

Lab # 5 – Binomial and Poisson Distributions

Answer/Grading Sheet

Step :	Answer (if requested)	Mark	
6	<p>a)</p> <pre>> dbinom(94,1000,0.094) [1] 0.043191</pre> <p>b)</p> <pre>> 1 - pbinom(81,1000,0.094) [1] 0.9143385</pre> <p>c)</p> <pre>> pbinom(65,1000,0.094) [1] 0.0006092706</pre> <p>d)</p> <pre>> pbinom(99,1000,0.094) [1] 0.7275475</pre> <p>e)</p> <pre>> 1 - pbinom(74,1000,0.094) [1] 0.9849876</pre> <p>f)</p> <pre>> pbinom(19,1000,0.094) [1] 2.295188e-22</pre> <p>g)</p> <pre>> pbinom(90,1000,0.094) - pbinom(50,1000,0.094) [1] 0.3569564</pre> <p>h)</p> <pre>> dbinom(32,1000,0.094) [1] 1.005326e-14</pre> <p>i)</p> $\mu = np$ $\mu = (1000)(0.094)$ $\mu = 94$ <p>j)</p> $s = \sqrt{n \cdot p \cdot (1 - p)}$ $s = \sqrt{1000 \cdot 0.094 \cdot (1 - 0.094)}$ $s = 9.2284$		/1 0
7	<p>#7 using $\mu = np = \text{lamda}$</p> <pre>p <- 1.1/10000</pre> <p>a)</p> <pre>> dpois(2,p*200) [1] 0.01942095</pre> <p>b)</p> <pre>> dpois(1,p*500) + (dpois(2,p*500) - dpois(2,p*1000)) [1] 0.203199</pre>		/3

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Step :	Answer (if requested)	Mark	
	c) <pre>> ppois(10,p*5000) - ppois(4,p*5000)</pre> <pre>[1] 0. 6172307</pre>		
8	a) a = probability a <- 0.4/60 <pre>> dpois(2, a*60)</pre> <pre>[1] 0.0536256</pre> b) <pre>> ppois(3, a*300)</pre> <pre>[1] 0.8571235</pre> c) <pre>> 1 - ppois(3, a*120)</pre> <pre>[1] 0. 0474226</pre>		/3
R script Paste your R script here. Make sure that it contains ALL of the elements worth points listed above. # Lab 5 # Markus Afonso library(mosaic) # 6 a dbinom(94,1000,0.094) #b 1 - pbinom(81,1000,0.094) #c pbinom(65,1000,0.094) #d pbinom(99,1000,0.094) #e 1 - pbinom(74,1000,0.094) #f pbinom(19,1000,0.094) #g pbinom(90,1000,0.094) - pbinom(50,1000,0.094) #h dbinom(32,1000,0.094) #7 using u = np = lamda p <- 1.1/1000 #a dpois(2,p*200) #b			

Step :	Answer (if requested)	Mark	
	<pre> dpois(1,p*500) + (dpois(2,p*500) - dpois(2,p*1000)) #c ppois(10,p*5000) - ppois(4,p*5000) #8 a <- 0.4/60 dpois(2, a*60) ppois(3, a*300) 1 - ppois(2, a*120) </pre>		
	<p>Paper and Pencil problem #1 (this is just a space for your marks)</p> <p>1.) 30/82 games assume '16 - '17 = '18 - '19</p> <p>a) $b(x, n, p) = \frac{n!}{(n-x)! x!} p^x q^{n-x}$</p> $b(8, 10, \frac{30}{82}) = \frac{10!}{(10-8)! 8!} \cdot \left(\frac{30}{82}\right)^8 \cdot \left(1 - \frac{30}{82}\right)^{10-8}$ $b(8, 10, \frac{30}{82}) = 0.005808$ <p>b) $P(x > 79)$ $P(x \geq 80) = P(x=80) + P(x=81) + P(x=82)$</p> $= b(80, 82, \frac{30}{82}) + b(81, 82, \frac{30}{82}) + b(82, 82, \frac{30}{82})$ $= \left[\frac{82!}{(82-80)! 80!} \cdot \left(\frac{30}{82}\right)^{80} \cdot \left(1 - \frac{30}{82}\right)^{82-80} \right] + \left[\frac{82!}{(82-81)! 81!} \cdot \left(\frac{30}{82}\right)^{81} \cdot \left(1 - \frac{30}{82}\right)^{82-81} \right] + \left[1 \cdot \left(\frac{30}{82}\right)^{82} \cdot \left(1 - \frac{30}{82}\right)^{82-82} \right]$ $= [1.54967 \times 10^{-22}] + [2.207511 \times 10^{-24}] + [1.553127 \times 10^{-46}]$ $= 1.5719 \times 10^{-22}$		/2
	Paper and Pencil problem #2		/3

Step :	Answer (if requested)	Mark	
	<p>2) $p = .65$</p> <p>a) $x = 6$ $n = 6$ $b(x, n, p) = {}^nC_x \cdot p^x \cdot (1-p)^{n-x}$ $b(6, 6, .65) = 1 \cdot (.65)^6 \cdot (1-.65)^0$ $= 0.07542$</p> <p>b) $b(0, 6, 0.65) = {}^6C_0 \cdot (0.65)^0 \cdot (1-0.65)^6$ $= 0.001838$</p> <p>c) $6 \cdot .65 = 3.9$ 3.9 out of the 6 are expected to be below the min size. Assumption: can't have a fraction of a sample so: 4 are expected to be undersize</p> <p>$\therefore P(x \geq 4) = P(x=4) + P(x=5) + P(x=6)$ $= [{}^6C_4 \cdot (0.65)^4 \cdot (0.35)^2] + [{}^6C_5 \cdot (0.65)^5 \cdot (0.35)^1] + [1 \cdot (0.65)^6 \cdot (0.35)^0]$ $= [0.32800] + [0.243661] + [0.0754189]$ ≈ 0.6471 chance that there will be more than 4 undersize samples.</p>		
	Paper and Pencil problem #3		/3

$$3) 0.1 \text{ per min} = \rho$$

$$\mu = \lambda = \rho$$

$$a) \lambda = 2 \cdot 0.1$$

$$\lambda = 0.2$$

$$P(x=1 \text{ per 2 mins}) = \frac{\lambda^x e^{-\lambda}}{x!}$$

$$P(x=1) = \frac{0.2^1 e^{-0.2}}{1!}$$

$$= 0.1637$$

$$b) \lambda = 10 \cdot 0.1$$

$$\lambda = 1$$

$$P(x \geq 2) = 1 - P(x \leq 1)$$

$$= 1 - [P(x=1) + P(x=0)]$$

$$= 1 - \left[\left(\frac{1^1 e^{-1}}{1!} \right) + \left(\frac{1^0 e^{-1}}{0!} \right) \right]$$

$$= 1 - [0.3678 + 0.3678]$$

$$= 0.2642$$

$$b) \lambda = 20 \cdot 0.1$$

$$\lambda = 2$$

$$P(x \leq 1) = P(x=1) + P(x=0)$$

$$= \frac{2^1 e^{-2}}{1!} + \frac{2^0 e^{-2}}{0!}$$

$$= 0.27067 + 0.13533$$

$$= .40600$$

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