, expenditure $X1)
76 [1] 0.5317212
77 > scatter.smooth(expenditure $Y, expenditure $X2)
78 > \# \text{ regions } X2
79 > cor (expenditure $Y, expenditure $X2)
80 [1] 0.4482876
s1 > scatter.smooth(expenditure $Y, expenditure $X3)
82 > \# \text{ Region X3}
83 > cor(expenditure $Y, expenditure $X3)
84 [1] 0.4636787
85 > scatter.smooth(expenditure$X1, expenditure$X2)
```