

Problem 1 A length of the road is straight, and it has a profile in the x-y plane described by

$$f(x) = 200 \ln \left[7.06 \cdot 10^{-4} (x + 1416) \right].$$

Where $0 \leq x \leq 3 \text{ miles} = 15,840 \text{ ft.}$; $f(x)$ and x are in feet.

- Plot the road profile in the x-y plane for $0 \leq x \leq 15,840 \text{ ft.}$
- Derive an expression for $\beta(x)$. Calculate $\beta(500 \text{ ft.})$. (answer: $\beta(500 \text{ ft.}) = 5.96^\circ$)
- Derive an expression for $\text{percent grade}(x)$. Calculate $\text{percent grade}(500 \text{ ft.})$. (answer: $\% \text{Grade}(500 \text{ ft.}) = 10.4\%$)
- Derive an expression for tangential road length $s(x)$, such that $s(0) = 0$. Calculate $s(500 \text{ ft.})$ (answer: $s(500 \text{ ft.}) = 504 \text{ ft.}$)

Problem 2 An electric vehicle has the following parameter values:

$$m = 692 \text{ kg}, C_D = 0.2, A_F = 2 \text{ m}^2, C_0 = 0.009, C_1 = 1.75 \cdot 10^{-6} \text{ s}^2/\text{m}^2,$$

$$\text{Also, take } \rho = 1.16 \text{ kg/m}^3, g = 9.81 \text{ m/s}^2,$$

The EV is stopped at a stop sign at a point in the road where the grade is +15%. The tractive force of the vehicle is supplied by the vehicle brakes.

- Calculate the tractive force necessary for zero rolling resistance (The vehicle is at rest). (answer: $F_{TR} = 1007 \text{ N}$)
 - Calculate the minimum tractive force required from the brakes to keep the EV from rolling down the grade. ((answer: $F_{TR} = 946 \text{ N}$)
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Problem 3

The EV in problem # 2 is moving at a constant velocity along a road that has a constant grade of -12%.

i) Plot, on the same graph, the magnitudes of the tangential gravitational force (F_{gT}), the aerodynamic drag force (F_{AD}), and the rolling resistance force (F_{ROLL}) versus velocity for $0 < V \leq 180 \text{ mph}$. Over that range of velocity, does F_{gT} dominate? When does F_{AD} dominate?

When does F_{ROLL} dominate? Label these regions on the graph.

ii) Derive an expression for the tractive force as a function of velocity. Plot this expression on its own graph. Is the tractive force always in the same direction?