TMR 4585 Specialization Course UWT Introduction to Subsea Pipeline Technology Heat transfer and thermal insulation by Prof. Svein Sævik, Trondheim, 2019

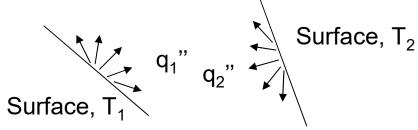
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- The heat transferr coefficient
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- Simplified shut-down simulation

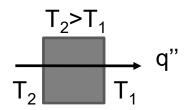
The heat transferr coefficient

- Heat is transmitted in three ways:
 - > By radiation
 - > Conduction
 - > Surface convection:
 - ✓ at the inner pipe wall (wellstream)
 - ✓ At the outer pipe surface

a) radiation:



b) conduction:



c) convention:

Moving fluid, T
$$\xrightarrow{\qquad \qquad } q'' \qquad T < T_s$$

$$\xrightarrow{\qquad \qquad } \int T_s$$

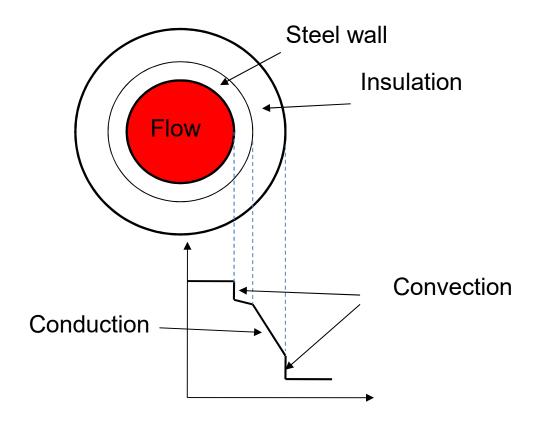
Steady state heat transferr in pipelines

 Radiation can be neglected here because temperatures are below 200 deg.

Conduction

- Surface convection:
 - > at the inner pipe wall (well-stream)
 - > At the outer pipe surface

Steady state heat transferr in pipelines



The heat transferr coefficient

Multilayered conduction of a pipe cross-section:

$$Q_r = -2\pi r k \frac{dT}{dr} \qquad Q_r = u 2\pi r_i (T_1 - T_n)$$

Referring to inner radius:

$$u_i = \frac{1}{r_i \sum \frac{\ln(\frac{r_{j+1}}{r_j})}{k_i}}$$

- ➤ k=thermal conductivity (W/mK, note: W=J/s)
- $ightharpoonup r_j$ =inner radius of layer j

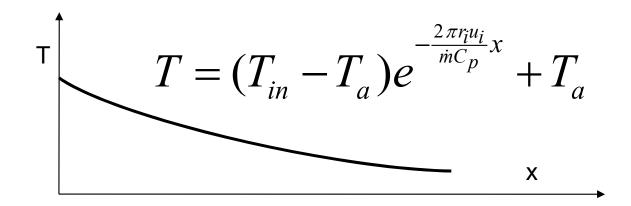
The heat transferr coefficient

 For insulated flowlines the heat transferr is governed by the insulation and the soil cover

$$u_i = \frac{1}{r_i \left(\frac{1}{k_{soil}} \cosh^{-1} \frac{z}{r_o} + \sum \frac{\ln(\frac{r_{j+1}}{r_j})}{k_j} \right)}$$

$$h_{soil} = \frac{k_{soil}}{r_o \cosh^{-1}(\frac{z}{r_o})} \qquad D=2r_o$$

Steady state temperature profile



- $ightharpoonup T_{in}$ = Inlet temperature
- \succ T_a = Ambient temperature (°C)
- $\rightarrow \dot{m} = \text{mass flux (kg/s)}$
- $ightharpoonup C_p = Specific heat capacity (J/(kgK))$
- \rightarrow x = distance from inlet (m)

Time from shut-down to critical hydrate temperature is reached

"The lumped capacity model":

- Only valid if the temperature gradient is governed by a thin insulation layer
- For thick layer insulation (e.g. buried pipes) more advanced mehtods such as finite differences need to be used

