

10. Evaluate limit

$$\lim_{x \rightarrow 0} \frac{\sqrt{2x+4} - 2}{x}$$

substitute will lead to indeterminate form $\frac{0}{0}$

Therefore we need to manipulate

$$\frac{\sqrt{2x+4} - 2}{x} \left(\frac{\sqrt{2x+4} + 2}{\sqrt{2x+4} + 2} \right)$$

$$\frac{(\sqrt{2x+4})^2 - 2^2}{x(\sqrt{2x+4} + 2)} = \frac{2x+4-4}{x(\sqrt{2x+4} + 2)}$$

$$\frac{2x}{x(\sqrt{2x+4} + 2)} = \frac{2}{\sqrt{2x+4} + 2}$$

now we evaluate at $x=0$

$$\frac{2}{\sqrt{2(0)+4} + 2} =$$

$$\frac{2}{2+2} = \frac{1}{2}$$