Overview
Parallel performance
Quantifying parallel performance
Summary and next lecture

### **XJCO3221 Parallel Computation**

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Lecture 4: Theory of parallel performance

#### Previous lecture

In the last lecture we started to look at solving problems in parallel:

- Vector addition, which can be parallelised for shared memory systems by using the fork-join construct.
- Implemented in OpenMP as a single line just before the loop:
   #pragma omp parallel for
- Mandelbrot set, which has a nested loop.
- Both data parallel problems ('maps') as calculations in the loop are independent.
- Still difficult to achieve good performance for the Mandlebrot set.

# Today's lecture

Today we will look at some general considerations for **parallel performance**:

- Introduce common parallel overheads.
- Common **metrics** for parallel performance.
- Classic models for predicting parallel speed-up and highlighting potential pitfalls.
- How these relate to **scaling**, *i.e.* how performance varies with the number of processors and the problem size.

#### Notation

For this lecture we will use the following notation:

Symbol	Meaning	Notes
n	Problem size	e.g. vector size, list length,
		image size,
p	No. processing units	e.g. cores, threads, pro-
		cesses,
$t_s$	Serial execution time	'Optimal'
$t_p$	Parallel execution	
	time	
f	Serial fraction	Amdahl, Gustafson-Barsis

### What we are trying to achieve

Assume a problem can be solved by a **serial** algorithm in a time  $t_s$ .

• We assume this is **optimal**, *i.e.* cannot be improved (in serial).

In practice the optimal  $t_s$  is rarely employed.

- Optimal solution may not be known.
- May be known, but take too long to implement.

Usually consider the serial algorithm which is 'equivalent' to the parallel one.

 For instance, if developing a parallel bubblesort, would probably compare to serial bubblesort (rather than quicksort, mergesort, heapsort etc.).

#### Parallel acceleration

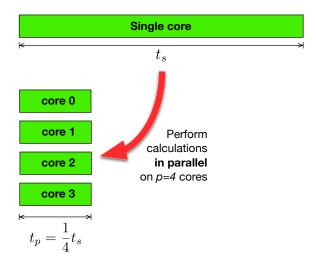
One way to improve on the **serial** execution time  $t_s$  is to implement a **parallel** solution on **parallel** hardware.

- May be possible to 'beat' t<sub>s</sub> by exploiting simultaneous calculations.
- Can also make better use of shared memory cache.

Denote the (not necessarily optimal) parallel execution time  $t_p$ .

- Measured in same units as  $t_s$ .
- On 'as similar as possible' hardware.
- Sometimes known as the wall clock time, as it is what 'a clock on the wall' would measure.

# Simultaneous calculations (ideally)

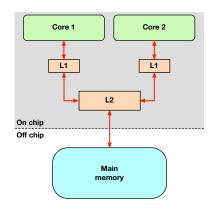


# Multi-core memory cache

Recall from Lecture 2 that using multiple cores can make better use of **memory cache**.

#### Fewer cache misses:

- Cache lines pulled up by one core may include data required by another core.
- Depending on how data is arranged in memory and accessed, a parallel code may result in fewer cache misses overall that the equivalent serial algorithm.



### Challenges to parallel performance

These potential benefits must be offset by the many challenges to achieving good parallel performance.

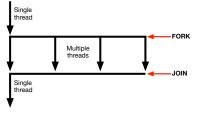
In Lecture 2 we saw one example: **false sharing**:

 Hardware performance loss in maintaining cache coherency when two cores repeatedly write to the same cache line, even though they never read the other core's data.

Over the coming lectures we will see two important, general challenges: **synchronisation** and **load balancing**.

# Synchronisation

In the **fork-join** construct from last lecture, multiple threads complete before the main thread continues.



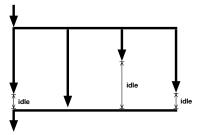
This **joining** requires resources:

- Main thread may repeatedly **probe** worker thread status.
- Alternatively, workers may **signal** their completion to main.
- An example of synchronisation.

# Load balancing

#### A related issue is **load balancing**:

- What if the slave threads did not all finish at the same time?
- Some would be **idle**, waiting for others to finish.
- Poor use of available resources.



This happens in the Mandelbrot set since each thread performs different numbers of calculations [cf. last lecture; Lecture 13].

#### Parallel overheads

Even if these challenges could be overcome, there are inevitable **overheads**. For example:

- Time and resources to create, schedule and destroy threads and/or processes during runtime (e.g. fork-join).
- **Communication** between threads/processes not present in the serial equivalent.
- **Computation** not present in serial, *e.g.* when partitioning the problem size between threads.

The impact may be small or large depending on parallel algorithm and hardware architecture.

# Metrics for parallel performance

There are various measurements of parallel vs. serial performance.

The most common is the **speedup** S:

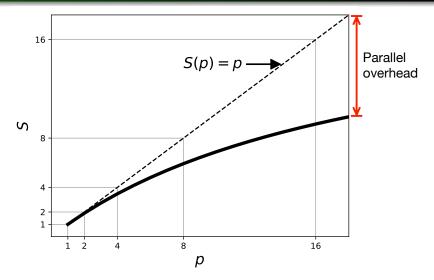
$$S=\frac{t_s}{t_p}$$

• If the parallel version was *p* times faster than the serial:

$$t_p = \frac{1}{p}t_s \implies S = \frac{t_s}{\frac{1}{p}t_s} = p$$

Rarely realised in practice due to parallel overheads.

# Speedup example



### Superlinear speedup

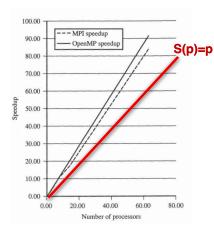
### S(p) > p is possible:

• Usually due to memory cache (or suboptimal  $t_s$ ).

This is super-linear speedup.

Example (right): Benchmark computational fluid dynamics algorithm.

However, this is rare - most commonly see S(p) < p.



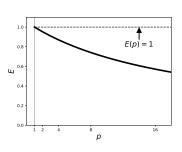
From Parallel Programming in OpenMP, Chandra et al. (Academic, 2001).

# Efficiency

Another common parallel performance metric is the **efficiency** E:

$$E = \frac{t_s}{pt_p} = \frac{S}{p}$$

- 'Ideal' speedup S = p corresponds to E = 1.
- Often expressed as a percentage: F = 1 = 100%.
- Typically E < 1 due to parallel overheads.
- Superlinear speedup gives E > 1.



### Models for parallel performance

Desirable to theoretically predict  $t_p$  for parallel algorithms.

- Select the 'best' without development and testing.
- Identify 'bottlenecks' for further investigation.

Challenging to derive **precise** equations for  $t_p$ :

- Need to include e.g. memory cache, thread scheduler etc.
- Involve many unknown parameters requiring calibration.
- Would need re-calibration for new hardware.

However, even **simple** models can predict **trends**.

• **Parallel scaling**, which refers to the variation with *p*.

#### Amdahl's law

Suppose a fraction f of  $t_s$  cannot be parallelised.

$$t_{s} = ft_{s} + (1 - f)t_{s}$$

$$\implies t_{p} \geq ft_{s} + \frac{(1 - f)t_{s}}{p}$$

$$\implies S = \frac{t_{s}}{t_{p}} \leq \frac{t_{s}}{ft_{s} + \frac{(1 - f)t_{s}}{p}} = \frac{1}{f + \frac{1 - f}{p}}$$

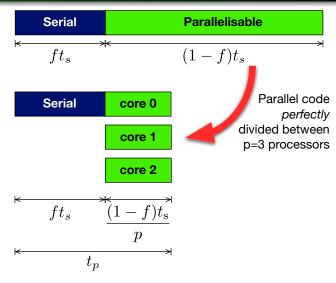
This is Amdahl's law<sup>1</sup> (1967).

For large p it predicts  $S \leq \frac{1}{f}$  regardless of p.

• e.g. f = 0.2, maximum speedup of 5, **even for p**= $\infty$ !

<sup>&</sup>lt;sup>1</sup>Amdahl, AFIPS Conference Proceedings 30, 483 (1967).

# Schematic for Amdahl's law (p = 3)



### Gustafson-Barsis law

However, Amdahl assumed  $t_s$  — and hence n — was fixed.

• Suppose instead n increases with p such that  $t_p$  is fixed.

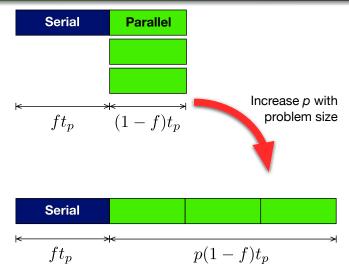
$$t_p = ft_p + (1-f)t_p$$
  
 $\implies t_s \le ft_p + p(1-f)t_p$   
 $\implies S \le f + p(1-f) = p + f(1-p)$ 

Now  $S \leq (1 - f)p$  for large p - **no upper bound** as  $p \to \infty$ .

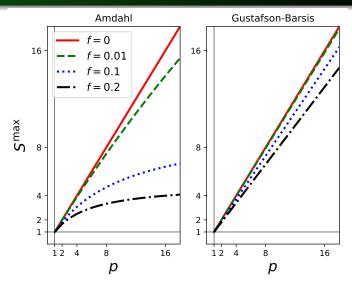
This is the Gustafson-Barsis law, or just Gustafson's law<sup>1</sup>.

<sup>&</sup>lt;sup>1</sup>Gustafson, Comm. ACM **31**, 532 (1988).

# Schematic for Gustafson-Barsis law (p=3)



### Amdahl versus Gustafson-Barsis



# Weak versus strong scaling

The differences are encapsulated in **weak** versus **strong** scaling:

**Strong scaling**: Increasing p with n fixed.

- Amdahl's law.
- Cannot control system size.
- e.g. data analysis/mining.

**Weak scaling**: Increasing n with p.

- Gustafson-Barsis law.
- Have freedom to vary *n*.
- *e.g.* higher resolution meshes for scientific/engineering applications; more/larger layers in neural networks.

### Summary and next lecture

Today we have looked at **parallel performance**:

- Two common metrics: **speedup** and **efficiency**.
- Challenging to achieve ideal speedup due to various parallel overheads.
- Classic models known as Amdahl's law and the Gustafson-Barsis law.
- Correspond to strong and weak scaling, respectively.

Next time we will look more closely at **data dependencies** in parallel loops.