

Master of Science in Information Systems  
Business Analytics

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**Predicting the Norwegian Elspot markets:  
Evaluation of Methods and Price-drivers**

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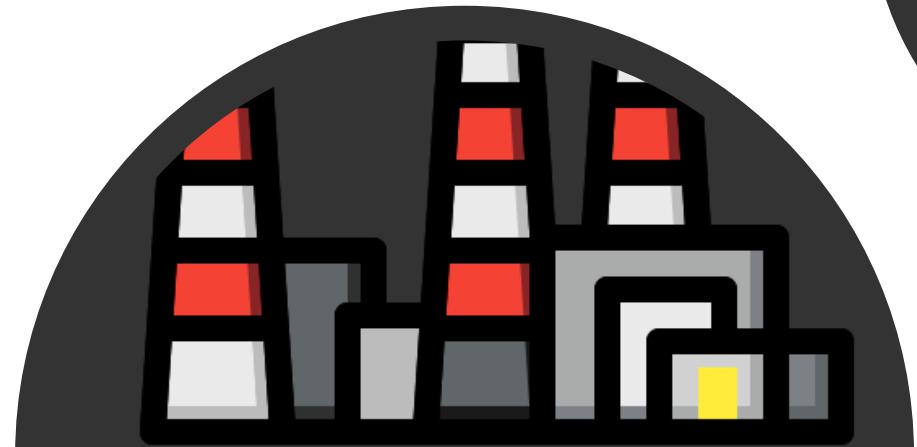
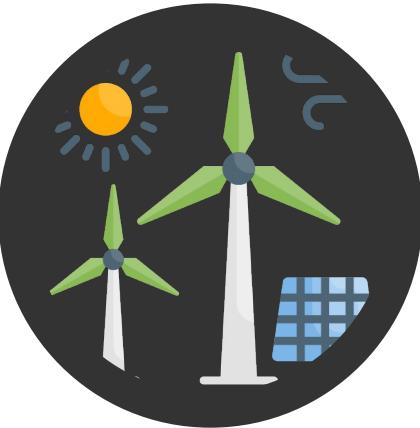
Markus W. Jensen

Candidate: 1065



# Background and Motivation

- Use of energy is strongly related to almost every conceivable aspect of development
- Forecasting is crucial in the efficient functioning of electricity markets
- Norwegian markets role in deregulation, renewable integration and recent disruption



# Research questions

- Which price drivers shape the behaviour of the elspot markets in Norway?
- Which methods are most effective in forecasting the hourly day-ahead elspot prices in Norway?

# Background Theory

## Electricity Consumption and Generation

- Electricity consumption
- Electricity production

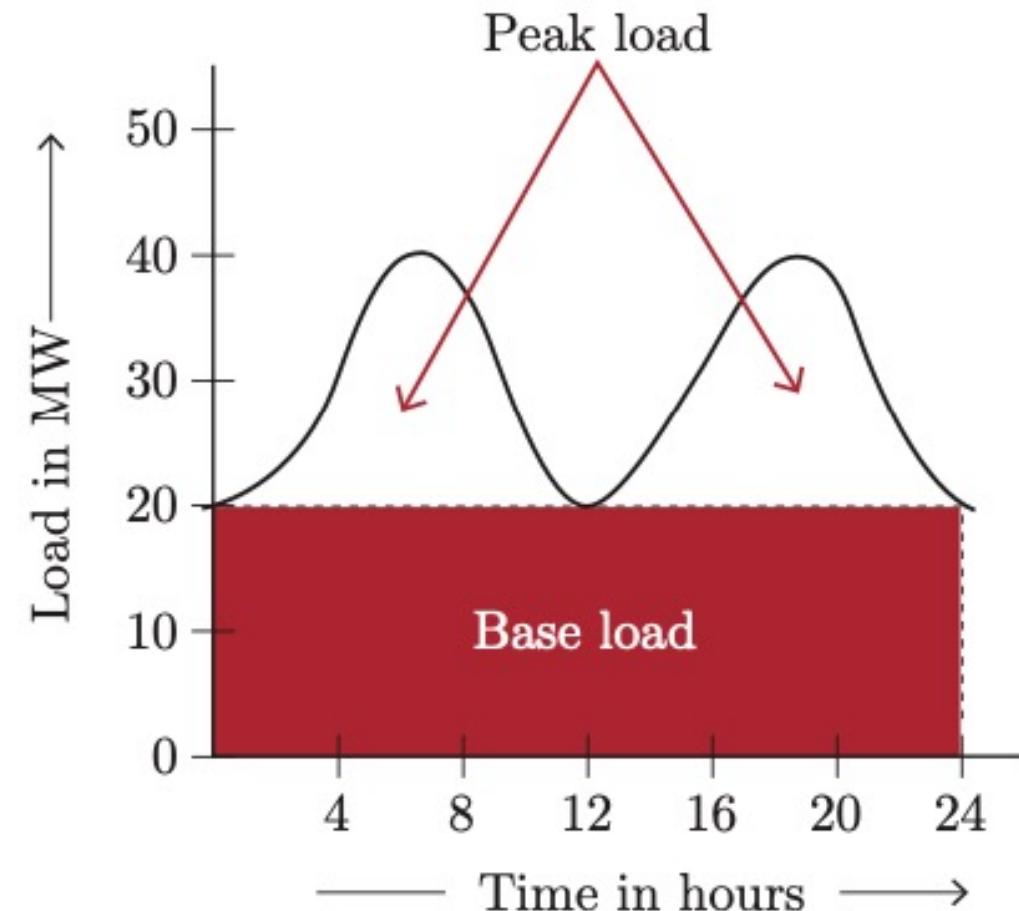


Figure 1: Base-load vs. Peak-load.

# Electricity markets and pricing

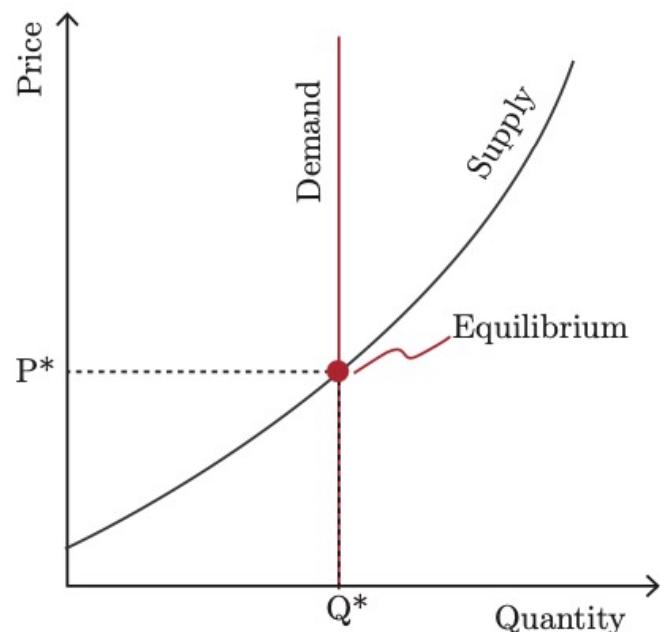
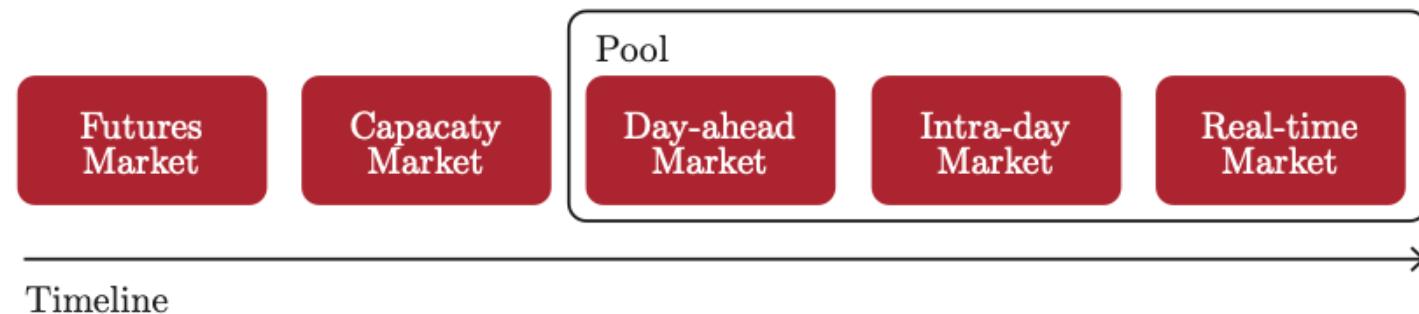


Figure 3: Equilibrium-curve for determining the market clearing price (spot-price).

Figure 2: The Fragmented Market Scheme.

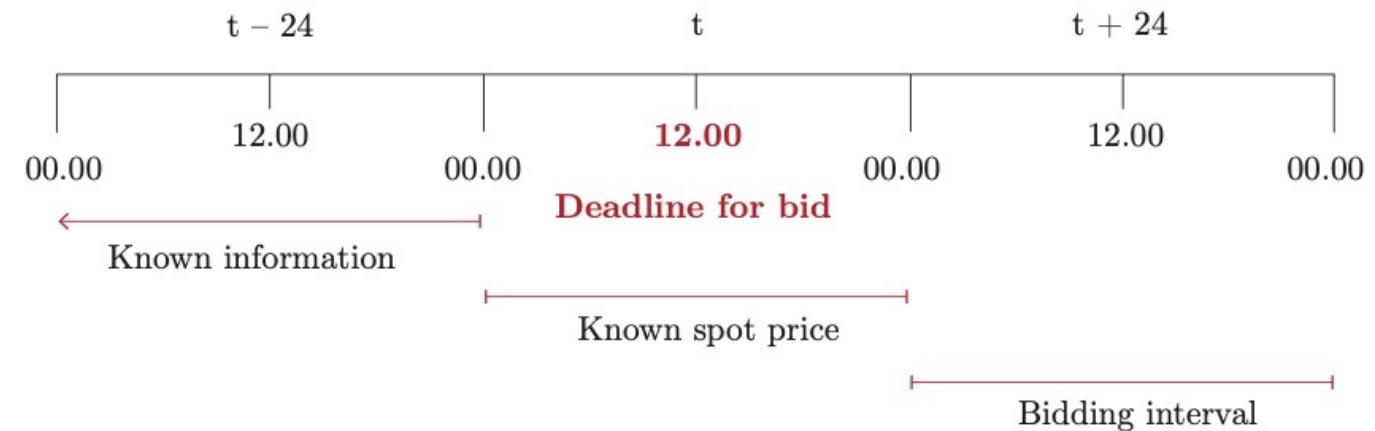


Figure 4: Deadline for bids.

# Machine Learning

- Fits mathematical models to data
- “no free lunch”
- Representation
- Evaluation
- Optimization
- Error components
- Bias-variance trade-off
- Regularization
- Ensembling
- Deep Learning

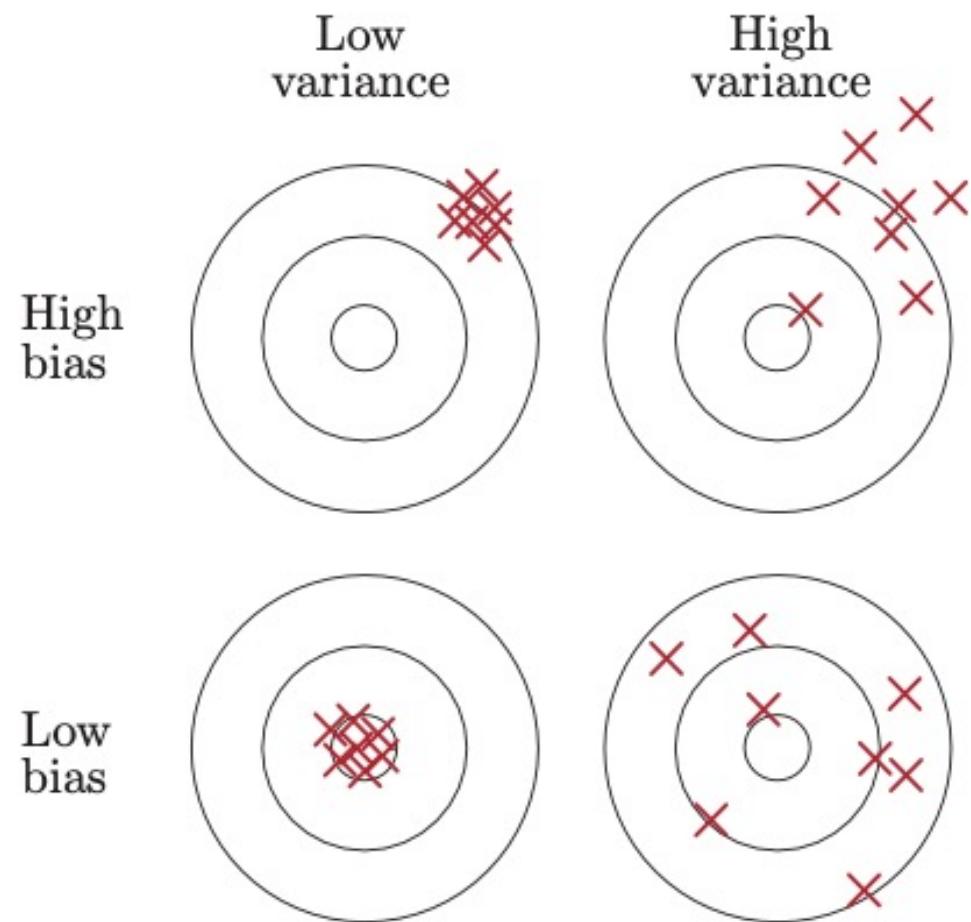
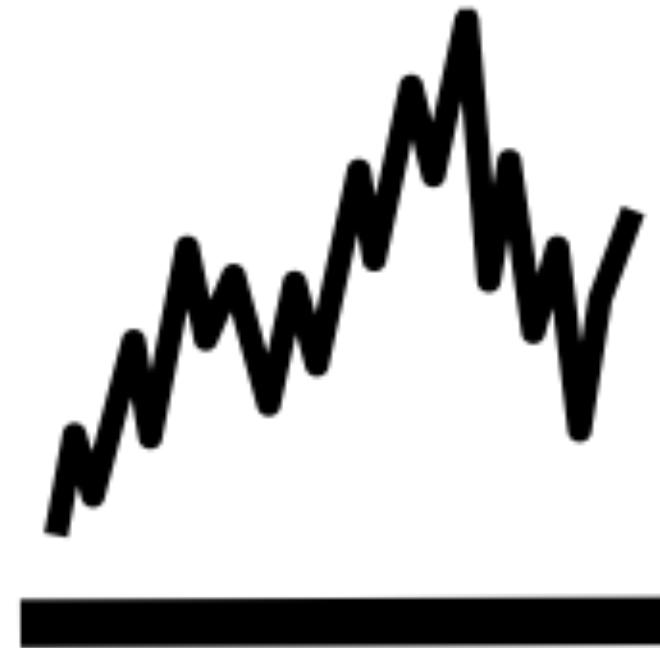


Figure 7: Bias and variance in dart-throwing.

# Time Series Forecasting

$$X = X_{t=1}^{\infty} = (X_1, X_2, \dots)$$

- Look-ahead-bias
- Stationarity
- Auto-correlation
- Smoothing
- Components
- Differencing



# Related work

Approach	Papers
Long-term price modeling	[48, 24, 14]
Day-ahead-prices (spot) forecasting	[15, 32, 33, 51, 26, 39, 25, 6, 47, 4, 3, 16, 18]
Hourly prices (intraday) forecasting	[35, 23, 9, 10, 37]
Regulating price modeling	[42]

Table 1: Previous targets.

Input Variables	Papers
Previous prices	[3, 37, 18, 14, 25, 33, 35, 30, 15, 4, 42, 51, 26, 39, 16, 47, 6, 23, 9, 32, 10]
System loads	[37, 18, 25, 33, 35, 30, 39, 47]
Weather variables	[18, 48, 35, 26, 9]
Fuel costs	[28, 6, 9]
Sector indeces	[43]
Reserve margin	[30, 37, 42]
Generation costs	[30]

Table 2: Previous input-variables.

Pre-processing	Papers
Interpolation of Missing Values	[47]
Lagged Variables	[3]
Mean Normalization	[47, 9]
Min-max Scaling	[3, 10]
Wavelet Transform	[33, 15, 37, 51, 26, 10]
Differentiation	[16]

Table 3: Previous pre-processing techniques.

Feature Selection	Papers
Gaussian Radial Basis Function (GRBF) network	[28]
Principle Component Analysis (PCA)	[39]

Table 4: Previous feature-selection techniques.

Model Type	Papers
Fundamental Models	[14, 30]
Statistical Models	[42, 30, 48, 18, 33, 51, 18, 15, 26, 16, 47, 6, 23]
Deep-learning Models	[3, 25, 33, 35, 28, 30, 3, 37, 23, 18, 32, 10]
Ensemble Models	[6, 9]
Hybrid Models	[51, 37, 32]

Table 5: Previous model types.

# Limitations of related work

- Lack of transparency and details
- Bias in model selection
- Convolved
- Lack of baseline

# Research Method

- Theoretical, empirical and practical
  - Statistically rigorous and systematic
  - Bottom-up approach
  - Absolute terms
1. Research on price-drivers
    - Data collection
    - Exploratory data analysis
    - Model interpretation
  2. Research on methods
    - Model evaluation
    - Naive baseline
    - Statistical/econometric
    - Algorithmic ensemble
    - Deep learning
    - Experiments

# Research on price-drivers

- Data selection and collection
- Exploratory analysis
  - Visualizations
  - Auto-correlation
  - Descriptive statistics
  - Correlation
  - Principal Component Analysis
  - ADF statistics
- Model interpretation
  - Univariate vs Multivariate configurations
  - XGBoost Feature importance
  - Comparing bidding-zones and performances on bidding-zones

# Research on methods

- Model evaluation
- Experiments
  - 365-fold rolling forecast origin cross validation
  - Out-of-sample evaluation on recent hold-out test set
  - Total 84 forecast considering models, experiments and configurations
- Methods
  - Weak/general assumptions
  - Different theoretical vantage points
  - SOTA from each model-family

$$MSE = \frac{1}{n} \sum_{i=1}^n (\text{actual}_i - \text{predicted}_i)^2$$

$$RMSE = \sqrt{\frac{1}{n} \sum_{i=1}^n (\text{actual}_i - \text{predicted}_i)^2}$$

$$MAE = \frac{1}{n} \sum_{i=1}^n |\text{actual}_i - \text{predicted}_i|$$

$$MAPE = \frac{1}{n} \sum_{i=1}^n \left| \frac{\text{actual}_i - \text{predicted}_i}{\text{actual}_i} \right| \times 100$$

$$RSS = \sum_{i=1}^n (\text{actual}_i - \text{predicted}_i)^2$$

# Naïve baseline

- Persistence forecast
- Heuristic (“price tomorrow is the same as the price today”)
- Predicts the current value as the value in 24-timesteps
- Easy to implement
- Surprisingly accurate
- Lower bound of performance

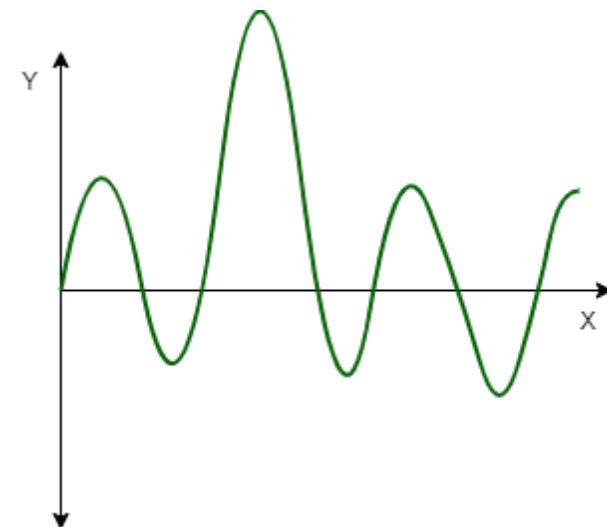
$$\hat{P}_t = P_{t-24}$$

# Statistical/econometric approach

- Autoregressive Integrated Moving Average (ARIMA(p,d,q))

$$Y_t = c + \sum_{i=1}^p \Phi_i Y_{t-i} + \varepsilon_t - \sum_{j=1}^q \theta_j \varepsilon_{t-j}$$

- $Y_t$  is the value of the timeseries at time t
- C is a constant term
- $\Phi_1, \Phi_2, \dots, \Phi_p$  are the AR coefficients
- $\varepsilon_t$  is the error term at time t
- $\theta_1, \theta_2, \dots, \theta_q$  are the MA coefficients
- P, d, q are integers that represent the order of the AR, differencing and MA components, respectively



# Algorithmic ensemble approach

- XGBoost: A gradient boosting framework
- Combines multiple weak models (decision trees) to make a strong prediction

The objective function for XGBoost can be written as:

$$\mathcal{L}(\Theta) = \sum_{i=1}^n l(y_i, \hat{y}_i) + \sum_{k=1}^K \Omega(f_k)$$

- $\Theta$  represents the set of model parameters
- $n$  is the number of training examples
- $y_i$  is the true value of the  $i$ -th example
- $\hat{y}_i$  is the predicted value
- $l(y_i, \hat{y}_i)$  is the loss function
- $K$  is the number of weak models in the ensemble
- $f_k$  represents the  $k$ -th weak model
- $\Omega(f_k)$  is the regularization term that penalizes complex models



The weak models used in XGBoost are decision trees, which can be expressed as:

$$f(x) = \sum_{t=1}^T w_t q_t(x), \quad w \in \mathbb{R}^T, \quad q: \mathbb{R}^d \rightarrow \{1, 2, \dots, T\}$$

# Deep learning approach

- LSTM (Long Short-Term Memory)
- Type of RNN (recurrent neural network) for seq-to-seq tasks
- Vanishing gradients
- Specialized memory unit
  - Input gates
  - Forget gates
  - Output gates
- Combined with feed-forward layers

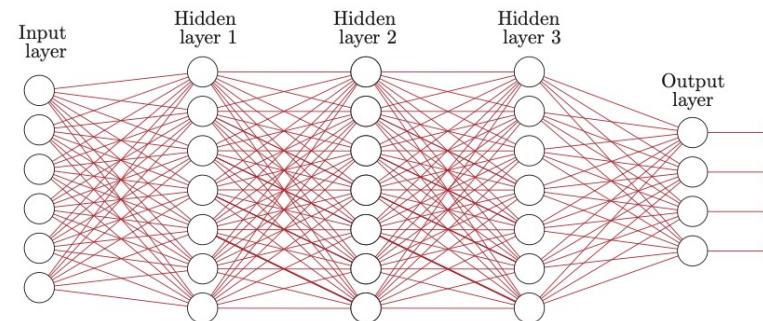


Figure 8: Deep Neural Network.

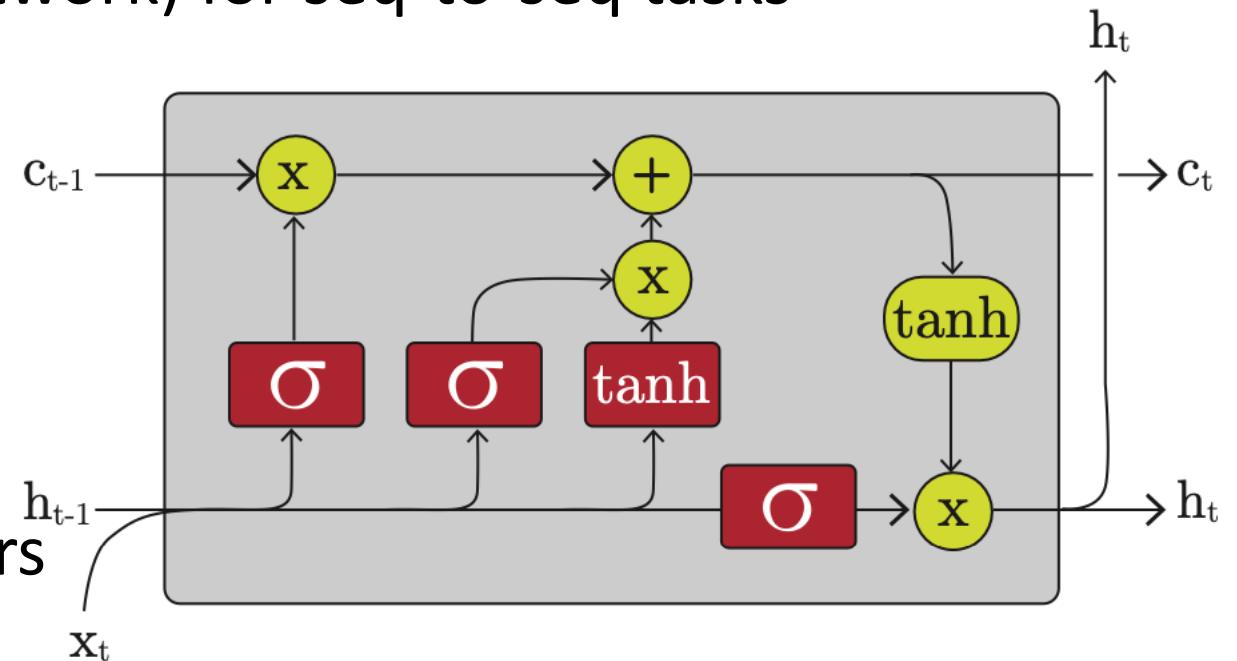
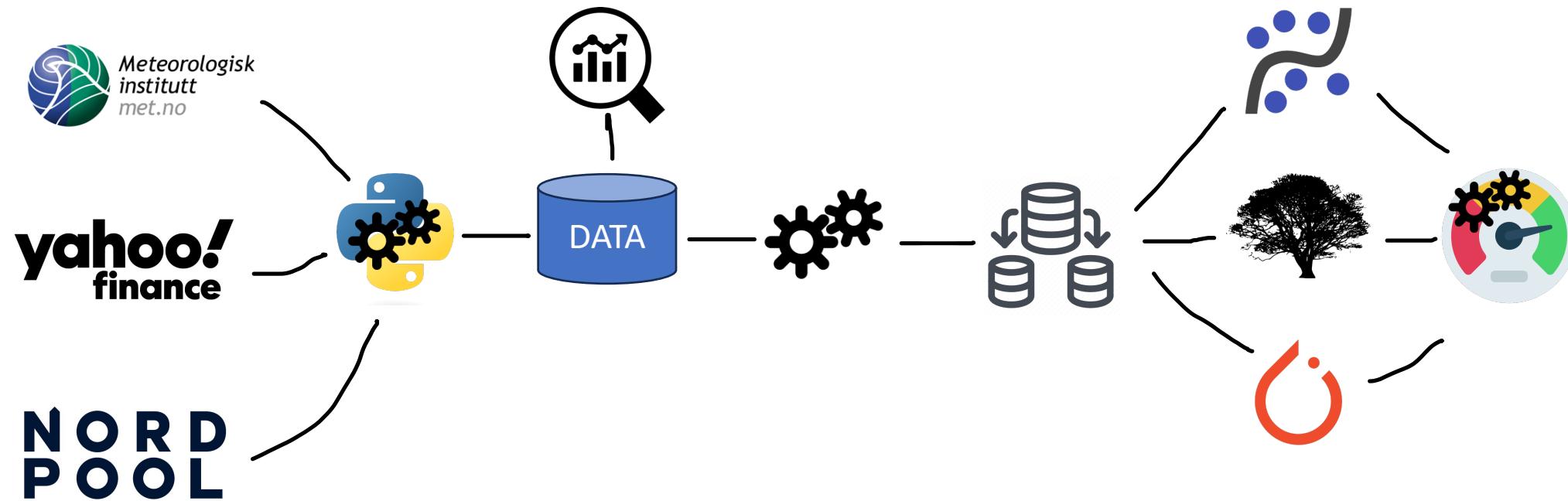


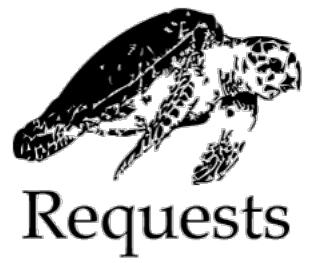
Figure 10: Long Short-Term Memory Network Diagram (LSTM).

# Design and Implementation



# Data collection

Period: 01.01.2020 – 30.03.2023



Variable (units) [granularity]	Description (source) [bidding-zones]
Elspot price (NOK/MWh) [h]	Settlement prices (Nordpool) [NO1-NO6].
Elspot day-ahead price (NOK/MWh) [h]	Day-ahead price targets (Nordpool) [NO1-NO6].*
Power production (MWh) [h]	Settlement of production bids (Nordpool) [NO1-NO6].
Power production prognosis (MWh) [h]	Day-ahead prognosis of production bids (Nordpool) [NO1-NO6].
Exchange (MWh) [h]	Exchange between bidding-zones including export/import (Nordpool) [NO1-NO6].
Power consumption (MWh) [h]	Total consumption (Nordpool) [NO1-NO6].
Reservoir levels (GWh) [w]	Hydro reservoir content (Nordpool).
Reservoir capacity (GWh) [w]	Total hydro reservoir content capacity (Nordpool).
Gas price (NOK/mmbtu) [d]	LNG-price per million british thermalunits (Yahoo-finance).
Oil price (NOK/barrel) [d]	Oil-price per barrel (Yahoo-finance).
OSEBX price (NOK/OSEBX) [d]	Oslo Børs Benchmark Index price (Yahoo-finance).
Air temperature (mean/degC) [d]	Temperature averaged by bidding-zones (Met) [NO1-NO6].
Wind speed (mean/ms) [d]	Wind speed averaged by bidding-zones (Met) [NO1-NO6].
Precipitation (sum/mm) [d]	Precipitation averaged by bidding-zones (Met) [NO1-NO6].

Table 6: Description of data.

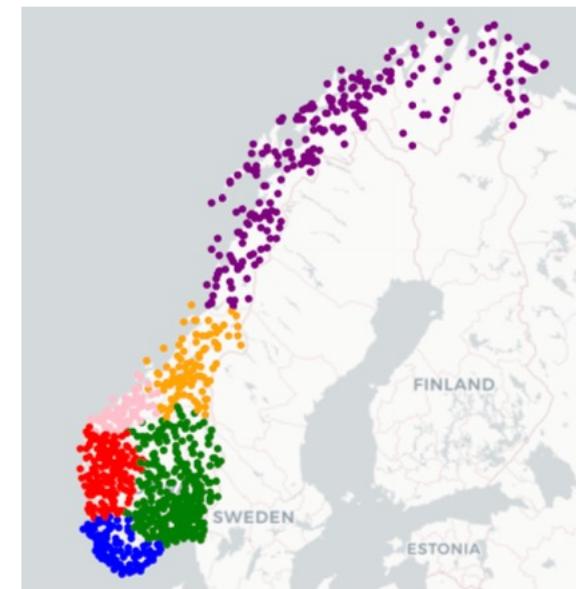
\*Target variables

# Oparational data



NORD  
POOL

# Weather data

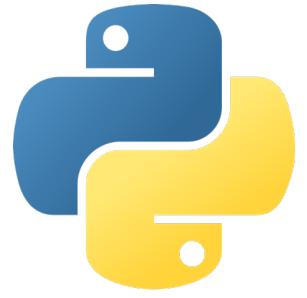


- █ NO1: Oslo
- █ NO2: Kr.sand
- █ NO3: Molde
- █ NO4: Tromsø
- █ NO5: Bergen
- █ NO6: Tr.heim

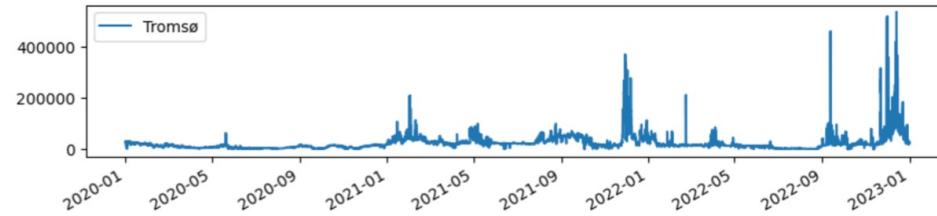
Figure 11: Locations of weather stations color-labeled by bidding zones.

# Financial data

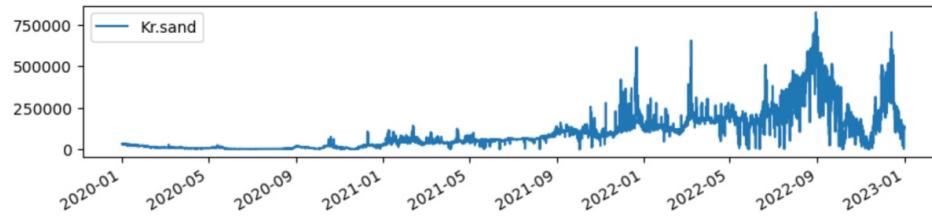
**yahoo!**  
finance



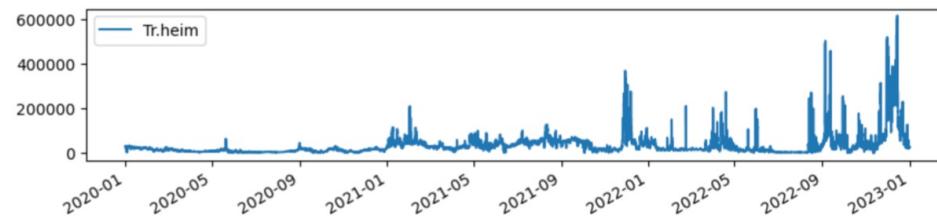
# Exploratory analysis



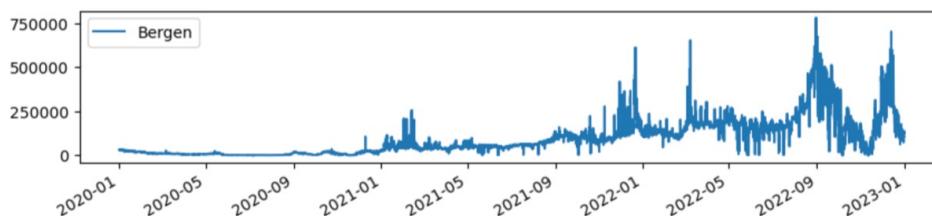
(a) Tromsø (NO4).



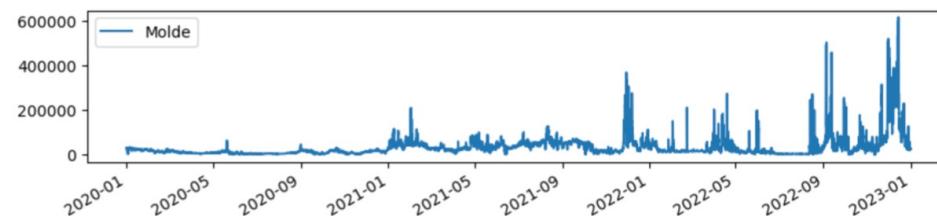
(b) Kristiansand (NO2).



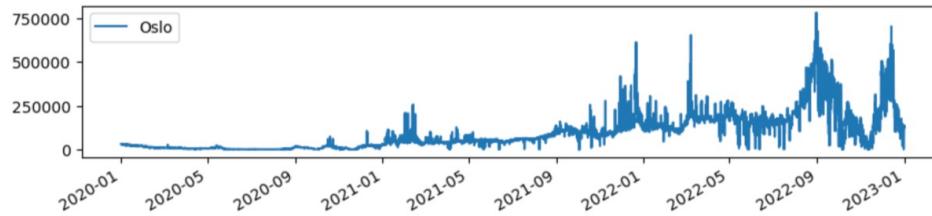
(c) Trondheim (NO6).



(d) Bergen (NO5).



(e) Molde (NO3).



(f) Oslo (NO1).

Figure 12: Historical prices from 1.1.2020-31.12.2022 in each bidding zone.

# Decomposition

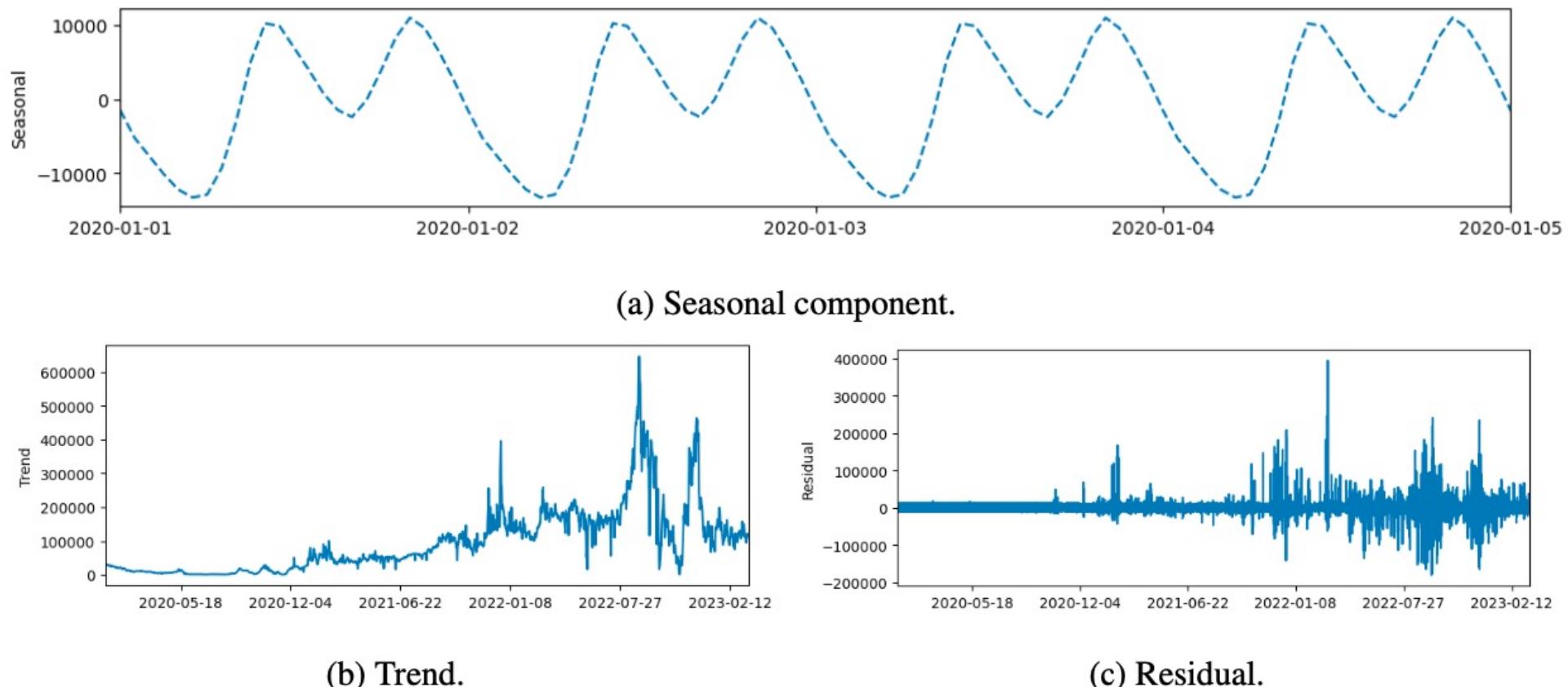
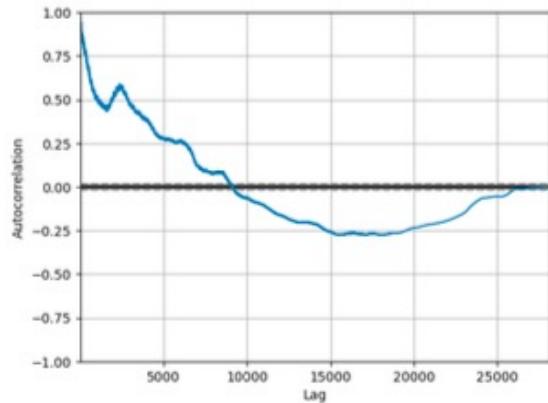
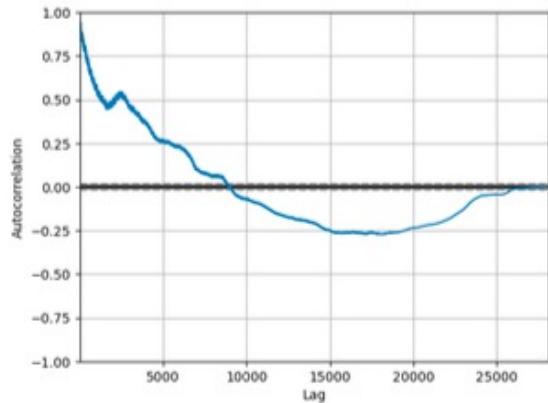


Figure 13: Additive decomposition of time series (NO1).

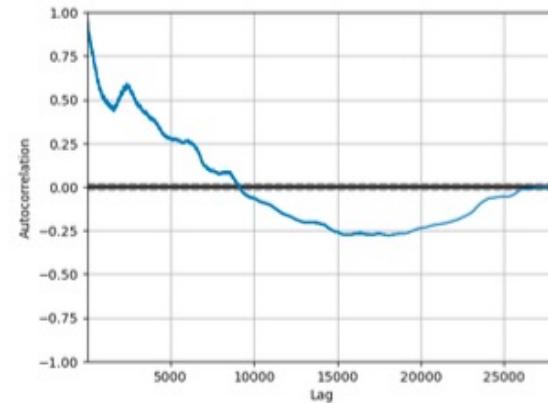
# Autocorrelation



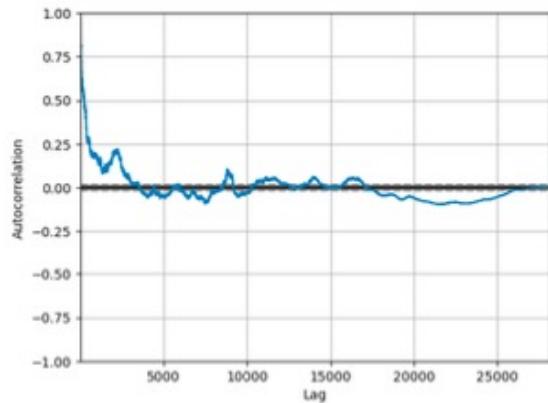
(a) Oslo (NO1).



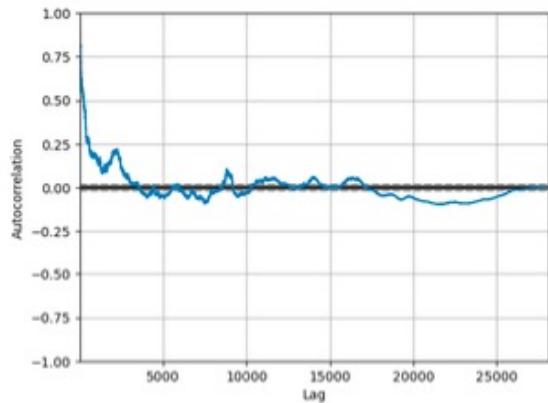
(b) Kristiansand (NO2).



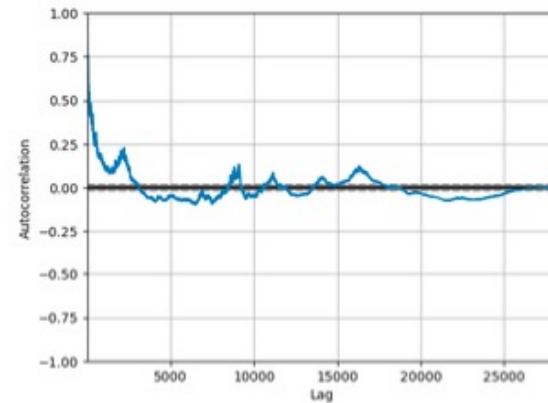
(c) Bergen (NO5).



(d) Molde (NO3).



(e) Trondheim (NO6).



(f) Tromsø (NO4).

Figure 14: Auto-correlation function (ACF) of historical elspot prices.

# Partial autocorrelation

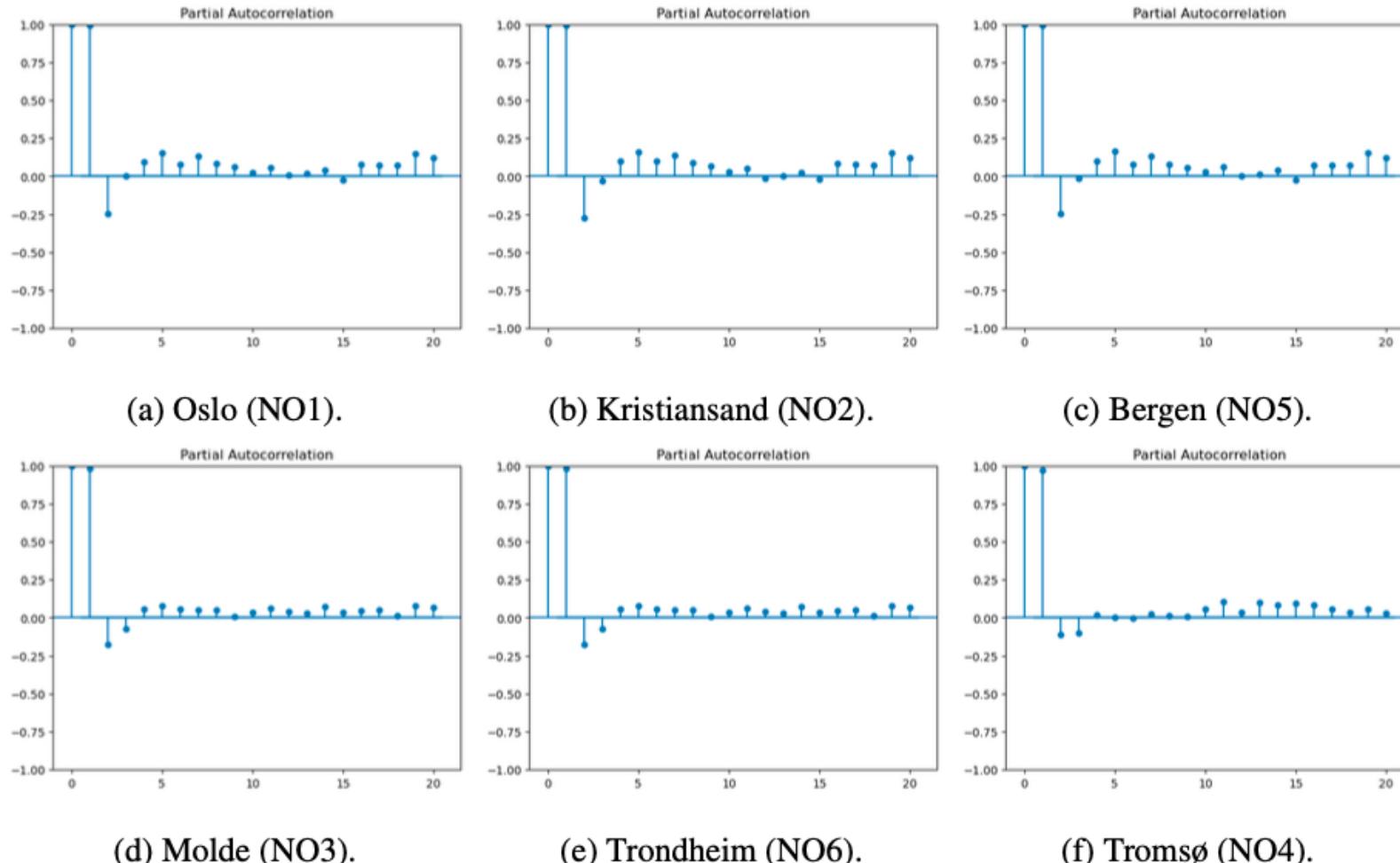


Figure 15: Partial auto-correlation function (PACF) of historical elspot prices.

# Descriptive statistics

	<b>Oslo</b>	<b>Kr.sand</b>	<b>Bergen</b>	<b>Molde</b>	<b>Tr.heim</b>	<b>Tromsø</b>
<i>mean</i>	94888	100901	94641	33437	33437	24650
<i>std</i>	100203	111353	99828	45960	45960	31427
<i>min</i>	-1972	-1972	-96	-2137	-2137	-1058
25%	16089	16101	16300	9695	9695	8995
50%	62348	62670	62419	19904	19904	16580
75%	141576	143056	140894	43740	43740	28782
<i>max</i>	782033	822463	782033	617574	617574	533509

Table 7: Descriptive statistics of historical elspot-prices (NOK).

# Visualizations

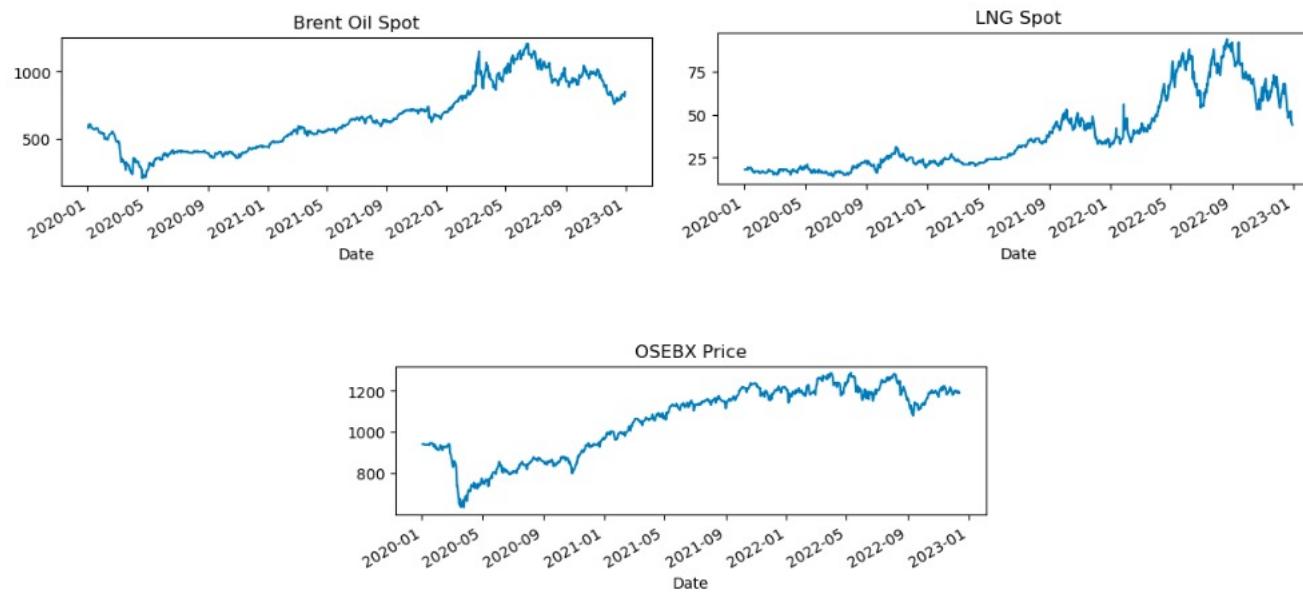


Figure 18: Historical economic variables (NOK).

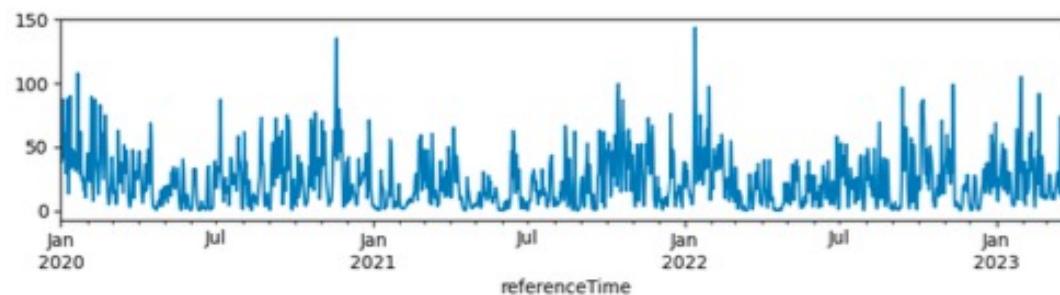


Figure 16: Precipitation.

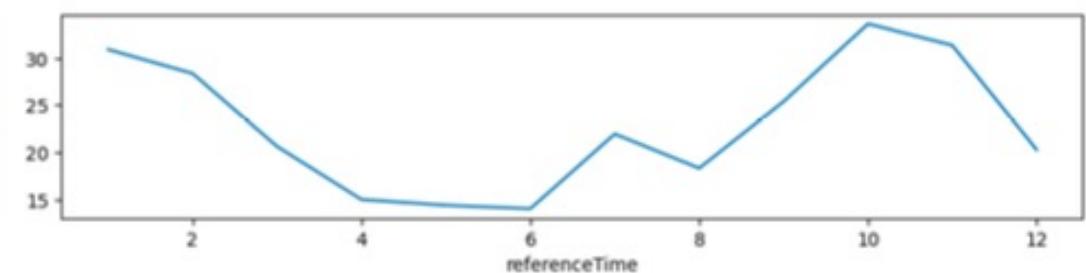
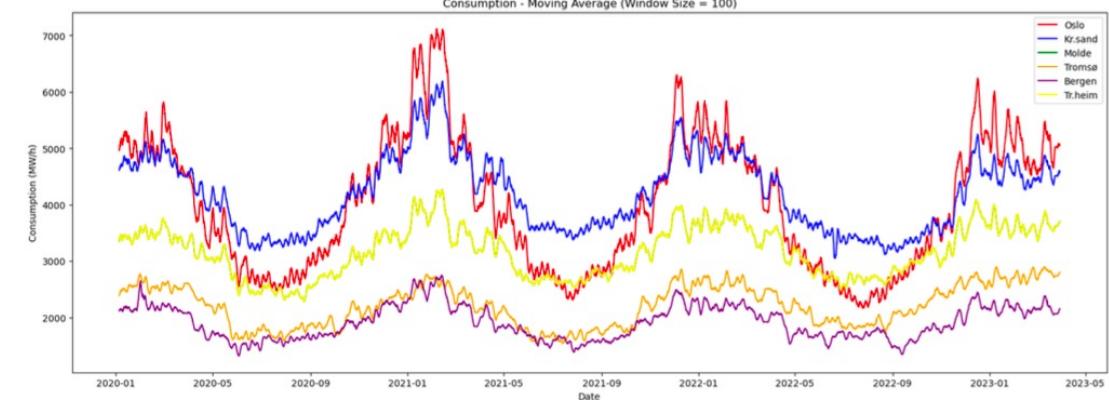
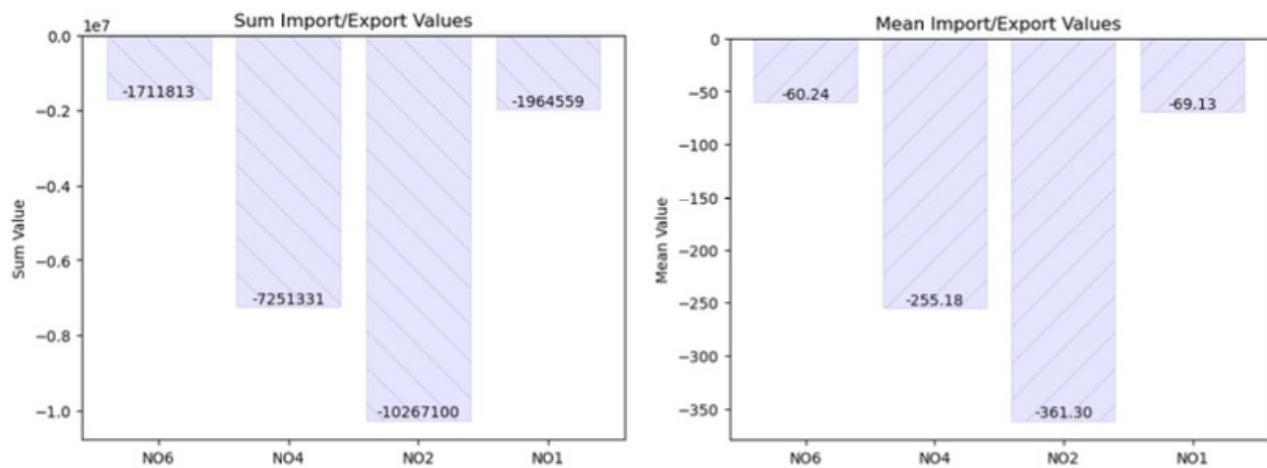


Figure 17: Precipitation averaged by month.

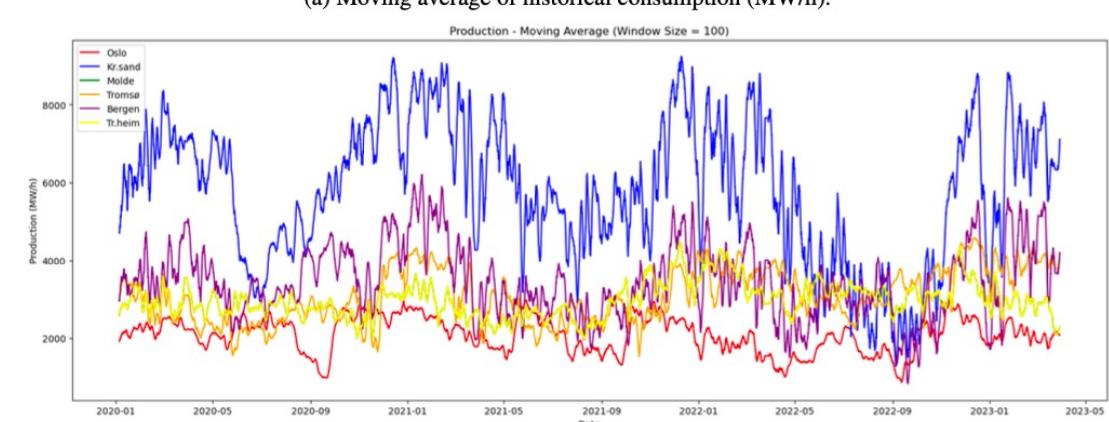


(a) Moving average of historical consumption (MW/h).

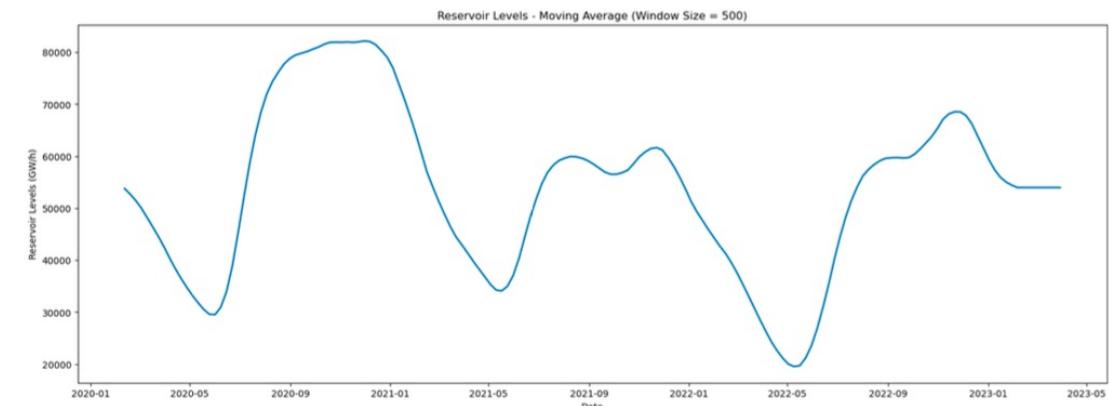


(a) Sum.

(b) Mean.



(b) Moving average of historical production (MW/h).



(c) Historical reservoir levels in Norway (GW/h)

Figure 19: Inter-Country Import/Export of Electricity (MW/h).

# Correlation

	<b>Oslo</b>	<b>Kr.sand</b>	<b>Bergen</b>	<b>Molde</b>	<b>Tr.heim</b>	<b>Tromsø</b>
<b>Oslo</b>	1.0000	0.9719	0.9984	0.4722	0.4722	0.3562
<b>Kr.sand</b>	0.9719	1.0000	0.9703	0.3975	0.3975	0.2815
<b>Bergen</b>	0.9984	0.9703	1.0000	0.4728	0.4728	0.3572
<b>Molde</b>	0.4722	0.3975	0.4728	1.0000	1.0000	0.8104
<b>Tr.heim</b>	0.4722	0.3975	0.4728	1.0000	1.0000	0.8104
<b>Tromsø</b>	0.3562	0.2815	0.3572	0.8104	0.8104	1.0000

Table 9: Pearson correlation between bidding-zones.

# Exogenous variables

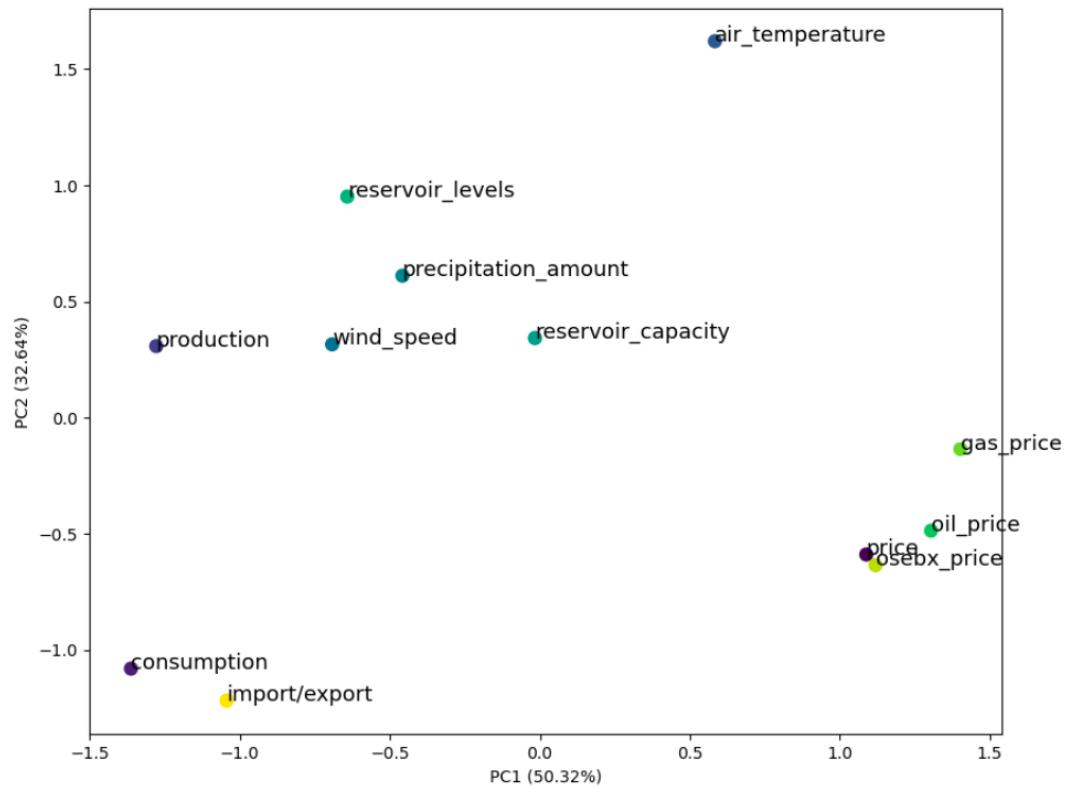


Figure 22: Approximation and projection of variables onto two-dimensional feature-space (PCA).

	price	consumption	production	da_production	air_temperature	wind_speed	precipitation_amount	reservoir_capacity	reservoir_levels	oil_price	gas_price	osebx_price	import/export	target
price	1	-0.027	-0.29	-0.3	-0.074	-0.23	-0.11	0.038	-0.16	0.68	0.76	0.67	0.24	0.95
consumption	-0.027	1	0.38	0.38	-0.9	0.082	-0.042	-0.11	-0.093	-0.14	-0.32	-0.019	-0.11	-0.038
production	-0.29	0.38	1	0.99	-0.24	-0.012	0.11	-0.083	0.32	-0.31	-0.33	-0.26	-0.43	-0.31
da_production	-0.3	0.38	0.99	1	-0.24	-0.015	0.11	-0.08	0.32	-0.31	-0.34	-0.26	-0.42	-0.31
air_temperature	-0.074	-0.9	-0.24	-0.24	1	-0.025	0.081	0.097	0.2	0.022	0.2	-0.081	-0.05	-0.065
wind_speed	-0.23	0.082	-0.012	-0.015	-0.025	1	0.19	0.043	-0.076	-0.1	-0.14	-0.15	0.25	-0.2
precipitation_amount	-0.11	-0.042	0.11	0.11	0.081	0.19	1	-0.086	0.22	-0.048	-0.0066	-0.067	0.05	-0.093
reservoir_capacity	0.038	-0.11	-0.083	-0.08	0.097	0.043	-0.086	1	-0.068	0.066	0.062	0.019	-0.018	0.037
reservoir_levels	-0.16	-0.093	0.32	0.32	0.2	-0.076	0.22	-0.068	1	-0.25	-0.093	-0.22	-0.26	-0.16
oil_price	0.68	-0.14	-0.31	-0.31	0.022	-0.1	-0.048	0.066	-0.25	1	0.83	0.86	0.49	0.68
gas_price	0.76	-0.32	-0.33	-0.34	0.2	-0.14	-0.0066	0.062	-0.093	0.83	1	0.69	0.35	0.76
osebx_price	0.67	-0.019	-0.26	-0.26	-0.081	-0.15	-0.067	0.019	-0.22	0.86	0.69	1	0.47	0.67
import/export	0.24	-0.11	-0.43	-0.42	-0.05	0.25	0.05	-0.018	-0.26	0.49	0.35	0.47	1	0.28
target	0.95	-0.038	-0.31	-0.31	-0.065	-0.2	-0.093	0.037	-0.16	0.68	0.76	0.67	0.28	1

Figure 21: Correlation matrix Oslo (NO1).

# Testing for stationarity

Time Series	ADF Statistic	P-Value	Critical Value (1%)	Critical Value (5%)	Critical Value (10%)
Oslo	-4.019	0.001	-3.431	-2.862	-2.567
Kr.sand	-3.965	0.002	-3.431	-2.862	-2.567
Bergen	-3.967	0.002	-3.431	-2.862	-2.567
Molde	-7.567	< 0.001	-3.431	-2.862	-2.567
Tr.heim	-7.567	< 0.001	-3.431	-2.862	-2.567
Tromsø	-8.708	< 0.001	-3.431	-2.862	-2.567

Table 10: ADF Test Results for Target Time-series.

# Data transformations

Missing values

Resampling

Normalization

Train-test split

<b>Fold</b>	<b>Train Start</b>	<b>Train End</b>	<b>Val Start</b>	<b>Val End</b>
1	2020-01-01 00:00:00	2021-12-31 23:00:00	2022-01-01 00:00:00	2022-01-01 23:00:00
2	2020-01-01 00:00:00	2022-01-01 23:00:00	2022-01-02 00:00:00	2022-01-02 23:00:00
3	2020-01-01 00:00:00	2022-01-02 23:00:00	2022-01-03 00:00:00	2022-01-03 23:00:00
4	2020-01-01 00:00:00	2022-01-03 23:00:00	2022-01-04 00:00:00	2022-01-04 23:00:00
5	2020-01-01 00:00:00	2022-01-04 23:00:00	2022-01-05 00:00:00	2022-01-05 23:00:00
...	...	...	...	...
365	2020-01-01 00:00:00	2022-12-28 23:00:00	2022-12-29 00:00:00	2022-12-29 23:00:00

Table 11: Rolling Forecast Origin Cross-validation Scheme.

# Hyperparameter optimization

## 1. ARIMA models

- $(p,d,q) = (\text{AR},\text{I},\text{MA})$
- Grid search
- Alkaline Information Criterion (AIC)
- Bayesan Information Criterion (BIC)

## 2. XGBoost models

- Depth
- Loss function
- Regularization (shrinkage)

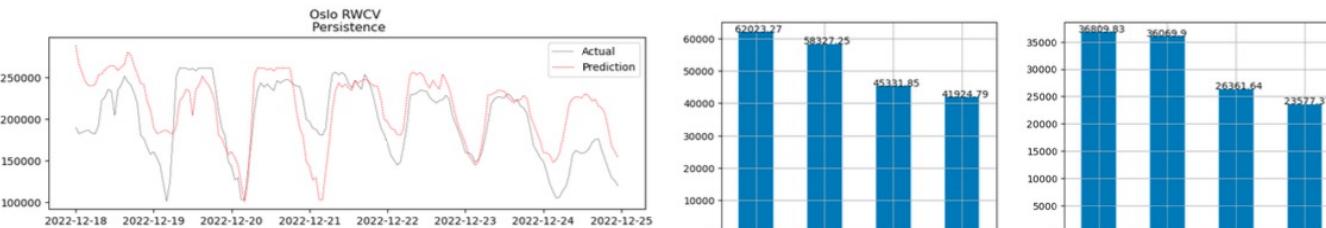
## 3. LSTM models

- Hidden size
- Hidden layers
- Sequence length
- Batch size
- Dropout (regularization)
- Activation function
- Loss function
- Learning rate
- Epochs

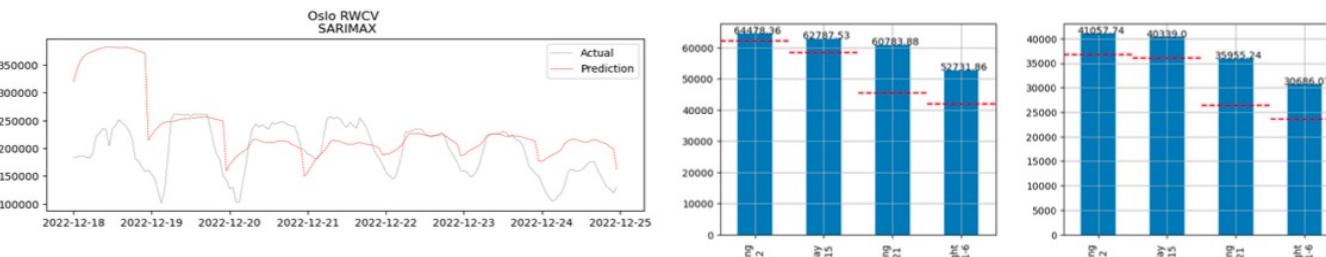


# Model evaluation

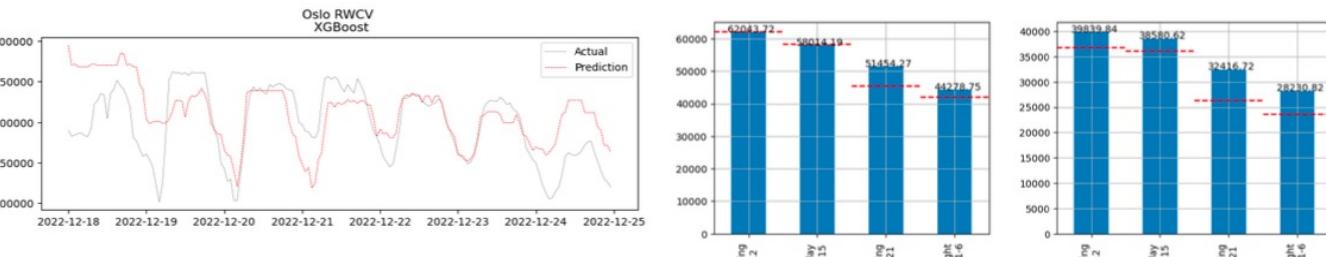
- Naïve baseline for comparisons against lower bound of performance
- Aggregated time-of-day scores (mornings 6-12, mid-days 12-15, evenings 15-21, nights 21-6)
- RMSE penalizes larger errors more than smaller ones (sensitive to outliers)
- MAE measures the absolute difference between predicted and actual price but weights the magnitude of errors equally
- Competing objectives between capturing the nuances of prices and generalizing trends and patterns



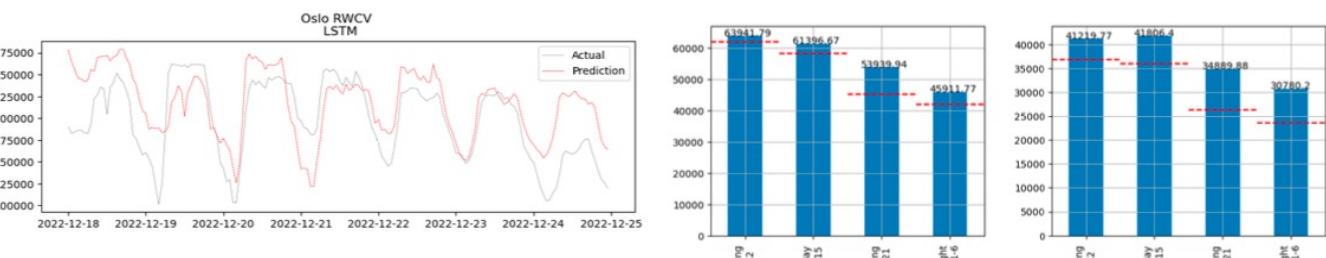
(a) 1-week of Rolling Forecast Origin Cross-validation.



(a) 1-week of Rolling Forecast Origin Cross-validation.



(a) 1-week of Rolling Forecast Origin Cross-validation.



(a) 1-week of Rolling Forecast Origin Cross-validation.

Oslo.

(b) RMSE.

(c) MAE.

# Results

- Univariate and multivariate (endogeneous and with exogeneous)
- All six bidding zones
- 365-fold rolling forecast cross validation (1 year)
- Out-of-sample evaluatiuon (3+months)
- 84 forecasts in total
- RMSE, MAE, MAPE and RSS
- XGBoost feature importance scores



Model performance

	RMSE		MAE		MAPE		RSS	
	endog	w/ exog	endog	w/ exog	endog	w/ exog	endog	w/ exog
Baseline (naive)	50595	/	<b>29143</b>	/	<b>81.82%</b>	/	<b>22.4e<sup>12</sup></b>	/
SARIMA	43970	42118	37346	35802	193%	177%	$17.0e^{17}$	$17.0e^{17}$
XGBoost	40366	<b>39476</b>	33055	33473	92.84%	135%	$16.6e^{17}$	$16.1e^{17}$
LSTM	40207	41640	33723	35795	126%	132%	$35.4e^{13}$	$34.2e^{13}$

Table 12: Results of 365-fold rolling forecast origin validation  
Oslo (NO1).

	RMSE		MAE		MAPE		RSS	
	endog	w/ exog	endog	w/ exog	endog	w/ exog	endog	w/ exog
Baseline (naive)	29469	/	19946	/	25.19%	/	$18.7e^{11}$	/
SARIMA	29469	44124	19946	36332	<b>25.18%</b>	36.84%	$18.7e^{11}$	$41.1e^{11}$
XGBoost	29156	27052	20268	<b>18838</b>	26.22%	26.92%	$17.9e^{11}$	<b>15.5e<sup>11</sup></b>
LSTM	29174	<b>21109</b>	21035	20134	29.21%	26.69%	$17.9e^{11}$	$17.9e^{11}$

Table 13: Results of Out-of-sample evaluation  
Oslo (NO1).

	RMSE		MAE		MAPE		RSS	
	endog	w/ exog	endog	w/ exog	endog	w/ exog	endog	w/ exog
Baseline (naive)	59768	/	35868	/	<b>85.10%</b>	/	<b>31.3e<sup>12</sup></b>	/
SARIMA	52832	50904	45122	43598	194%	180.82%	$22.4e^{17}$	$22.2e^{17}$
XGBoost	47145	45920	<b>20268</b>	39101	96.31%	153%	$21.5e^{17}$	$21.5e^{17}$
LSTM	<b>46129</b>	46220	39067	39516	131%	155%	$43.1e^{13}$	$42.9e^{13}$

Table 14: Results of 365-fold rolling forecast origin validation

Kristiansand (NO2).

	RMSE		MAE		MAPE		RSS	
	endog	w/ exog	endog	w/ exog	endog	w/ exog	endog	w/ exog
Baseline (naive)	29474	/	19943	/	25.19%	/	$18.7e^{11}$	/
SARIMA	29474	37216	19943	27932	25.18%	30.86%	$18.7e^{11}$	$29.2e^{11}$
XGBoost	29545	27259	20715	19266	26.77%	26.19%	$18.4e^{11}$	$15.7e^{11}$
LSTM	28354	<b>26431</b>	20317	<b>18173</b>	29.09%	<b>24.81%</b>	$16.9e^{11}$	<b><math>14.9e^{11}</math></b>

Table 15: Results of Out-of-sample evaluation

Kristiansand (NO2).

	RMSE		MAE		MAPE		RSS	
	endog	w/ exog	endog	w/ exog	endog	w/ exog	endog	w/ exog
Baseline (naive)	44054	/	<b>17969</b>	/	inf%	/	<b>17.0e<sup>12</sup></b>	/
SARIMA	<b>22587</b>	42118	18878	35802	inf%	inf%	<b>17.0e<sup>12</sup></b>	$17.0e^{17}$
XGBoost	23386	23339	20715	19455	inf%	inf%	$58.1e^{16}$	$62.8e^{16}$
LSTM	24271	26279	20174	21622	inf%	inf%	$21.1e^{12}$	$29.7e^{12}$

Table 16: Results of 365-fold rolling forecast origin validation

Molde (NO3).

	RMSE		MAE		MAPE		RSS	
	endog	w/ exog	endog	w/ exog	endog	w/ exog	endog	w/ exog
Baseline (naive)	30448	/	21069	/	37.58%	/	$20.0e^{11}$	/
SARIMA	30448	44907	21069	34139	37.57%	47.61%	$20.0e^{11}$	$42.6e^{11}$
XGBoost	28469	29069	19687	19666	35.79%	31.79%	$17.1e^{11}$	$17.8e^{11}$
LSTM	28438	<b>28381</b>	20462	<b>19228</b>	40.91%	<b>31.29%</b>	$17.1e^{11}$	<b><math>16.6e^{11}</math></b>

Table 17: Results of Out-of-sample evaluation

Molde (NO3).

	RMSE		MAE		MAPE		RSS	
	endog	w/ exog	endog	w/ exog	endog	w/ exog	endog	w/ exog
Baseline (naive)	33532	/	<b>9878</b>	/	inf%	/	$98.5e^{11}$	/
SARIMA	13169	12754	11019	10651	inf%	inf%	$19.1e^{16}$	/
XGBoost	<b>12333</b>	13179	19687	10946	inf%	inf%	$22.5e^{16}$	$23.9e^{16}$
LSTM	12580	15867	10231	13100	inf%	inf%	<b>82.8e<sup>11</sup></b>	$95.9e^{11}$

Table 18: Results of 365-fold rolling forecast origin validation

Tromsø (NO4).

	RMSE		MAE		MAPE		RSS	
	endog	w/ exog	endog	w/ exog	endog	w/ exog	endog	w/ exog
Baseline (naive)	21456	/	11705	/	25.28%	/	$99.4e^{10}$	/
SARIMA	21456	30875	11705	22584	25.27%	45.46%	$99.4e^{10}$	$18.7e^{16}$
XGBoost	20592	23149	11424	12507	25.43%	29.35%	$89.6e^{10}$	$11.3e^{11}$
LSTM	<b>19448</b>	21675	<b>10519</b>	13155	<b>22.76%</b>	28.05%	<b>79.9e<sup>10</sup></b>	$96.1e^{10}$

Table 19: Results of Out-of-sample evaluation

Tromsø (NO4).

	RMSE		MAE		MAPE		RSS	
	endog	w/ exog	endog	w/ exog	endog	w/ exog	endog	w/ exog
Baseline (naive)	49520	/	28290	/	<b>80.67%</b>	/	<b>21.4e<sup>12</sup></b>	/
SARIMA	42755	41411	36593	35473	191%	183.02%	$16.9e^{17}$	$16.9e^{17}$
XGBoost	39208	39165	<b>11424</b>	33479	86.50%	154.40%	$16.5e^{17}$	$16.3e^{17}$
LSTM	<b>38759</b>	38818	32781	33351	126.24%	152.32%	$35.3e^{13}$	$36.3e^{13}$

Table 20: Results of 365-fold rolling forecast origin validation

Bergen (NO5).

	RMSE		MAE		MAPE		RSS	
	endog	w/ exog	endog	w/ exog	endog	w/ exog	endog	w/ exog
Baseline (naive)	25240	/	<b>16953</b>	/	<b>15.75%</b>	/	<b>13.7e<sup>10</sup></b>	/
SARIMA	25240	27679	<b>16953</b>	19177	<b>15.75%</b>	17.28%	<b>13.7e<sup>10</sup></b>	$16.1e^{11}$
XGBoost	24950	<b>24156</b>	17137	17018	16.27%	15.94%	$13.1e^{11}$	$12.3e^{11}$
LSTM	25427	24584	18391	18189	17.80%	17.49%	$13.6e^{11}$	$12.9e^{11}$

Table 21: Results of Out-of-sample evaluation

Bergen (NO5).

	RMSE		MAE		MAPE		RSS	
	endog	w/ exog	endog	w/ exog	endog	w/ exog	endog	w/ exog
Baseline (naive)	44054	/	17969	/	inf%	/	<b>17.0e<sup>12</sup></b>	/
SARIMA	22587	<b>22154</b>	18878	18547	inf%	inf%	$60.0e^{16}$	$61.2e^{16}$
XGBoost	23386	22915	<b>17137</b>	18979	inf%	inf%	$58.1e^{16}$	$61.6e^{16}$
LSTM	24050	25940	19957	21375	inf%	inf%	$21.0e^{12}$	$32.9e^{12}$

Table 22: Results of 365-fold rolling forecast origin validation

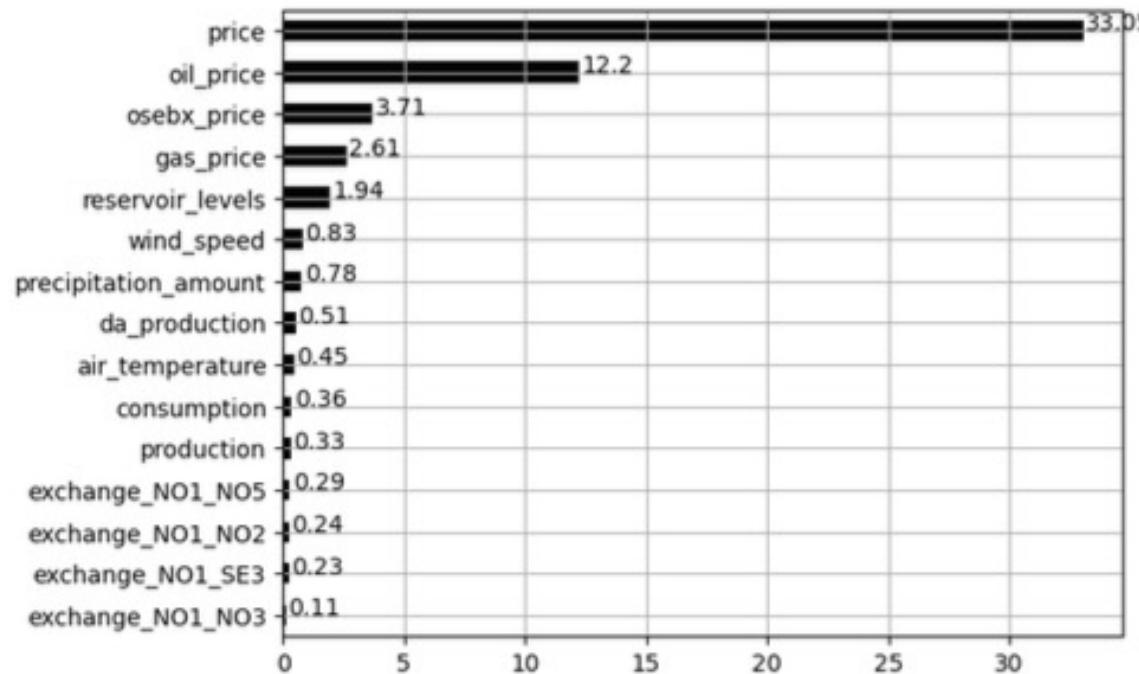
Trondheim (NO6).

	RMSE		MAE		MAPE		RSS	
	endog	w/ exog	endog	w/ exog	endog	w/ exog	endog	w/ exog
Baseline (naive)	30448	/	21069	/	37.58%	/	$20.0e^{11}$	/
SARIMA	30448	45333	21069	34465	37.57%	48.04%	$20.0e^{11}$	$43.4e^{11}$ /
XGBoost	28469	<b>28326</b>	19687	<b>19532</b>	35.79%	<b>31.70%</b>	$17.1e^{11}$	<b>16.9e<sup>11</sup></b>
LSTM	28438	30100	20462	22870	40.91%	48.58%	$17.1e^{11}$	$19.1e^{11}$

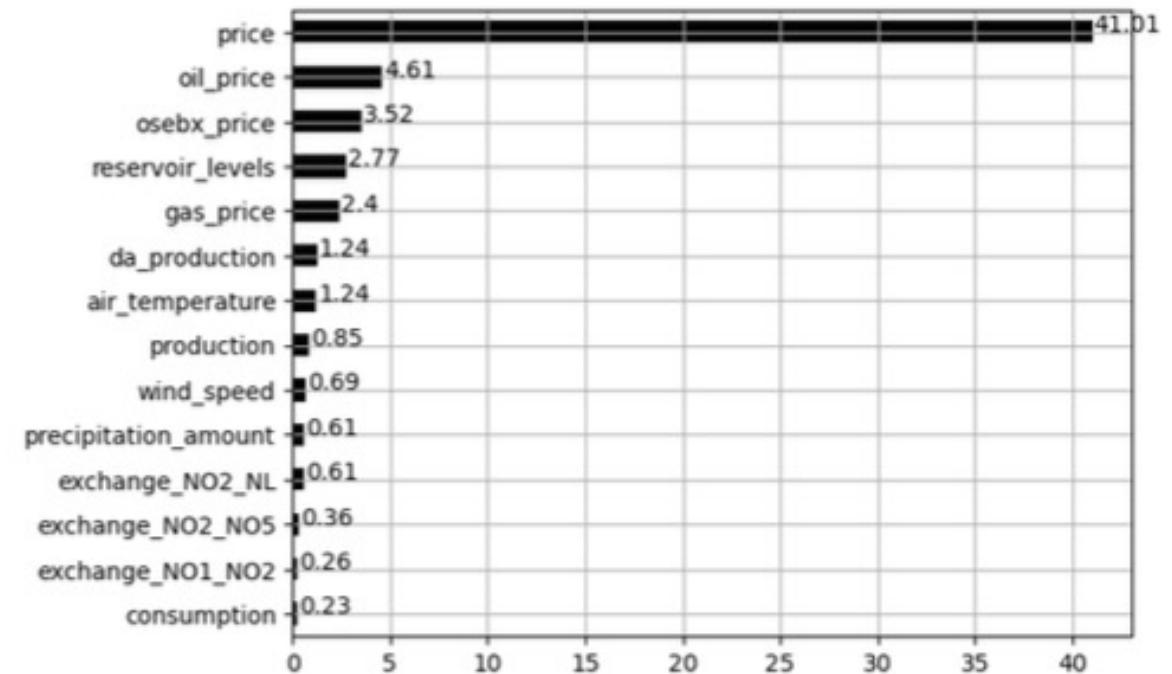
Table 23: Results of Out-of-sample evaluation

Trondheim (NO6).

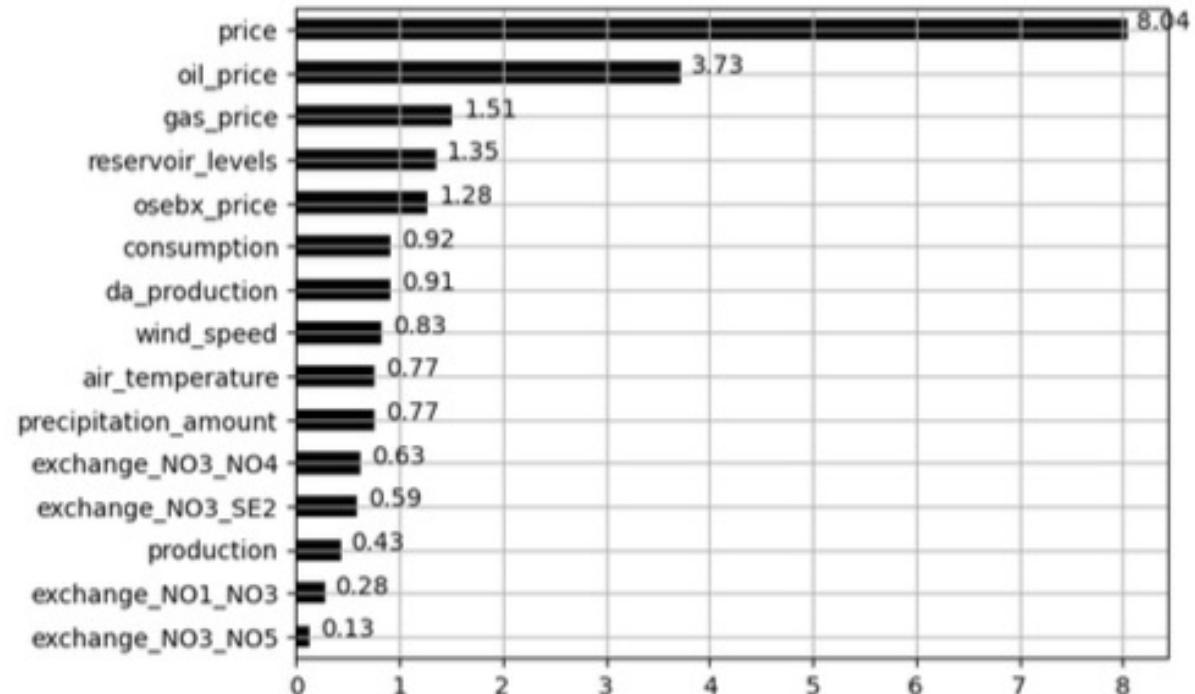
# Feature importance



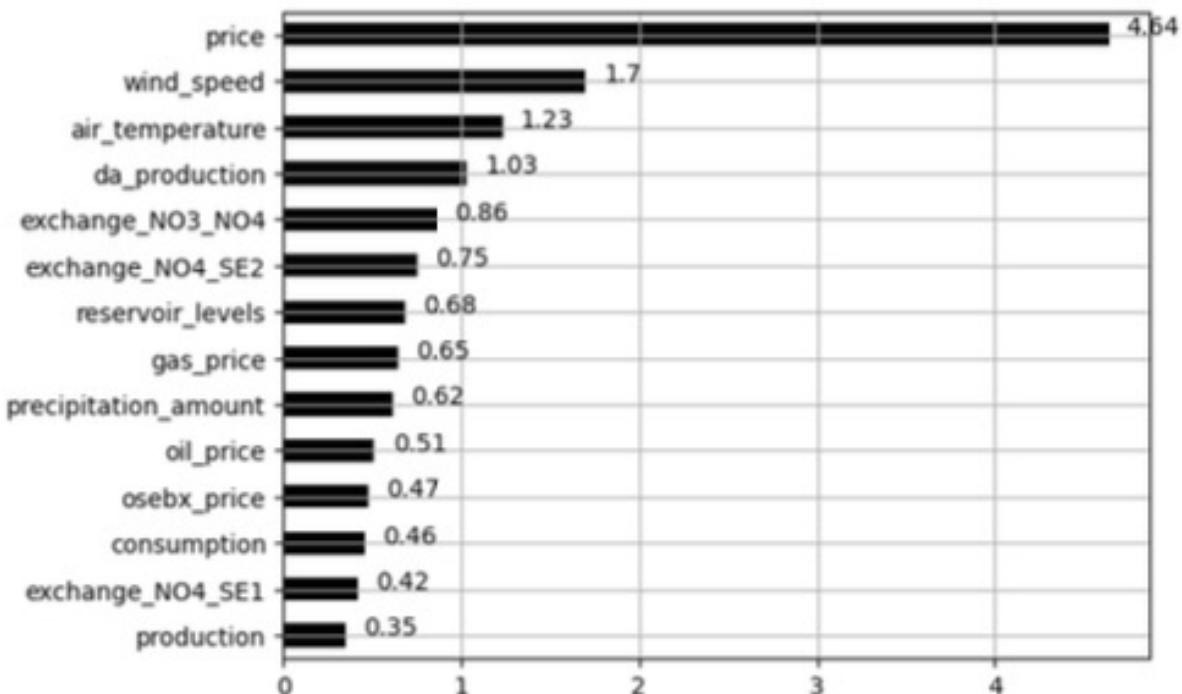
(a) Oslo (NO1).



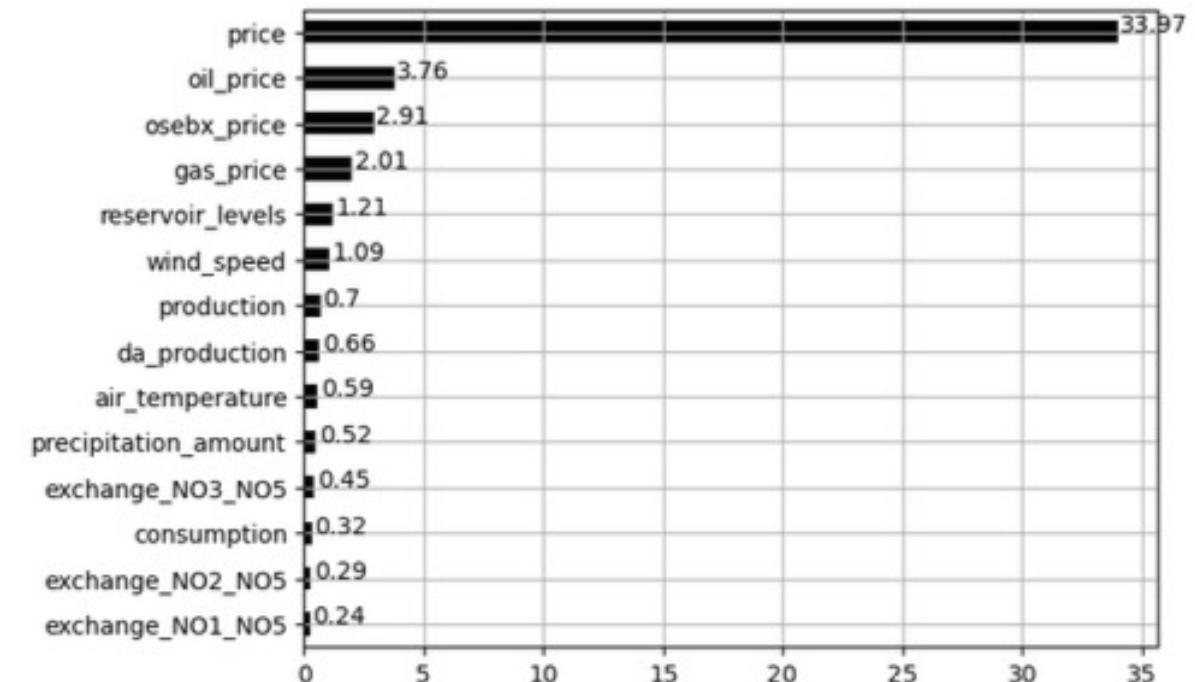
(b) Kristiansand (NO2).



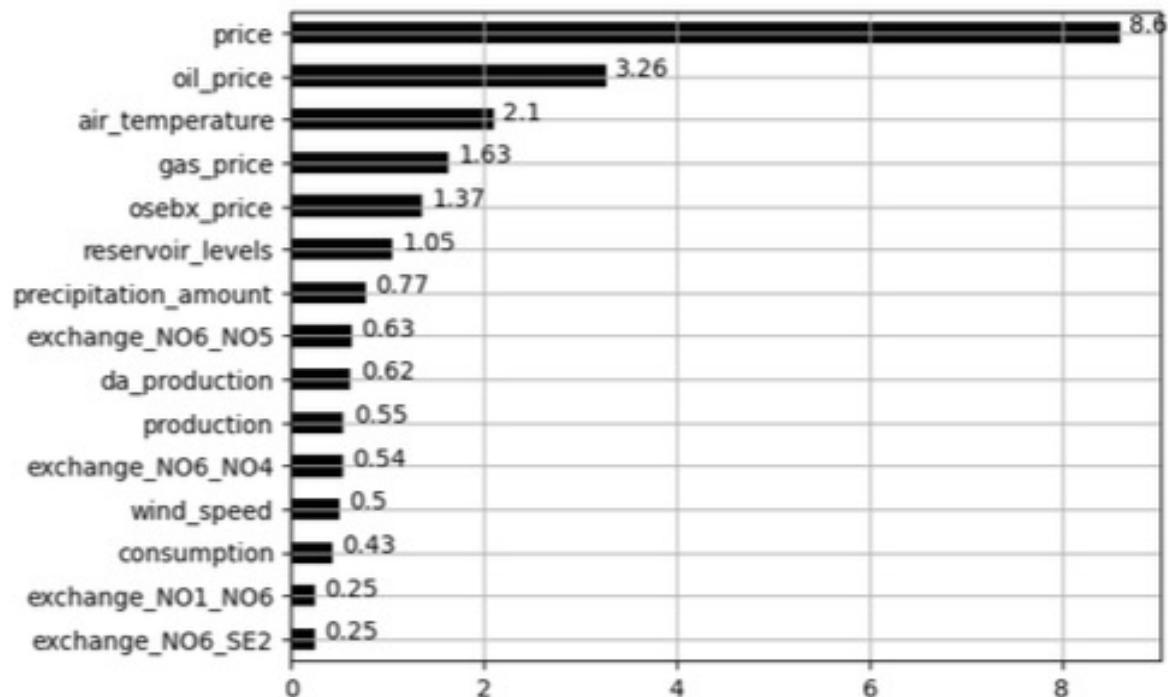
(c) Molde (NO3).



(d) Tromsø (NO4).



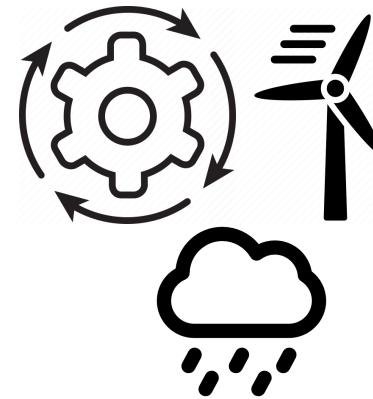
(e) Bergen (NO5).



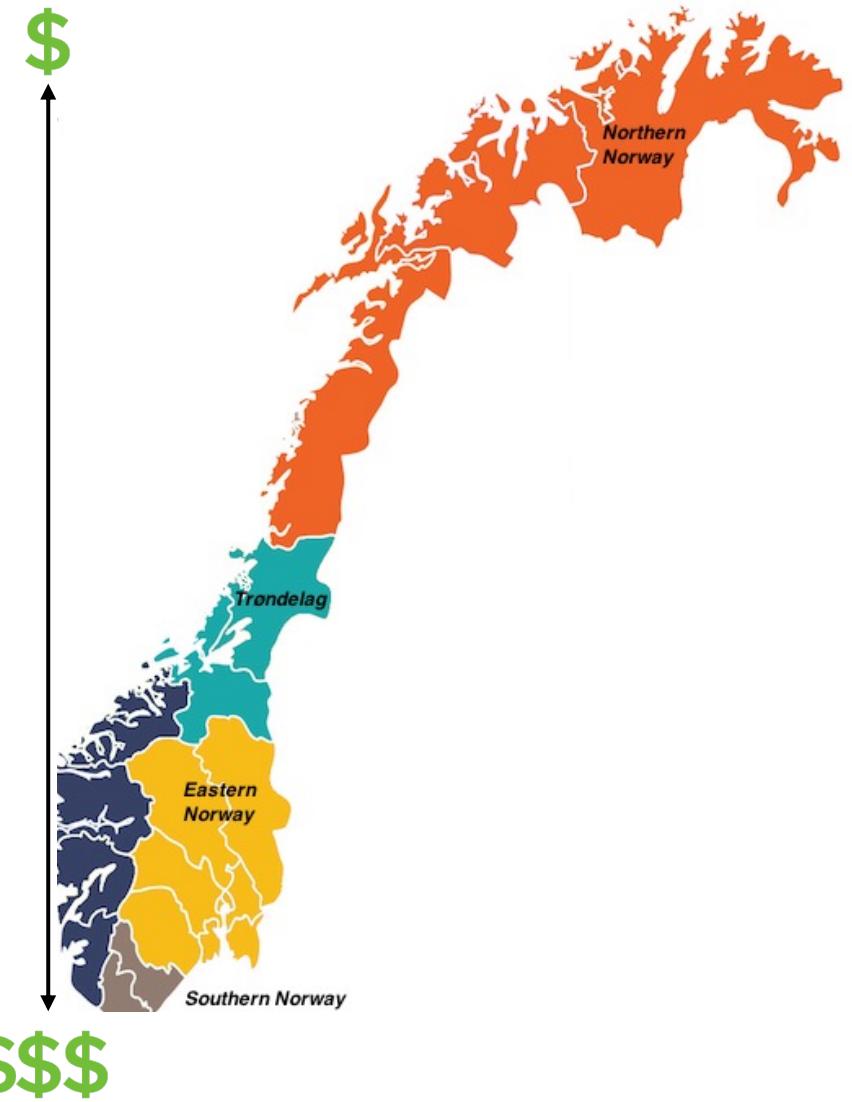
(f) Trondheim (NO2).

# Discussion on price drivers

- Correlation, PCA and XGBoost scores
- Varying across bidding-zones
- Convenience yields as opposed to marginal cost of production
- Disruption of global energy after Ukraine



Period: 01.01.2020 – 31.03.2023

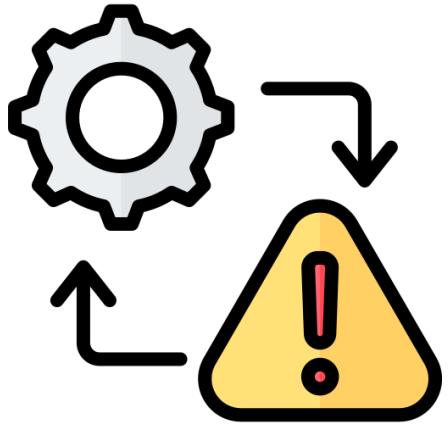
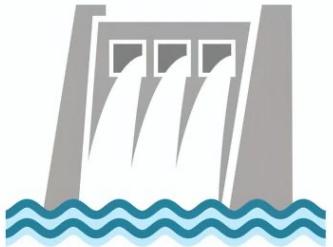


# Discussion on methods

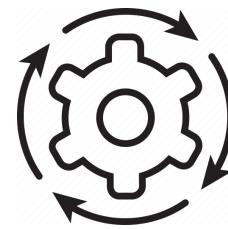
- ARIMA performs well on validation-set with short inference horizons (but fails during further out-of-sample evaluation)
- LSTM and XGBoost manages to strike a balance in the bias-variance trade-off during out-of-sample evaluation
- XGBoost has the benefit of being interpretable
- LSTM performs better overall
- No one-size-fits-all model
- No one-size-fits-all metric



# Implications



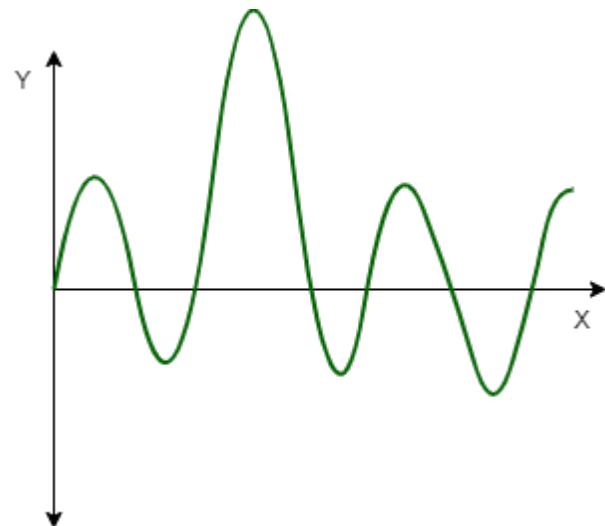
# Conclusion



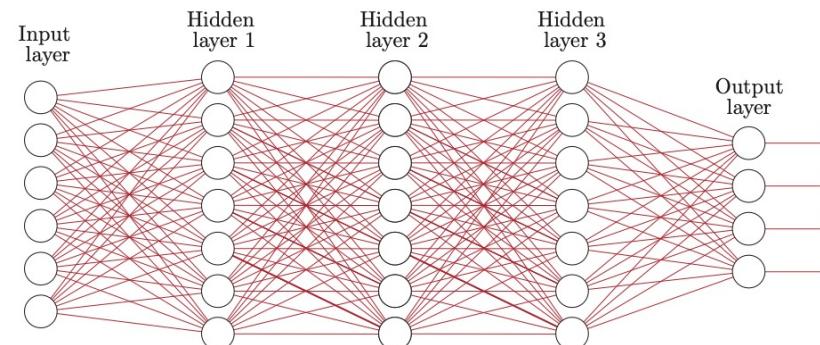
Which methods are most effective in predicting the Norwegian day-ahead elspot prices?

Which price-drivers shape the behaviour of the Norwegian elspot prices?

**ARIMA**



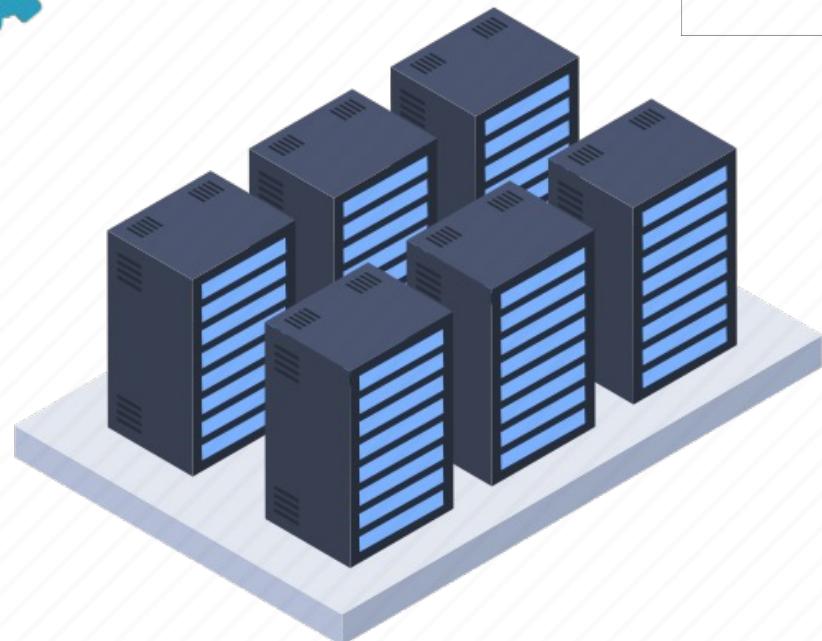
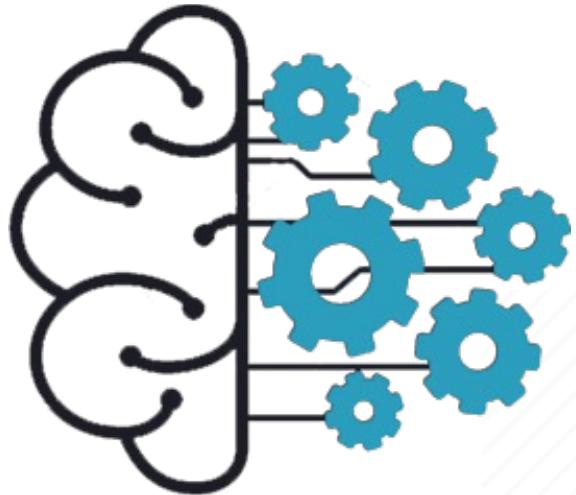
**LSTM**



**XGBoost**



# Limitations and Future Work



# Thank you!

Special thanks to supervisor Huamin Ren for guidance, and all of my professors and classmates in KUC, Oslo and UPC, Barcelona!

