

# AA 274A HW2

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## 1 Problem 1: A\* Motion Planning & Path Smoothing

### 1.1 Part i

After defining the functions "is\_free", "distance", "get\_neighbors", and "solve", I ran the "Simple Environment" example. The following is my resulting plot.

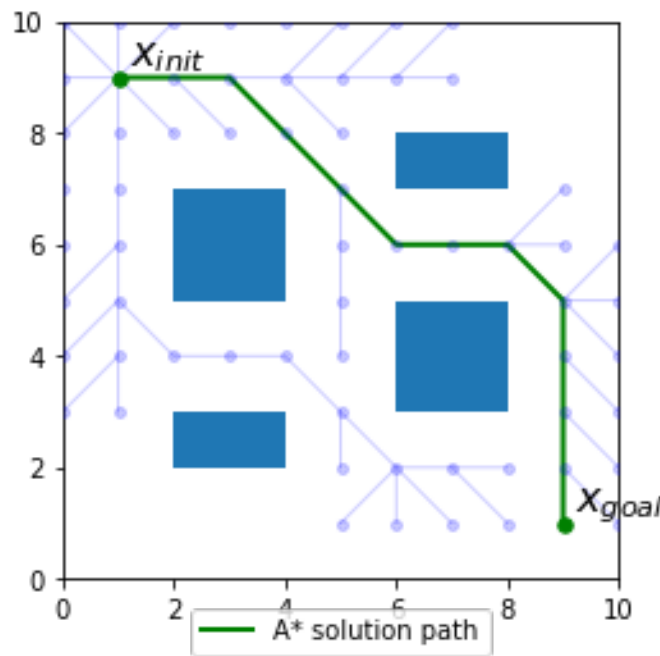


Figure 1: A\* Path Planning

## 1.2 Part ii

After implementing the function "compute\_smooth\_plan" to smooth our path, I ran the function on the "Simple Environment" example above. The resulting smoothed plot using  $\alpha = 0.03$  can be observed below.

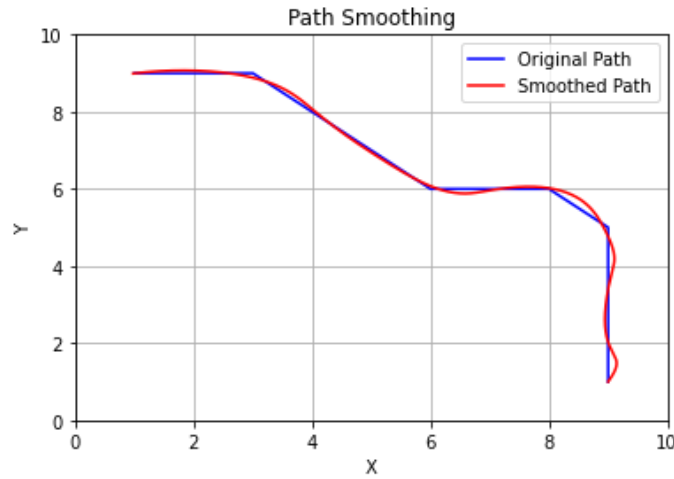


Figure 2: A\* Path vs Smoothed Path ( $\alpha = 0.03$ )

## 2 Problem 2: Rapidly-exploring Random Trees (RRT)

Collaborated with Anna Sulzer

### 2.1 Part i

After defining the functions "RRT.solve", "GeometricRRT.find\_nearest", and "GeometricRRT.steer\_towards", I ran the "Geometric Planning" example. The following is my resulting plot.

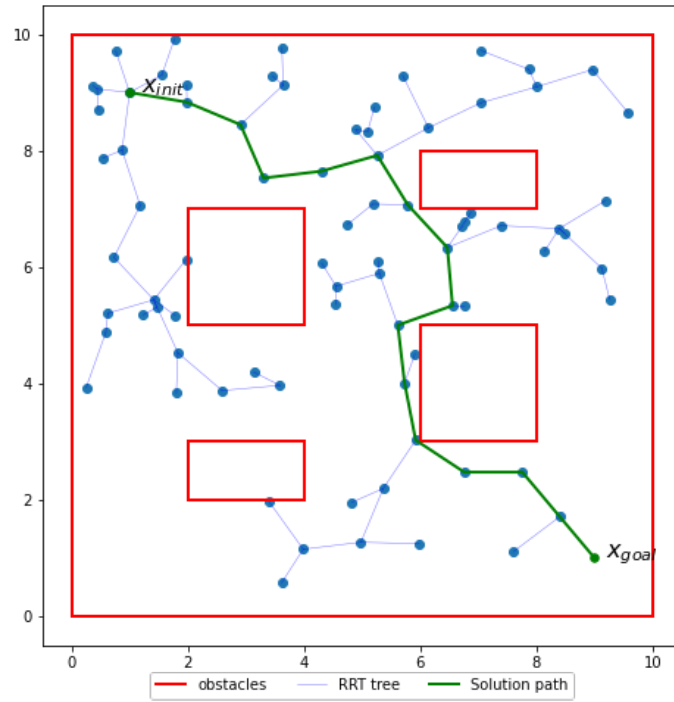


Figure 3: RRT Path Planning

## 2.2 Part ii

After implementing the function "RRT.shortcut\_path", I ran the code in the "Adding shortcutting" example. The following plot is my result.

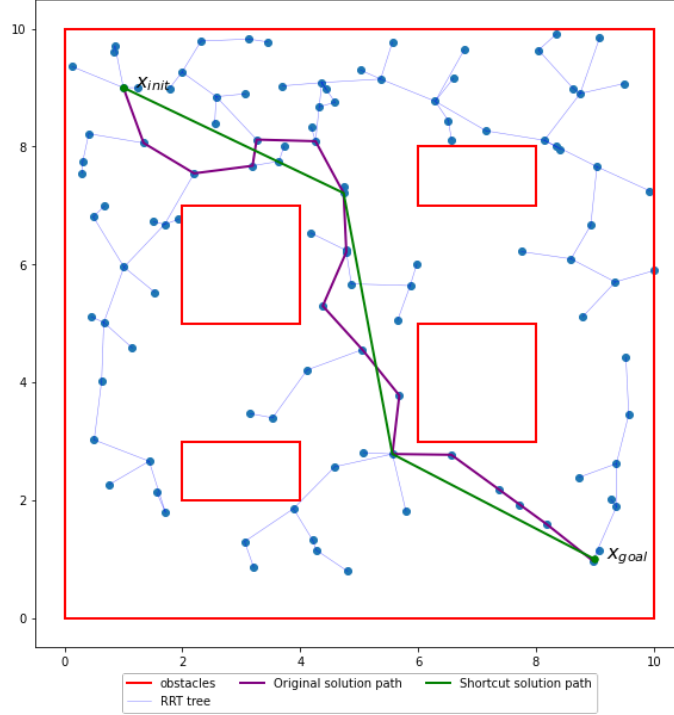


Figure 4: RRT Path Planning with Shortcut

### 3 Problem 3: LQR with gain scheduling

#### 3.1 Part i

The dimensionality of the state space for the quadcopter is 6. The values are as follows:

$x$  is the x position in the vertical plane

$y$  is the y position in the vertical plane

$v_x$  is the translational velocity in the x direction

$v_y$  is the translational velocity in the y direction

$\phi$  is the angle of pitch

$\omega$  is the pitching rate of the quadcopter

### 3.2 Part ii

The dimensionality of the control space of the quadcopter is 2. The values are as follows:

$T_1$  is the thrust for the left propeller

$T_2$  is the thrust for the right propeller

### 3.3 Part iii

The method used to solve for the trajectory is a direct method. This can be described by the equations

$$\min_{(x_i, u_i)} \sum_{i=0}^{N-1} \Delta t_i g(x_i, u_i, t_i)$$
$$x_{i+1} = x_i + \Delta t_i a(x_i, u_i, t_i), \quad i = 0, \dots, N-1$$
$$u_i \in U, \quad i = 0, \dots, N-1$$

### 3.4 Part iv

After writing the code for section "LQR Controller and Gain Scheduling", I ran the example and returned the following plot.

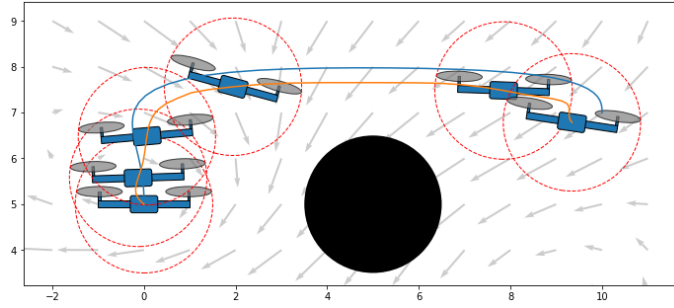


Figure 5: Drone Trajectory Plot