from functools import partial from typing import Sequence import random import time Rapid intro to supervised learning with neural nets II: using JAX This notebook gives a rapid introduction to supervised learning with neural networks. The example is based on Chapter 1 of Nielsen's online book "Neural Networks and Deep Learning" and it guides you to set up the neural network training using the JAX and Flax libraries. For further reading I recommend also the review article "A high-bias, low-variance introduction to Machine Learning for physicists". A few words on JAX JAX is a Python library that provides useful functionality for machine learning applications (especially deep learning), namely automatic differentiation, just-in-time compilation, and vectorization. This is implemented in JAX through function transformations, i.e., functions that map functions to new functions. **Automatic differentiation** With automatic differentiation we can let the computer compute gradients of arbitrary functions. In JAX the function jax.grad() takes a function as argument and returns a function that is the gradient of the given function. Example: In [2]: # Define a function def f(x): return x**2 # Get the gradient f_prime = jax.grad(f) # Evaluate function and gradient x=np.arange(-1,1,.1)y=np.array([f prime(r) for r in x]) plt.plot(x, f(x), label=r"\$f(x)\$") plt.plot(x,y,label=r"\$f'(x)\$")plt.xlabel(r"\$x\$") plt.legend() WARNING:absl:No GPU/TPU found, falling back to CPU. (Set TF CPP MIN LOG LEVEL=0 and rerun for more info.) <matplotlib.legend.Legend at 0x7fb313241890> 1.5 1.0 0.5 0.0 -0.5-1.0-1.5-1.00 -0.75 -0.50 -0.25 0.00 0.25 0.50 Vectorization The jax.vmap() function allows us to apply a function that is defined for a single input to an array. For example, we can replace the line y=np.array([f_prime(r) for r in x]) from the previous cell as follows: In [3]: # Get a vectorized version of the function f prime vectorized = jax.vmap(f prime) # Apply the vectorized function to an input array f_prime_vectorized(x) DeviceArray([-2.000000e+00, -1.800000e+00, -1.600000e+00, -1.400000e+00, -1.200000e+00, -1.000000e+00, -8.000000e-01, -6.000000e-01, -4.000000e-01, -2.000000e-01, -4.440892e-16, 2.000000e-01, 4.000000e-01, 6.000000e-01, 8.000000e-01, 1.000000e+00, 1.200000e+00, 1.400000e+00, 1.600000e+00, 1.800000e+00], dtype=float32) Just-in-time compilation With jax.jit() we can ask JAX to just-in-time (JIT) compile our Python code such that it can be executed with the high efficiency of XLA. A simple, yet not particularly spectacular, example is In [4]: # Get a vectorized version of the function f prime vectorized compiled = jax.jit(f prime vectorized) # Apply the vectorized function to an input array f prime vectorized compiled(x) DeviceArray([-2.000000e+00, -1.800000e+00, -1.600000e+00, -1.400000e+00, -1.200000e+00, -1.000000e+00, -8.000000e-01, -6.000000e-01, -4.000000e-01, -2.000000e-01, -4.440892e-16, 2.000000e-01, 4.000000e-01, 6.000000e-01, 8.000000e-01, 1.000000e+00, 1.200000e+00, 1.400000e+00, 1.600000e+00, 1.800000e+00] dtvpe=float32) Superficially, f_prime_vectorized_compiled() does not differ from f_prime_vectorized(). Under the hood, however, the compiled function executes its task (potentially) much more efficiently than the original one. In the code below you will find a number of jax.jit statements. By removing these statements and working only with the un-compiled versions of the respective functions you will observe a noticeable slow-down. Notice: In order to use JAX function transformations (like vectorization) we have to replace the Numpy library with its JAX version, which has the same interface. For example, instead of np.array all our arrays will be jnp.array s. The same for functions, e.g. instead of np.dot we have to use jnp.dot for the dot-product. The MNIST hand-written digits data set Let's first get a simple exemplary data set - the MNIST hand-written digits. The following cell downloads both the test and training parts of the data set. In [5]: trainData = jnp.array(tfds.as numpy(tfds.load('mnist', split='train', batch_size=-1, shuffle_files=False))['image'].reshape(-1,28,28) trainLabels = jnp.array(tfds.as_numpy(tfds.load('mnist', split='train', batch size=-1, shuffle files=False))['label'] testData = jnp.array(tfds.as numpy(tfds.load('mnist', split='test', batch size=-1, shuffle files=False))['image'].reshape(-1,28,28) testLabels = jnp.array(tfds.load('mnist', split='test', batch size=-1, shuffle files=False))['label'] trainData is now a jax.numpy.array of shape (60000,28,28), meaning that we have 60k images of 28×28 pixels (grayscale), each showing one hand-written digit. trainLabels holds the corresponding labels, i.e. an integer for each image, stating which digit it shows. Let's have a look at some examples: Defining a neural network model using Flax Flax is a library built on top of JAX, which allows you to easily compose complicated deep learning models. If you are familiar with Pytorch, the following syntax will be very intuitive for you. In Flax a new model can be defined as a class that inherits from the nn. Module base class. Here, we introduce Flax's abbreviated model definition; notice that general model definitions can be more involved. In the short form, a model is defined by defining a __call__ method that evaluates the network on the given input. The library provides implementations of typical linear transformations as well as typical activation functions (among other typical building blocks of neural networks). In the cell below we use the provided Dense linear transformation and the sigmoid activation function to implement the same network architecture as the one that we coded from scratch in part I of this tutorial: class MyNet(nn.Module): layers: Sequence[int] # A tuple that contains the widths of all layers follwing the input layer @nn.compact def call (self, x): a = x.ravel() # flatten the input # Evaluate network layer by layer for width in self.layers: # Apply a the Dense layer with given width followed by the non-linearity a = nn.sigmoid(nn.Dense(width)(a)) # Return activations of the output layer return a Now we can again what the network thinks about our images of digits. For this purpose we define initialize_network and neural_network analogous to part I of the tutorial, but this time based on our MyNet class. In [7]: def initialize network(layers, seed=123): # Get random initial parameters. Notice: The `init` method needs an example input for this purpose. return MyNet(layers=layers).init(jax.random.PRNGKey(seed), trainData[0]) def neural network(params, image, layers): # Evaluate the network with given parameters neural_network = MyNet(layers=layers) return jax.jit(jax.vmap(lambda x: neural network.apply(params, x)))(image) # Define the network size. # Here we only need to include the width of layers *after* the input layer. # The size of the input layer is determined automatically from the input data. net layers=(100,10) # Get initial parameters params = initialize_network(net_layers) # Evaluate the network neural network(params, trainData[:3], net layers) DeviceArray([[0.6283565 , 0.50599694, 0.6832025 , 0.50604314, 0.42828634, 0.25097242, 0.6408896 , 0.5169621 , 0.38393703, 0.39720345], [0.6706722, 0.57142377, 0.6822245, 0.7108034, 0.30151436,0.48183188, 0.35933733, 0.6973047, 0.4983423, 0.38091958], [0.48349693, 0.5223302 , 0.6942643 , 0.55765235, 0.46390426, 0.4895871 , 0.51695365, 0.6439555 , 0.60555077, 0.6348824]], dtype=float32) Next, we need a cost function: In [8]: @partial(jax.jit, static argnums=3) def cost function(params, images, labels, layers): '''This function evaluates the cost function for given predictions and labels * `params`: Network parameters. * `images`: A batch of input images. * `labels`: Correct labels for the given images. * `layers`: Size of the network (list of widths). Returns: Cost associated with the neural network predictions for the given data. labels = jax.nn.one hot(labels, 10) # get one-hot encoding of labels predictions = neural network(params,images,layers) cost = jnp.sum((predictions-labels)**2) return cost / labels.shape[0] With this, we can check the performance of our randomly initialized network in classifying some of our images: In [9]: batch = trainData[:128] # select a batch of images labels = trainLabels[:128] # and corresponding labels cost function(params, batch, labels, net layers) Out[9]: DeviceArray(2.7373376, dtype=float32) Now, what is missing is a function to compute the gradients of the cost function. This is easily solved using <code>jax.grad</code> for automatic differentiation: In [10]: cost function gradients = jax.grad(cost function) Finally, we are ready to train the network: In [11]: def evaluate predictions(predictions, labels): '''This is a helper function that counts how many of the given predictions match the labels. * `predictions`: Predictions from neural network (=activations on output layer) * `labels`: correct labels Returns: Number of correct predictions, i.e., number of cases, in which the index of the maximal activation matches the given label. pred labels = jnp.argmax(predictions, axis=1) return jnp.where(pred labels==labels)[0].shape[0] # Get a key for the PRNG prng key = jax.random.PRNGKey(123) # Here we define the hyperparamters num epochs = 10 # Number of epochs to loop over learning rate = 0.001 # Learning rate batch size = 128 # Size of mini-batches # Compute the number of mini-batches that matches the chosen mini-batch size batch number = trainData.shape[0] // batch size # Evaluate network and assess performance predictions = neural network(params, testData, net layers) current_cost = cost_function(params, testData, testLabels, net_layers) correct_predictions = evaluate_predictions(predictions, testLabels) print(" Initial cost: %f" % (current cost)) print(" Correctly predicted labels: %d / %d" % (correct predictions, len(testLabels))) # Training loop over epochs for n in range(num epochs): tic = time.perf_counter() print("* Episode %d" % (n)) # Generate batches from randomly permuted data prng_key, tmp_key = jax.random.split(prng_key) # jax-style treatment of random numbers batches = (jax.random.permutation(tmp_key, trainData)[:batch_number*batch_size].reshape(-1,128,28,28), jax.random.permutation(tmp key, trainLabels)[:batch number*batch size].reshape(-1,128)) # Loop over mini-batches for samples, labels in zip(*batches): # compute gradients grads = jax.jit(cost function gradients, static argnums=3)(params, samples, labels, net layers) # Perform SGD parameter update step params = jax.tree util.tree multimap(lambda a,b: a-learning rate*b, params, grads) # Evaluate network and assess performance predictions = neural network(params, testData, net layers) current_cost = cost_function(params, testData, testLabels, net_layers) correct_predictions = evaluate_predictions(predictions, testLabels) print(" Current cost: %f" % (current cost)) print(" Correctly predicted labels: %d / %d" % (correct_predictions, len(testLabels))) print(" -- Time for episode: %fs" % (time.perf_counter()-tic)) Initial cost: 2.685170 Correctly predicted labels: 781 / 10000 * Episode 0 Current cost: 0.876519 Correctly predicted labels: 3529 / 10000 -- Time for episode: 2.045670s * Episode 1 Current cost: 0.805401 Correctly predicted labels: 4743 / 10000 -- Time for episode: 1.411812s * Episode 2 Current cost: 0.758254 Correctly predicted labels: 5466 / 10000 -- Time for episode: 1.384086s * Episode 3 Current cost: 0.717020 Correctly predicted labels: 6019 / 10000 -- Time for episode: 1.364848s * Episode 4 Current cost: 0.681147 Correctly predicted labels: 6409 / 10000 -- Time for episode: 1.468741s * Episode 5 Current cost: 0.647137 Correctly predicted labels: 6812 / 10000 -- Time for episode: 1.410022s * Episode 6 Current cost: 0.615984 Correctly predicted labels: 7088 / 10000 -- Time for episode: 1.335578s * Episode 7 Current cost: 0.588617 Correctly predicted labels: 7338 / 10000 -- Time for episode: 1.394118s * Episode 8 Current cost: 0.563799 Correctly predicted labels: 7523 / 10000 -- Time for episode: 1.419925s * Episode 9 Current cost: 0.541183 Correctly predicted labels: 7650 / 10000 -- Time for episode: 1.414002s

import jax

import flax.linen as nn
import tensorflow as tf

import jax.numpy as jnp

import numpy as np

import tensorflow_datasets as tfds

import matplotlib.pyplot as plt