

## Quiz 1 - Monod's Nightmare

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Under ideal growing conditions in the laboratory, the population size of the common bacterium *Escherichia coli* can double in around 20 minutes. *E. coli*'s cells are rod-shaped and are roughly approximated by a rectangular box that is  $2\ \mu m$  long,  $1\ \mu m$  wide, and  $1\ \mu m$  high. ( $1\ \mu m = 1\ \text{micro-meter} = 1 \times 10^{-6}\ \text{meters} = 0.000001\ \text{m}$ ). For comparison, a strand of human hair is roughly  $100\ \mu m$  wide.

(a) Would a continuous-time model (the solution for which is  $N_t = N_0 e^{rt}$ ) or a discrete-time model (the solution for which is  $N_t = \lambda^t N_0$ ) be more appropriate for describing this population? Why?

(b) What is *E. coli*'s growth rate  $r$  (in minutes) under these ideal growing conditions. Express your answer by solving for the equation you would use to calculate  $r$  to the simplest solution possible.

(c) Let's assume that our classroom is roughly  $10\ m$  long,  $10\ m$  wide, and  $8\ m$  high (its not, I just made up these numbers). How long it would take for an exponentially growing population of *E. coli* under ideal conditions to fill our empty classroom when starting from a single individual bacterium?