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Abstract

A concise description of the XCS classifier system's parameters, structures, and algorithms is presented as an aid to research. The algorithms are written in modularly structured pseudo code with accompanying explanations.

1 Introduction

XCS is a recently developed learning classifier system (LCS) that differs in several ways from more traditional LCSs. In XCS, classifier fitness is based on the *accuracy* of a classifier's payoff prediction instead of the prediction itself. Second, the genetic algorithm (GA) takes place in the action sets instead of the population as a whole. Finally, unlike the traditional LCS, XCS has no message list and so is only suitable for learning in Markov environments (XCS extensions using an internal-state register have shown promise in non-Markov environments).

XCS's fitness definition and GA locus together result in a strong tendency for the system to evolve accurate, maximally general classifiers that efficiently cover the state-action space of the problem and allow the system's 'knowledge' to be readily seen. As a result of these properties, there has been considerable interest in further investigation and potential extension of XCS and its principles. We therefore thought it would be useful to provide a basic algorithmic description of XCS, both as a core definition of the system and as a common framework from which new variants and research directions could spring.

We first present XCS's relation to the problem environment, followed by the system's structures and parameters. The rest of the paper consists of a top-down modular description of the XCS algorithm, written in pseudo-code accompanied by explanatory notes. We hope the result will be useful, and we encourage researchers to give us feedback regarding potential problems and clarifications. This document should definitely be read in conjunction with some of the basic XCS literature, for example Wilson (1995), Kovacs (1997), and Wilson (1998). Additional papers on XCS and other LCSs, together with a complete LCS bibliography, will be found in Lanzi, Stolzmann, and Wilson (2000).

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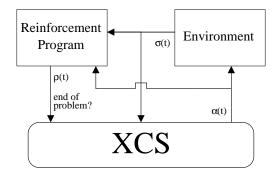


Figure 1: XCS interacts with an environment and a reinforcement program.

2 Environment Interaction, Structures, and Parameters

2.1 Interaction with the Environment

In keeping with the typical LCS model, the environment provides as input to the system a series of sensory situations $\sigma(t) \in \{0,1\}^L$, where L is the number of bits in each situation. In response, the system executes actions $\alpha(t) \in \{a_1, ..., a_n\}$ upon the environment. Each action results in a scalar reward $\rho(t)$ (possibly zero). The interaction is divided into problems, which may be either single-step or multi-step. A flag eop indicates the end of a problem. While $\sigma(t)$ and $\sigma(t)$ are interactions with the environment itself, the reward $\rho(t)$ and the flag are normally provided by another component which, following Dorigo and Colombetti (1998), we term the reinforcement program rp. The reinforcement program determines the reward according to the current environmental input and the action that was executed. The separation of environment and reinforcement components is useful and natural because reinforcement is often not an inherent aspect of the environment, but may be due, e.g., to a trainer or to the system's own priorities. Figure 1 illustrates the interaction of the environment and rp with XCS.

In a single-step problem such as the Boolean multiplexer, the successive situations are not related to each other. After execution of an action the rp provides the appropriate reward ρ and signals with the flag eop that the problem has ended. In a multi-step problem such as a maze, the successive situations are related to each other. Reward is only provided in certain situations (e.g. the food position(s) in mazes). The point at which a problem ends in a multi-step environment must be defined by the rp according to the task that is to be solved.

2.2 A Classifier in XCS

XCS keeps a population of classifiers which represent its knowledge about the problem. Each classifier is a condition–action–prediction rule having the following parts:

- The condition $C \in \{0, 1, \#\}^L$ specifies the input states (sensory situations) in which the classifier can be applied (matches).
- The action $A \in \{a_1, ..., a_n\}$ specifies the action (possibly a classification) that the classifier proposes.
- The prediction p estimates (keeps an average of) the payoff expected if the classifier matches and its action is taken by the system.

Moreover, each classifier keeps certain additional parameters:

- The prediction error ϵ estimates the errors made in the predictions.
- The fitness f denotes the classifier's fitness.
- The experience *exp* counts the number of times since its creation that the classifier has belonged to an action set.
- The time stamp ts denotes the time-step of the last occurrence of a GA in an action set to which this classifier belonged.
- The action set size as estimates the average size of the action sets this classifier has belonged to.
- The numerosity num reflects the number of micro-classifiers (ordinary classifiers) this classifier—which is technically called a macroclassifier—represents.

To refer to one of the attributes of a classifier cl we will write x_{cl} where x can be any of the above attributes (i.e. $x \in \{C, A, p, \epsilon, f, exp, ts, as, num\}$).

Important in our notation is the term payoff. Due to the Q-learning-like reinforcement learning in XCS, payoff does not refer solely to the expected reward ρ but is a combination of ρ and the payoff prediction of the best possible action in the next state. However, in the case of a single-step problem payoff reduces to the reward produced by the proposed action.

Note that ϵ measures the error of the predictions in units of payoff. The same is true of the parameter ϵ_0 that is defined in section 2.4.

Classifiers in XCS are macroclassifiers, i.e., each classifier represents num traditional or microclassifiers having identical conditions and actions. Algorithms covering creation, deletion, and adjustment of the numerosity of macroclassifiers are given in section 3.2.7 and 3.2.8. In XCS, macroclassifiers are always handled as though they consist of num microclassifiers.

2.3 The Different Sets

There are four different sets that need to be considered in XCS.

- The population [P] consists of all classifiers that exist in XCS at any time t.
- The match set [M] is formed out of the current [P]. It includes all classifiers that match the current situation $\sigma(t)$.
- The action set [A] is formed out of the current [M]. It includes all classifiers of [M] that propose the executed action.
- The previous action set $[A]_{-1}$ is the action set that was active in the last execution cycle.

2.4 Learning Parameters in XCS

In order to control the learning process in XCS the following parameters are used:

- N specifies the maximum size of the population (in micro-classifiers, i.e., N is the sum of the classifier numerosities).
- β is the learning rate for p, ϵ, f .

- α , ϵ_0 , and ν are used in calculating the fitness of a classifier.
- γ is the discount factor used—in multi-step problems—in updating classifier predictions.
- θ_{GA} is the GA threshold. The GA is applied in a set when the average time since the last GA in the set is greater than θ_{GA} .
- χ is the probability of applying crossover in the GA.
- μ specifies the probability of mutating an allele in the offspring.
- θ_{del} is the deletion threshold. If the experience of a classifier is greater than θ_{del} , its fitness may be considered in its probability of deletion.
- δ specifies the fraction of the mean fitness in [P] below which the fitness of a classifier may be considered in its probability of deletion.
- θ_{sub} is the subsumption threshold. The experience of a classifier must be greater than θ_{sub} in order to be able to subsume another classifier.
- $P_{\#}$ is the probability of using a # in one attribute in C when covering.
- p_I , ϵ_I , and f_I are used as initial values in new classifiers.
- p_{exp} specifies the probability during action selection of choosing the action uniform randomly.
- θ_{mna} specifies the minimal number of actions that must be present in a match set [M], or else covering will occur.
- doGASubsumption is a Boolean parameter that specifies if offspring are to be tested for possible logical subsumption by parents.
- doActionSetSubsumption is a Boolean parameter that specifies if action sets are to be tested for subsuming classifiers.

2.5 Commonly Used Parameter Settings

For parameter settings, it is best to check the literature for a similar experiment. In some cases, the following suggestions could be taken as starting points. The population size, N, should be large enough so that, starting from an empty population, covering occurs only at the very beginning of a run. The learning rate, β , could be in the range 0.1-0.2. The parameter α is normally 0.1. The parameter ϵ_0 is the error below which classifiers are considered to have equal accuracy; a typical value would be about one percent of the maximum value of ρ , e.g., 10 if the maximum value is 1000. The power parameter ν is typically 5. The discount factor γ has been 0.71 in many problems in the literature, but larger or smaller values could certainly work, depending on the environment. The threshold θ_{GA} is often in the range 25-50. Crossover probabilities χ in the range 0.5-1.0 have been used. Mutation probabilities μ in the range 0.01-0.05 are often used.

The deletion threshold θ_{del} could be about 20. δ is often taken to be 0.1. The subsumption threshold θ_{sub} could be about 20, though larger values (more experience) are important in some problems. $P_{\#}$ could be around 0.33. Larger values reduce the need for covering, but may make it harder to evolve accurate classifiers. The initialization parameters p_I , ϵ_I , and f_I should be taken very small—essentially zero. The exploration probability p_{exp} could be 0.5, but this depends on the

type of experiment contemplated. To cause covering to provide classifiers for every action, choose θ_{mna} equal to the number of available actions.

The setting of doGASubsumption and doActionSetSubsumption depends on the problem. In general, subsumption is used to eliminate classifiers that clearly add nothing to the system's decision capability. In the case of GA subsumption, these are offspring classifiers whose conditions are logically subsumed by a parent's condition, given that the parent is both accurate and sufficiently experienced. In the case of action set subsumption, a general, accurate, and experienced classifier in an action set eliminates classifiers in the set that its condition logically subsumes. The two subsumption methods are independent and different in their effects. Broadly, action set subsumption appears to be 'stronger': it causes greater 'condensation' of the population. Subsumption is useful in problems where there is a well-defined underlying target function, such as the Boolean multiplexer.

Note, however, that subsumption is not necessary for XCS to form accurate maximal generalizations (see Wilson (1995) for the basic XCS generalization hypothesis). Subsumption tends to result in accurate classifiers that are as formally general as possible without being contradicted by any actually occurring input. Without subsumption, the system produces these as well as accurate but more-specific classifiers that match the same inputs as the general ones do (Wilson, 1998). Subsumption produces smaller final populations, but because the more-specific classifiers are not present, the system is more vulnerable to environmental changes—it does not have the more-specific classifiers to "fall back on".

3 An Algorithmic Description of XCS

This section presents the algorithms used in XCS. The description starts from the top level. First, the overall execution cycle is described. The following subsections specify the single parts in more detail. Each specified sub-procedure in this description is written in capital letters. When referring to a module other than XCS (e.g. rp), a colon is used.

3.1 Initialization and the Main Loop

When XCS is started, the modules must first of all be initialized. The parameters in the environment must be set and, e.g., a maze must be read in. Also, the reinforcement program rp must be initialized. Finally, XCS itself must be initialized. Apart from the parameter settings and the start of the learning step counter referred to as actual time t, the population [P] needs to be initialized. The population [P] can either be left empty or can be filled with the maximal number of classifiers N, generating each classifier with a random condition and action and the initial parameters. The two methods differ only slightly in their effect on performance. Thus the simpler way of leaving the population empty in the beginning is commonly used. After the initialization, the main loop is called.

XCS:

- 1 initialize environment env
- 2 initialize reinforcement program rp
- 3 initialize XCS
- 4 RUN EXPERIMENT

In the main loop RUN EXPERIMENT, the current situation is first sensed (received as input). Second, the match set is formed from all classifiers that match the situation. Third, the prediction

array PA is formed based on the classifiers in the match set. PA predicts for each possible action a_i the resulting payoff. Based on PA, one action is chosen for execution and the action set [A] is formed, which includes all classifiers of [M] that propose the chosen action. Next, the winning action is executed. Then the previous action set $[A]_{-1}$ (if this is a multi-step problem and there is a previous action set) is modified using the previous reward ρ_{-1} and the largest action prediction in the prediction array. Moreover, the GA may be applied to $[A]_{-1}$. If a problem ends on the current time-step (single-step problem or last step of a multi-step problem), [A] is modified according to the current reward ρ and the GA may be applied to [A]. The main loop is executed as long as the termination criterion is not met. A termination criterion is, e.g., a certain number of trials or a 100% performance level.

```
RUN EXPERIMENT():
```

```
1 do{
       \sigma \leftarrow env: get situation
 2
 3
       GENERATE MATCH SET [M] out of [P] using \sigma
 4
       GENERATE PREDICTION ARRAY PA out of [M]
 5
       act \leftarrow \texttt{SELECT} ACTION according to PA
 6
       GENERATE ACTION SET [A] out of [M] according to act
 7
       env: execute action act
 8
       \rho \leftarrow rp: get reward
 9
       if([A]_{-1}) is not empty)
           P \leftarrow \rho_{-1} + \gamma * max(PA)
10
11
           UPDATE SET [A]_{-1} using P possibly deleting in [P]
12
           RUN GA in [A]_{-1} considering \sigma_{-1} inserting in [P]
13
       if(rp: eop)
14
           P \leftarrow \rho
           UPDATE SET [A] using P possibly deleting in [P]
15
           RUN GA in [A] considering \sigma inserting in [P]
16
17
           empty [A]_{-1}
18
       else
19
           [A]_{-1} \leftarrow [A]
20
           \rho_{-1} \leftarrow \rho
21
           \sigma_{-1} \leftarrow \sigma
22 }while(termination criteria are not met)
```

3.2 Sub-procedures

The main loop specifies many sub-procedures essential for learning in XCS. Some of the procedures are more or less trivial while others are complex and themselves call other sub-procedures. This section describes all procedures specified in the main loop. It covers all relevant processes and describes them algorithmically. Each of the following subsections again tries to specify the general idea and the overall process and then gives a more detailed description of single parts in the successive paragraphs.

3.2.1 Formation of the Match Set

The GENERATE MATCH SET procedure gets as input the current population [P] and the current situation σ . Although the procedure sounds trivial, it has within it a covering process. Covering is called when the number of different actions represented by matching classifiers is less than the parameter θ_{mna} . Thus, GENERATE MATCH SET first looks for the classifiers in [P] that match σ and next, checks if covering is required. Note that a classifier generated by covering can be directly added to the population since it must differ from all current classifiers.

```
GENERATE MATCH SET([P], \sigma):

1 initialize empty set [M]
2 for each classifier cl in [P]
3 if (DOES MATCH classifier cl in situation \sigma)
4 add classifier cl to set [M]
5 while (the number of different actions in [M] < \theta_{mna})
6 GENERATE COVERING CLASSIFIER cl_c considering [M] and covering \sigma
7 add classifier cl_c to set [P]
8 DELETE FROM POPULATION [P]
9 add classifier cl_c to set [M]
10 return [M]
```

In the following paragraphs we will describe the sub-procedures included in the *GENERATE MATCH SET* algorithm. The sub-procedure *DELETE FROM POPULATION* however can be found in section 3.2.7.

Classifier Matching The matching procedure is that commonly used in LCSs. A 'don't care'symbol # in C matches any symbol in the corresponding position of σ . A 'care' or non-# symbol
only matches with the exact same symbol at that position. The basic XCS relies on binary coding
and thus the care symbols are $\in \{0, 1\}$. Recently, Lanzi (1999b) and Lanzi (1999c) introduced an
extension of the conditions in XCS involving messy coding and Lisp s-expressions. Wilson (1999)
introduced the first XCS extension that is able to handle real coded inputs. However, here we will
consider only the basic kind of classifier condition.

The *DOES MATCH* procedure checks each component in the classifier's condition C. If a component is specified (i.e. is not a don't care symbol), it is compared with the corresponding attribute in the current situation σ . Only if all comparisons hold does the classifier match σ and the procedure return true.

```
DOES MATCH(cl, \sigma):

1 for each attribute x in C_{cl}

2 if (x \neq \# \text{ and } x \neq \text{ the corresponding attribute in } \sigma)

3 return false

4 return true
```

Covering Covering occurs if [M] is empty and $\theta_{mna} = 1$, or if not empty but the number of actions present is $<\theta_{mna}$. A classifier is created whose condition matches $\sigma(t)$ and contains don't cares with probability $P_{\#}$. The classifier's action is chosen randomly from among those not present in [M].

```
GENERATE COVERING CLASSIFIER ([M], \sigma):
 1 initialize classifier \it cl
 2 initialize condition C_{cl} with the length of \sigma
 3 for each attribute x in C_{cl}
        if(RandomNumber[0,1[ < P_{\#})
 5
 6
        else
 7
             x \leftarrow the corresponding attribute in \sigma
 8 A_{cl} \leftarrow random action not present in [M]
 9 p_{cl} \leftarrow p_I
10 \epsilon_{cl} \leftarrow \epsilon_{I}
11 f_{cl} \leftarrow f_I
12 exp_{cl} \leftarrow 0
13 ts_{cl} \leftarrow actual time t
14 as_{cl} \leftarrow 1
15 num_{cl} \leftarrow 1
```

3.2.2 The Prediction Array

Given an input, XCS makes a "best guess" prediction of the payoff to be expected for each possible action. These system predictions are stored in a vector called the Prediction Array PA. The system prediction for an action is a fitness-weighted average of the predictions of all classifiers in [M] that advocate that action. If no classifiers in [M] advocate a certain action, its system prediction is not defined, symbolized by null.

The $GENERATE\ PREDICTION\ ARRAY$ procedure considers each classifier in [M] and adds its prediction multiplied by its fitness to the prediction value total for that action. The total for each action is then divided by the sum of the fitnesses for that action to yield the system prediction.

```
GENERATE PREDICTION ARRAY([M]):

1 initialize prediction array PA to all null

2 initialize fitness sum array FSA to all 0.0

3 for each classifier cl in [M]

4 PA[A_{cl}] \leftarrow PA[A_{cl}] + p_{cl} * f_{cl}

5 FSA[A_{cl}] \leftarrow FSA[A_{cl}] + f_{cl}

6 for each possible action A

7 if (FSA[A] is not zero)

8 PA[A] \leftarrow PA[A] / FSA[A]

9 return PA
```

3.2.3 Choosing an Action

XCS does not prescribe any particular action-selection method, and any of a great variety can be employed. For example, actions may be selected randomly, independent of the system predictions, or the selection may be based on those predictions—using, e.g., roulette-wheel selection or simply picking the action with the highest system prediction.

In our SELECT ACTION procedure we illustrate a combination of pure exploration—choosing the action randomly—and pure exploitation—choosing the best one. Lanzi (1999a) published first experiments with so-called biased exploration where pure exploration is chosen with a probability p_{exp} and otherwise pure exploitation is chosen. This action selection method is known as ϵ -greedy selection in the reinforcement learning literature (Sutton & Barto, 1998). As an aside, it appears better to perform the GA only on exploration steps, especially if most steps are exploitation.

```
SELECT\ ACTION(PA):
1 if (RandomNumber[0,1[> p_{exp})
2 //Do pure exploitation here
3 return the best action in PA
4 else
5 //Do pure exploration here
6 return a randomly chosen action from those not null in PA
```

3.2.4 Formation of the Action Set

After the match set [M] is formed and an action is chosen for execution, the $GENERATE\ ACTION$ SET procedure forms the action set out of the match set. It includes all classifiers that propose the chosen action for execution.

```
GENERATE ACTION SET([M], act):

1 initialize empty set [A]

2 for each classifier cl in [M]

3 if (A_{cl} = act)

4 add classifier cl to set [A]
```

3.2.5 Updating Classifier Parameters

Although Wilson (1995) applied the update procedures as well as the GA originally in [M] and only later (Wilson, 1998) was this switched to [A], application in [A] is now commonly used and gives better performance in all cases known to us. Thus we will use the [A] notation in the following procedures although they are basically independent of the classifier set involved.

The reinforcement portion of the update procedure follows the pattern of Q-learning (Sutton & Barto, 1998). Classifier predictions are updated using the immediate reward and the discounted maximum payoff anticipated on the next time-step. The difference is that in XCS it is the prediction of a possibly general rule that is updated, whereas in Q-learning it is the prediction associated with an environmental state. Updates of classifier parameters other than prediction are unique to XCS. Note that in single-step problems, the prediction is updated using the immediate reward alone.

Each time a classifier enters the set [A], its parameters are modified in the order: exp, p, ϵ , as, and f. Variations in the order are possible. The principle one is to exchange the p and ϵ updates. If prediction comes before error, the prediction of a classifier in its very first update immediately predicts the correct payoff and consequently the prediction error is set to zero. This can lead to faster learning in simpler problems but can be misleading in more complex ones. A more conservative strategy which puts the error update first, seems to work better on harder problems. The update of the action set size estimate is independent from the other updates and consequently can

be executed at any point in time. While the updates of exp, p, ϵ , and as are straightforward, the update of f is more complex and requires more computational steps. Thus, we refer to another sub-procedure. Finally, if the program is using action set subsumption, the procedure calls the $DO\ ACTION\ SET\ SUBSUMPTION\$ procedure. This procedure is very powerful and is able to eliminate a large number of classifiers in the action set in one step. Section 3.2.8 describes the procedure in detail.

```
UPDATE\ SET([A],\ P,\ [P]):
 1 for each classifier cl in [A]
 2
         exp_{cl}++
 3
         //update prediction p_{cl}
 4
         if (exp_{cl} < 1/\beta)
             p_{cl} \leftarrow p_{cl} + (P - p_{cl}) / exp_{cl}
 5
 6
 7
              p_{cl} \leftarrow p_{cl} + \beta * (P - p_{cl})
 8
         //update prediction error \epsilon_{cl}
 9
         if (exp_{cl} < 1/\beta)
              \epsilon_{cl} \leftarrow \epsilon_{cl} + (|P - p_{cl}| - \epsilon_{cl}) / exp_{cl}
10
11
         else
12
              \epsilon_{cl} \leftarrow \epsilon_{cl} + \beta * (|P - p_{cl}| - \epsilon_{cl})
         //update action set size estimate as_{cl}
13
14
         if (exp_{cl} < 1/\beta)
              as_{cl} \leftarrow as_{cl} + (\sum_{c \in [A]} num_c - as_{cl}) / exp_{cl}
15
16
             as_{cl} \leftarrow as_{cl} + \beta * (\sum_{c \in [A]} num_c - as_{cl})
17
    UPDATE FITNESS in set [A]
    if(doActionSetSubsumption)
20
         DO ACTION SET SUBSUMPTION in [A] updating [P]
```

Fitness Update The fitness of a classifier in XCS is based on the *accuracy* of its predictions. The *UPDATE FITNESS* procedure first calculates the classifier's accuracy κ using the classifier's prediction error ϵ . Then the classifier's fitness is updated using the *normalized accuracy* computed in lines 7-9.

```
UPDATE\ FITNESS([A]):
 1 accuracySum \leftarrow 0
 2 initialize accuracy vector \kappa
 3 for each classifier cl in [A]
 4
         if(\epsilon_{cl} < \epsilon_0)
 5
              \kappa(cl) \leftarrow 1
 6
         else
              \kappa(cl) \leftarrow \alpha * (\epsilon_{cl} / \epsilon_0)^{-\nu}
 7
         accuracySum \leftarrow accuracySum + \kappa(cl) * num_{cl}
    for each classifier cl in [A]
         f_{cl} \leftarrow f_{cl} + \beta * (\kappa(cl) * num_{cl} / accuracySum - f_{cl})
10
```

3.2.6 The Genetic Algorithm in XCS

The final sub-procedure in the main loop, $RUN\ GA$, is also the most complex. First of all, the action set is checked to see if the GA should be applied at all. In order to apply a GA the average time period since the last GA application in the set must be greater than the threshold θ_{GA} . Next, two classifiers (i.e. the parents) are selected by roulette wheel selection based on fitness and the offspring are created out of them. After that, the offspring are possibly crossed and mutated. If the offspring are crossed, their prediction values are set to the average of the parents' values. Finally, the offspring are inserted in the population, followed by corresponding deletions. However, if GA subsumption is being used, each offspring is first tested to see if it is subsumed by either of its parents; if so, that offspring is not inserted in the population, and the subsuming parent's numerosity is increased. (Besides checking if an offspring is subsumed by a parent, one could also check if it is subsumed by other classifiers in the action set, or even the population as a whole.)

```
RUN GA([A], \sigma, [P]):
 1 if(actual time t - \sum_{cl \in [A]} ts_{cl} * num_{cl} / \sum_{cl \in [A]} num_{cl} > 	heta_{GA})
         for each classifier cl in [A]
 3
              ts_{cl} \leftarrow \texttt{actual time } t
 4
         parent_1 \leftarrow \texttt{SELECT} \ \texttt{OFFSPRING} \ \texttt{in} \ [A]
 5
         parent_2 \leftarrow \texttt{SELECT OFFSPRING in } [A]
 6
         child_1 \leftarrow \texttt{copy classifier } parent_1
 7
         child_2 \leftarrow \texttt{copy classifier } parent_2
 8
         num_{child_1} = num_{child_2} \leftarrow 1
 9
         exp_{child_1} = exp_{child_2} \leftarrow 0
10
         if (RandomNumber [0,1[ < \chi)
11
              APPLY CROSSOVER on child_1 and child_2
12
              p_{child_1} \leftarrow (p_{parent_1} + p_{parent_2})/2
13
              \epsilon_{child_1} \leftarrow 0.25 * (\epsilon_{parent_1} + \epsilon_{parent_2})/2
14
              f_{child_1} \leftarrow 0.1 * (f_{parent_1} + f_{parent_2})/2
15
              p_{child_2} \leftarrow p_{child_1}
16
              \epsilon_{child_2} \leftarrow \epsilon_{child_1}
17
              f_{child_2} \leftarrow f_{child_1}
18
         for both children child
19
              APPLY MUTATION on child according to \sigma
20
              if(doGASubsumption)
21
                   if (DOES SUBSUME parent_1, child)
22
                       num_{parent_1}++
23
                   else if (DOES SUBSUME parent_2, child)
24
                       num_{parent_2}++
25
                   else
26
                       INSERT child IN POPULATION
27
              else
28
                   INSERT child IN POPULATION
29
              DELETE FROM POPULATION [P]
```

The sub-procedures *INSERT IN POPULATION* and *DELETE FROM POPULATION* are defined in section 3.2.7 and the others in the following paragraphs.

Roulette-Wheel Selection The Roulette-Wheel Selection chooses a classifier for reproduction proportional to the fitness of the classifiers in set [A]. First, the sum of all the fitnesses in the set [A] is computed. Next, the roulette-wheel is spun. Finally, the classifier is chosen according to the roulette-wheel result.

```
SELECT\ OFFSPRING([A]):
1\ fitnessSum \leftarrow 0
2\ for\ each\ classifier\ cl\ in\ [A]
3\ fitnessSum \leftarrow fitnessSum\ +\ f_{cl}
4\ choicePoint \leftarrow \texttt{RandomNumber}\ [\texttt{0,1[*fitnessSum}
5\ fitnessSum \leftarrow 0
6\ for\ each\ classifier\ cl\ in\ [A]
7\ fitnessSum \leftarrow fitnessSum\ +\ f_{cl}
8\ if(fitnessSum\ >\ choicePoint)
9\ return\ cl
```

Crossover The crossover procedure is similar to the standard crossover procedure in GAs. Implementations of XCS with one point and two point crossover were tested and resulted in approximately identical results. In the *APPLY CROSSOVER* procedure we show two-point crossover. The actions are not affected by crossover.

```
APPLY\ CROSSOVER(c_1,\,c_2):

1 x\leftarrow RandomNumber [0,1[ * (LENGTH of C_{c_1} +1)
2 y\leftarrow RandomNumber [0,1[ * (LENGTH of C_{c_1} +1)
3 if (x>y)
4 switch x and y
5 i\leftarrow 0
6 do{
7 if (x\leq i \text{ and } i< y)
8 switch C_{cl_1}[i] and C_{cl_2}[i]
9 i++
10 }while (i< y)
```

A more sophisticated crossover could include assurance that x and y are different. However, even without such special checks the algorithm serves its purpose.

Mutation While crossover does not affect the action, mutation takes place in both the condition and the action. A mutation in the condition flips the attribute to one of the other possibilities. Mutation in the action changes it equiprobably to one of the other actions. Though more time-efficient methods are possible, we present here the simple one in which a die is flipped for each attribute. Since in XCS most of the time is spent in processes that operate on the whole population such as matching and deletion, the type of algorithm used for mutation only slightly affects efficiency. Note that our mutation is somewhat restricted. Rather than allowing an attribute of the condition to change to any other attribute, we only allow changes either to # or to the specific value that matches the corresponding component of $\sigma(t)$. Thus the resulting condition still matches the current input. The effect (if the action is unchanged) is to search the current action set niche along

the axis of specificity vs. generality. Less restricted mutation schemes are of course possible.

```
APPLY MUTATION(cl, \sigma):
 1 i \leftarrow 0
 2 do{
 3
        if (RandomNumber [0,1[<\mu])
 4
             if(C_{cl}[i] = \#)
                C_{cl}[i] \leftarrow \sigma[i]
 5
 6
                C_{cl}[i] \leftarrow \#
 7
 8
        i++
   \}while(i < length of <math>C_{cl})
   if (RandomNumber [0,1[ < \mu)
11
        A_{cl} \leftarrow a randomly chosen other possible action
```

3.2.7 Insertion in and Deletion from the Population

This section covers processes that handle the insertion and deletion of classifiers in the current population [P].

The INSERT IN POPULATION procedure checks to see if the classifier to be inserted is identical in condition and action with a classifier already in the population. If so, the latter's numerosity is incremented; if not, the new classifier is added to the population.

```
INSERT IN POPULATION(cl, [P]):

1 for all c in [P]

2 if(c is equal to cl in condition and action)

3 num_c++

4 return

5 add cl to set [P]
```

The deletion procedure realizes two ideas at the same time: (1) it assures an approximately equal number of classifiers in each action set, or environmental 'niche'; (2) it removes low-fitness individuals from the population. The following paragraphs describe the *DELETE FROM POPU-LATION* procedure and the *DELETION VOTE* sub-procedure.

Roulette-Wheel Deletion Like the selection procedure, the deletion procedure chooses individuals (for deletion) by roulette-wheel selection. But first, the procedure checks to see if the sum of classifier numerosities in [P] is less than N. If so, the procedure exits, as deletion is unnecessary. Otherwise, the sum of all deletion votes is calculated, and a classifier is chosen for deletion. If the classifier is a macro-classifier and currently represents more than one classifier, then its numerosity is merely decreased by one. Otherwise, the classifier is completely removed from the population.

```
DELETE\ FROM\ POPULATION([P]):
 1 if(\sum_{c \in [P]} num_c < N)
 2
        return
 3 \ voteSum \leftarrow 0
   for each classifier c in [P]
        voteSum \leftarrow voteSum + \texttt{DELETION} \ \texttt{VOTE} \ \texttt{of} \ c \ \texttt{in} \ [P]
   choicePoint \leftarrow \texttt{RandomNumber} \ [\texttt{0,1[}*voteSum
   voteSum \leftarrow 0
 7
   for each classifier c in [P]
 9
        voteSum \leftarrow voteSum + DELETION VOTE of c
10
        if(voteSum > choicePoint)
            if(num_c > 1)
11
12
                num_c--
13
            else
14
                remove classifier c from set [P]
15
            return
```

The Deletion Vote As mentioned above, the deletion vote realizes niching as well as removal of the lowest fitness classifiers. The deletion vote of each classifier is based on the action set size estimate as. Moreover, if the classifier has sufficient experience and its fitness is significantly lower than the average fitness in the population, the vote is increased in inverse proportion to the fitness. In this calculation, since we are deleting one micro-classifier at a time, we need to use as fitness the (macro)classifier's fitness divided by its numerosity. The following DELETION VOTE procedure realizes all this.

```
DELETION VOTE(cl, [P]):

1 vote \leftarrow as_{cl} * num_{cl}

2 averageFitnessInPopulation \leftarrow \sum_{c \in [P]} f_c / \sum_{c \in [P]} num_c

3 if(exp_{cl} > \theta_{del} and f_{cl} / num_{cl} < \delta * averageFitnessInPopulation)

4 vote \leftarrow vote * averageFitnessInPopulation / ( <math>f_{cl} / num_{cl})

5 return vote
```

3.2.8 Subsumption

Two subsumption procedures were introduced into XCS in Wilson (1998). The first, 'GA subsumption', checks an offspring classifier to see if its condition is logically subsumed by the condition of an accurate and sufficiently experienced parent. If so, the offspring is not added to the population, but the parent's numerosity is incremented. The idea is that such an offspring cannot improve the system's performance, since everything it accomplishes is accomplished just as well by the subsuming parent. GA subsumption, if enabled, occurs within the procedure RUNGA. It is detailed within that procedure, and is not called as a sub-procedure (though it could be). However, the sub-procedure $DOES\ SUBSUME$ is called, and is described in this section.

The second subsumption procedure, 'action set subsumption', if enabled, takes place in every action set. It has a purpose similar to GA subsumption but is different and independent of it. The action set is searched for the most general classifier that is both accurate and sufficiently experi-

enced. Then all other classifiers in the set are tested against the general one to see if it subsumes them. Any classifiers that are subsumed are eliminated from the population.

```
DO ACTION SET SUBSUMPTION([A], [P]):
 1 initialize cl
 2 for each classifier c in [A]
       if (c COULD SUBSUME)
 4
          if (cl) is empty or c IS MORE GENERAL than cl)
 5
              cl \leftarrow c
 6
   if(cl) is not empty)
 7
       for each classifier c in [A]
 8
          if (cl \text{ IS MORE GENERAL than } c)
 9
              num_{cl} \leftarrow num_{cl} + num_{c}
              remove classifier c from set [A]
10
11
              remove classifier c from set [P]
```

Subsumption of a classifier For a classifier to subsume another classifier, it must first be sufficiently accurate and sufficiently experienced. This is tested by the COULD SUBSUME function. Then, if a classifier could be a subsumer, it must be tested to see if it has the same action and is really more general than the classifier that is to be subsumed. This is the case if the set of situations matched by the condition of the potentially subsumed classifier form a proper subset of the situations matched by the potential subsumer. The IS MORE GENERAL procedure accomplishes this. The DOES SUBSUME procedure combines all the requirements.

```
DOES\ SUBSUME(cl_{sub},\ cl_{tos}):
1\ \text{if}(A_{cl_{sub}}=A_{cl_{tos}})
2\ \text{if}(cl_{sub}\ \text{COULD}\ \text{SUBSUME})
3\ \text{if}(cl_{sub}\ \text{IS}\ \text{MORE}\ \text{GENERAL}\ \text{than}\ cl_{tos})
4\ \text{return}\ true
5\ \text{return}\ false
COULD\ SUBSUME(cl):
1\ \text{if}(exp_{cl}>\theta_{sub})
2\ \text{if}(\epsilon_{cl}<\epsilon_{0})
3\ \text{return}\ true
4\ \text{return}\ false
```

```
IS MORE GENERAL(cl_{gen}, cl_{spec}):

1 if (the number of # in C_{cl_{gen}} \leq the number of # in C_{cl_{spec}})

2 return false

3 i \leftarrow 0

4 do{

5 if (C_{cl_{gen}}[i] \neq \text{# and } C_{cl_{gen}}[i] \neq C_{cl_{spec}}[i])

6 return false

7 ni++

8 }while (i < \text{length of } C_{cl_{gen}})

9 return true
```

4 Summary

This paper has revealed the processes inside XCS as well as the problem interaction. We hope that presentation of the algorithm in pseudo code with explanations will lead to deeper understanding of XCS and simplify research. Moreover, the modular structure should enable the reader to program the system in any programming language quite easily. However, our description only includes the basic framework of XCS. Starting from this baseline, we encourage modification as well as enhancement of the system, and welcome feedback on progress and results.

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