

Multi-Agent Reinforcement Learning

Multi-Agent Deep Reinforcement Learning – Part 2

Stefano V. Albrecht, Filippos Christianos, Lukas Schäfer

This lecture is based on

Multi-Agent Reinforcement Learning: Foundations and Modern Approaches

by Stefano V. Albrecht, Filippos Christianos and
Lukas Schäfer

MIT Press, 2024

Download book, slides, and code at:

www.marl-book.com



- Agent modeling with deep learning
- Parameter and experience sharing
- Policy self-play in zero-sum games
- Population-based training

Agent Modeling with Deep Learning

Agents Modeling – Motivation

In MARL, agents need to consider the policies of other agents to coordinate their actions.

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- Distribution of training data is dependent on the policies of all agents
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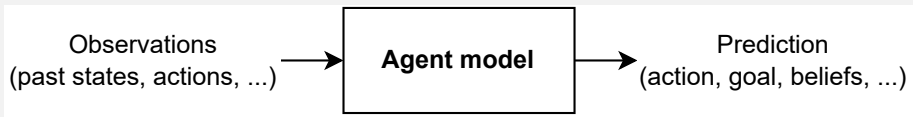
- Distribution of training data is dependent on the policies of all agents
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Can we provide agents with more **explicit** information about the policies of other agents so they can learn to coordinate better, e.g. by learning best-response policies?

Reminder

In Chapter 6, we have seen approaches that model other agents' policies:

- Learn models of other agents to predict their actions
- Compute optimal action (best-response) against agent models



S. Albrecht, P. Stone. **Autonomous Agents Modelling Other Agents: A Comprehensive Survey and Open Problems.** *Artificial Intelligence*, 2018

Recap: Tabular Agent Modeling

In Chapter 6, we modeled other agents' policies as stationary distributions by maintaining tables of action frequencies for each state

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Similar to tabular value functions, **tabular agent models** are limited due to their inability to generalise across states.

Solution

Use **deep learning** to learn generalisable agent models!

Recap: Joint-Action Learning with Agent Models

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We have already seen **joint-action learning with agent models** (JAL-AM)

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- Using the value function and agent models, agent i can compute its expected action values under the current models of other agents:

$$AV_i(s, a_i) = \sum_{a_{-i} \in A_{-i}} Q_i(s, \langle a_i, a_{-i} \rangle) \prod_{j \in I \setminus \{i\}} \hat{\pi}_j(a_j | s)$$

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- Use AV_i to select optimal actions and as learning update targets

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- Given the observation history of agent i , its model $\hat{\pi}_j^i(a_j | h_i; \phi_j^i)$ for agent j outputs a probability distribution over actions

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- Agent i can train its model for agent j by minimizing the cross-entropy loss between the predicted policy $\hat{\pi}_j^i$ and the observed actions of agent j :

$$\mathcal{L}(\phi_j^i) = \mathbb{E}_{a_j^t \sim \pi_j(h_j^t)} \left[-\log \hat{\pi}_j^i(a_j^t | h_i^t; \phi_j^i) \right]$$

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- Then, agent i can compute expected action values:

$$AV(h_i, a_i; \theta_i) = \sum_{a_{-i} \in A_{-i}} Q(h_i, \langle a_i, a_{-i} \rangle; \theta_i) \prod_{j \neq i} \hat{\pi}_j^i(a_j | h_i; \phi_j^i)$$

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Approximate AV with only K joint actions sampled from the agent models:

$$AV(h_i, a_i; \theta_i) = \frac{1}{K} \sum_{k=1}^K Q(h_i, \langle a_i, a_{-i}^k \rangle; \theta_i) \Big|_{a_j^k \sim \hat{\pi}_j^i(\cdot | h_i)}$$

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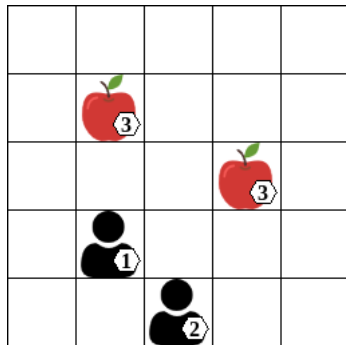
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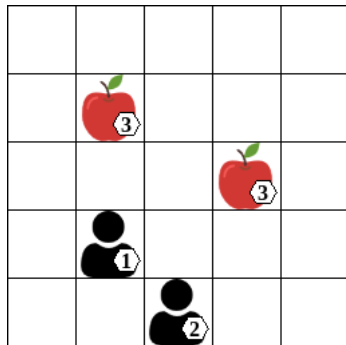
To optimise the centralized joint-action-value function of agent i , we then minimize the following loss over batches of experiences sampled from a replay buffer:

Joint-Action Learning with Deep Agent Models in LBF

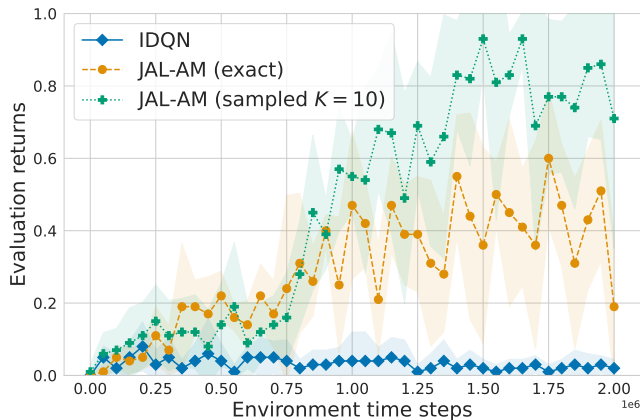


(a) Environment

Joint-Action Learning with Deep Agent Models in LBF



(a) Environment



(b) Learning curve

Learning Compact Representations of Agent Policies

- JAL-AM combines agent models and centralized value functions to compute best-response policies.
- Can we integrate agent models into multi-agent policy gradient algorithms, e.g. by conditioning policies on agent models?

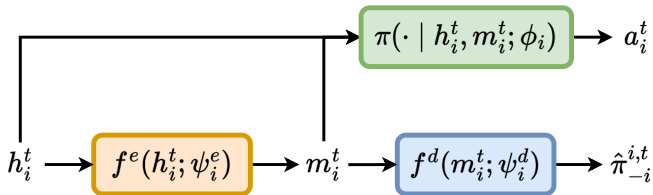
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To condition policies (and value functions) of agents on the policies of other agents, we need **compact** representations of the policies of other agents. How can we learn such representations?

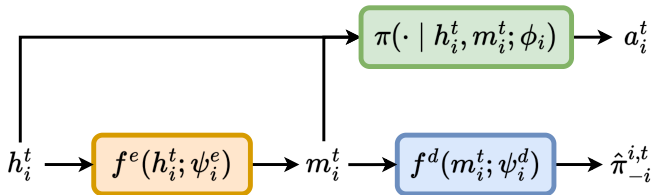
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Agent i trains encoder-decoder architecture with

- **Encoder f^e** with parameters ψ_i^e : given observation history h_i^t of agent i , output compact representation m_i^t of the policies of other agents
- **Decoder f^d** with parameters ψ_i^d : given compact representation m_i^t , predict the policies $\hat{\pi}_{-i}^{i,t}$ of other agents

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Then, agent i can condition its policy on the compact representations m_i^t .

Learning Compact Representations of Agent Policies

The encoder and decoder are jointly trained to minimize the cross-entropy loss for the predicted action probabilities and true actions of all other agents:

$$\mathcal{L}(\psi_i^e, \psi_i^d) = \sum_{j \neq i} -\log \hat{\pi}_j^{i,t}(a_j^t) \quad \text{with} \quad \hat{\pi}_j^{i,t} = f^d \left(f^e(h_i^t; \psi_i^e); \psi_i^d \right)_j$$

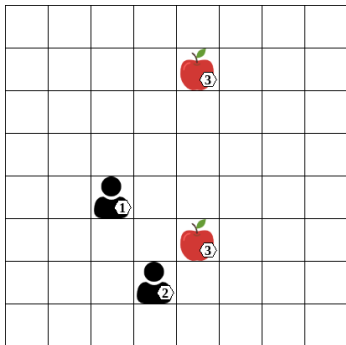
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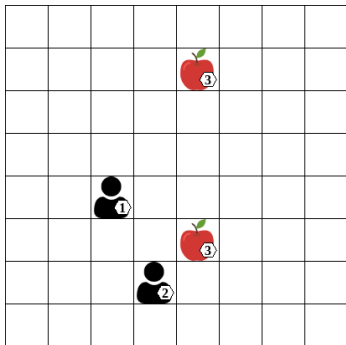
Encoder-decoder agent models can be integrated into MARL algorithm by conditioning value functions and policies on the obtained policy representations.

Compact Agent Policy Representations in LBF

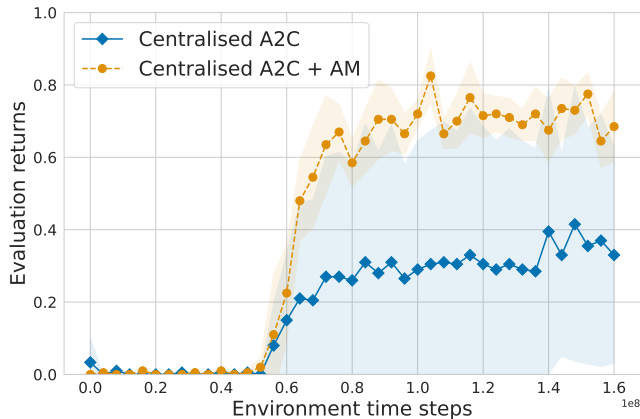


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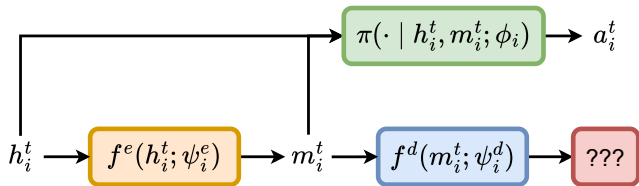


(a) Environment



(b) Learning curve

Reconstruction Targets to Learn Compact Representations



Note

We used the ground truth actions as information to encode by using them as targets for the decoder. We could also use

- Observations – try to capture information that other agents have access to
- Rewards – try to predict the objectives that other agents optimise for
- ...

Parameter and Experience Sharing

Parameter and Experience Sharing – Motivation

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Solution

Two approaches to improve the efficiency of training many agents:

- **Parameter sharing:** agents share their network parameters with each other
- **Experience sharing:** agents share experiences with each other

Environments with Homogeneous Agents

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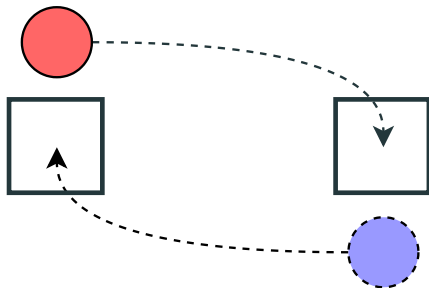
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- **Weakly homogeneous agents**: Agents can be permuted and their expected returns remain the same under the permutation $\sigma : I \mapsto I$:

$$U_i(\pi) = U_{\sigma(i)}(\langle \pi_{\sigma(1)}, \pi_{\sigma(2)}, \dots, \pi_{\sigma(n)} \rangle), \quad \forall i \in I$$

Environments with Homogeneous Agents – Examples

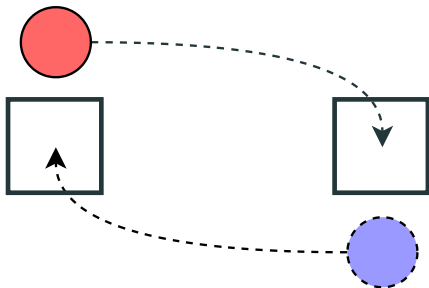
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Agents need to learn similar policies.

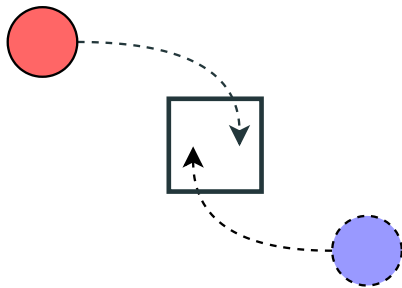
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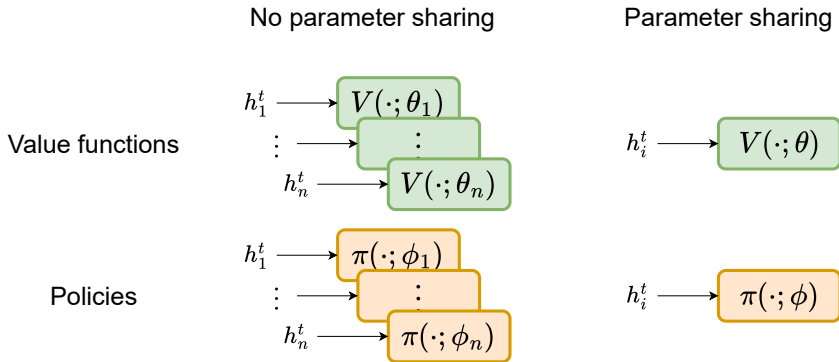
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Parameter Sharing

Sharing network parameters across agents is common practice to make MARL training more efficient. Share parameters across value functions, policies, or both.



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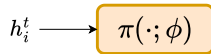
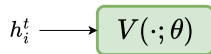
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Parameter sharing has two primary benefits:

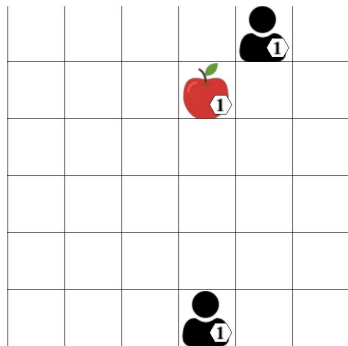
- **Scalability:** the number of parameters remains constant independent of the number of agents \rightarrow less computational cost
- **Efficiency:** shared parameters are updated using the experiences of all agents \rightarrow more training data for the shared parameters

The downside is that (naive) parameter sharing assumes strongly homogeneous agents.

Parameter sharing

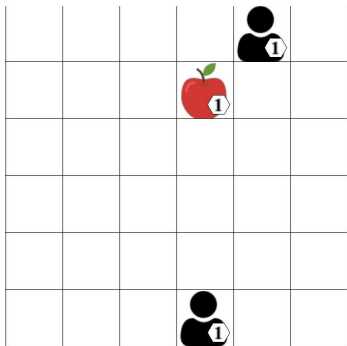


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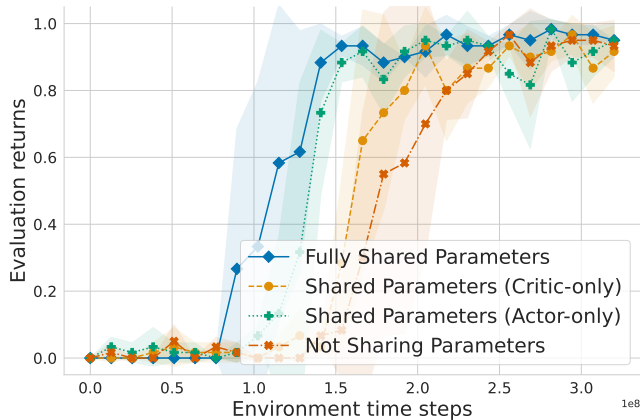


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Note

The experiences of agent j is **off-policy** data for agent $i \rightarrow$ experience sharing needs to use off-policy MARL algorithms or correct for the differences in data distributions.

Deep Q-Networks with Shared Experience Replay

We can extend IDQN with experience sharing by following the steps below:

- Collect the experience of all agents in a shared replay buffer $\mathcal{D}_{\text{shared}}$
- Each agent samples from $\mathcal{D}_{\text{shared}}$ to update its value function
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DQN is an off-policy algorithm so it is theoretically sound to use the experience of other agents that have different policies.

Shared Experience Actor-Critic (SEAC)

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SEAC policy loss (based on IA2C) with importance sampling (IS) weight correction:

policy loss on own data



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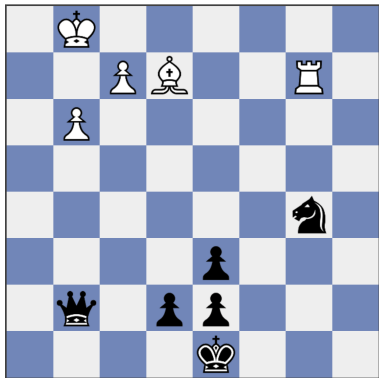
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Hyperparameter λ determines weighting for the loss over the experience of other agents. The same IS weight correction can be applied to the critic loss.

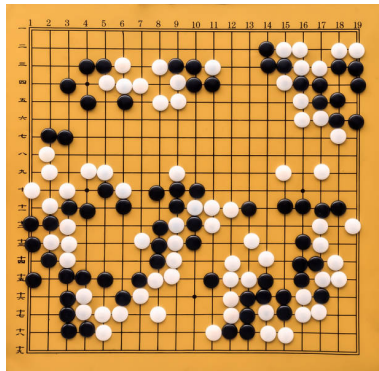
Policy Self-Play in Zero-Sum Games

The Challenge of Zero-Sum Board Games

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(a) Chess



(b) Go

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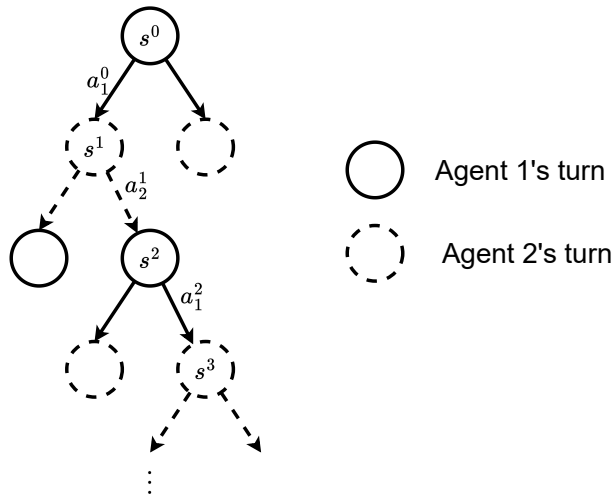
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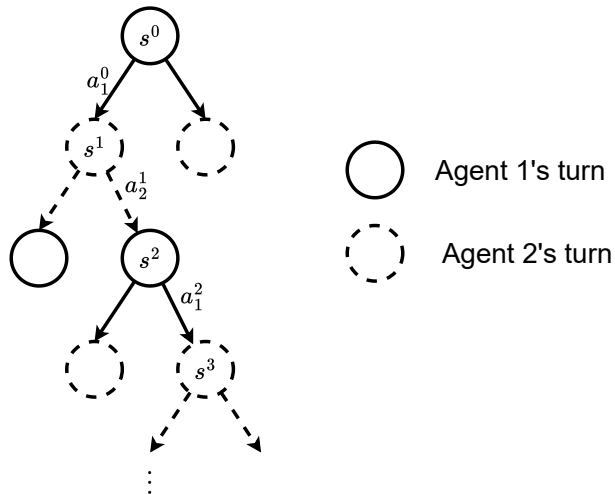
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Fortunately, we can exploit the structure of these games to develop effective algorithms.

Tree Search for Zero-Sum Games



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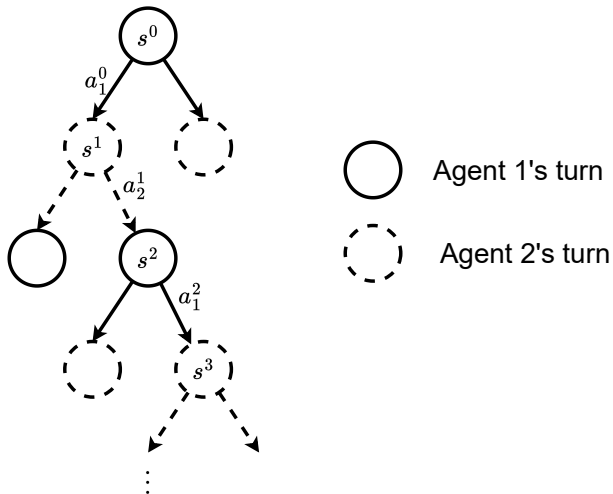


We can view turn-based zero-sum games as trees where

- *nodes* represent game states
- *edges* represent actions
- *leaves* represent terminal states

in each node either agent 1 or agent 2 makes a move.

Tree Search for Zero-Sum Games



Problem

The tree can grow very large depending on its

- **Depth:** number of time steps until terminal states
- **Breadth:** number of actions available in each state

→ makes search computationally expensive

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- **Backpropagation:** update the estimated values of the nodes visited during the selection step

Monte Carlo Tree Search – Simulation

MCTS maintains two statistics for each visited state-action pair:

- Value estimates $Q(s, a)$
- Visitation counts $N(s, a)$

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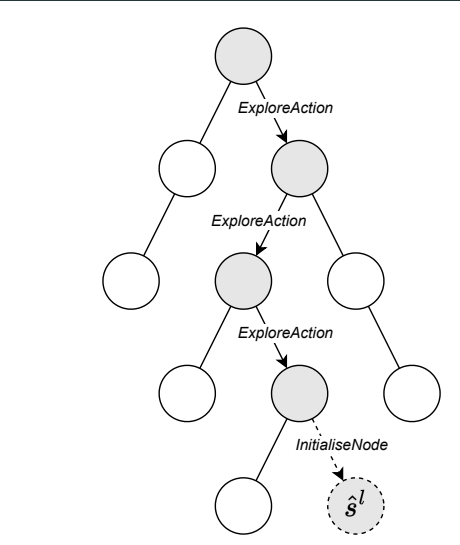
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To sample actions, MCTS commonly uses ϵ -greedy policies with respect to action-value function Q , or the upper confidence bound (UCB) policy:

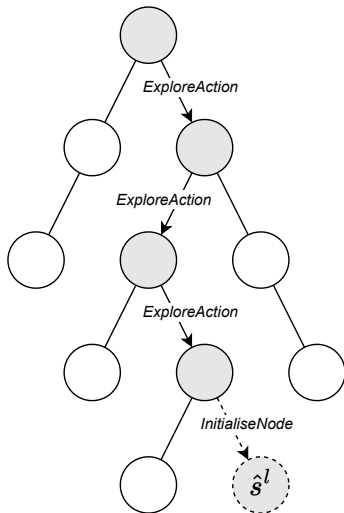
$$\hat{a}^\tau = \begin{cases} \hat{a} & \text{if } N(\hat{s}^\tau, \hat{a}) = 0 \\ \arg \max_{\hat{a} \in A} \left(Q(\hat{s}^\tau, \hat{a}) + \sqrt{\frac{2 \ln N(\hat{s}^\tau)}{N(\hat{s}^\tau, \hat{a})}} \right) & \text{otherwise} \end{cases}$$

Monte Carlo Tree Search – Expansion



If leaf node is reached \rightarrow **expand** the search tree by adding a new node for the reached state \hat{s}^l

Monte Carlo Tree Search – Expansion

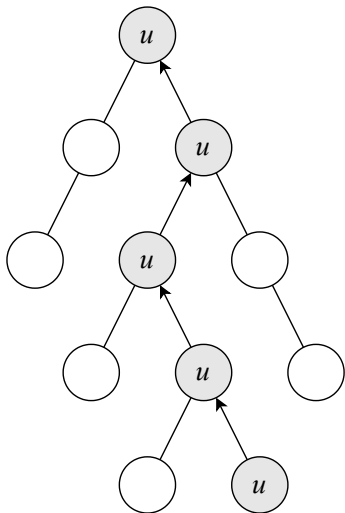


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The new node is initialized with

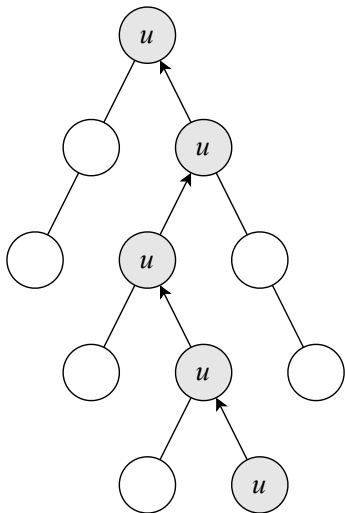
- $N(\hat{s}^l, \hat{a}) = 0$ for all actions \hat{a}
- An initial value estimate $Q(\hat{s}^l, \hat{a})$ for all actions \hat{a} , e.g. from a learned value function, heuristic, or random samples of outcomes.

Monte Carlo Tree Search – Backpropagation



Once a value estimate u for the leaf node is obtained → **backpropagate** rewards and value estimates starting from the leaf node up to the root node.

Monte Carlo Tree Search – Backpropagation

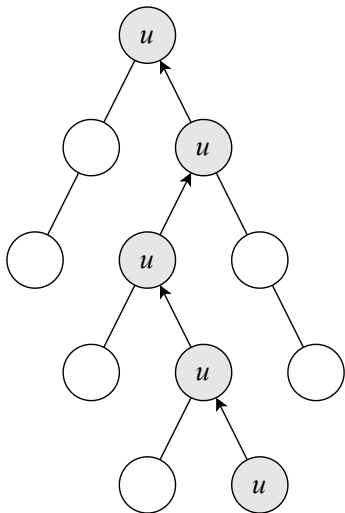


Once a value estimate u for the leaf node is obtained \rightarrow **backpropagate** rewards and value estimates starting from the leaf node up to the root node.

For each visited state-action pair $(\hat{s}^\tau, \hat{a}^\tau)$, we increment the visitation count and update the value:

$$Q(\hat{s}^\tau, \hat{a}^\tau) \leftarrow Q(\hat{s}^\tau, \hat{a}^\tau) + \frac{1}{N(\hat{s}^\tau, \hat{a}^\tau)} [u - Q(\hat{s}^\tau, \hat{a}^\tau)]$$

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(Any RL TD update rule can be used to update the value estimates.)

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Simulation, expansion, and backpropagation steps are repeated at every time step to iteratively grow the search tree and obtain better value estimates.

Monte Carlo Tree Search – Action Selection

Simulation, expansion, and backpropagation steps are repeated at every time step to iteratively grow the search tree and obtain better value estimates.

Following k simulations from the current state s^t , the best action is selected. This process can be done by choosing the action with:

- highest value estimate: $BestAction(s^t) = \arg \max_{\hat{a} \in A} Q(s^t, \hat{a})$
- highest visitation count: $BestAction(s^t) = \arg \max_{\hat{a} \in A} N(s^t, \hat{a})$

Monte Carlo Tree Search – Pseudocode

Algorithm Monte Carlo tree search (MCTS) for MDPs

```
1: Repeat for every episode:
2:   for  $t = 0, 1, 2, 3, \dots$  do
3:     Observe current state  $s^t$ 
4:     for  $k$  simulations do
5:        $\tau \leftarrow t$ 
6:        $\hat{s}^\tau \leftarrow s^t$  ▷ Perform simulation
7:       while  $\hat{s}^\tau$  is non-terminal and  $\hat{s}^\tau$ -node exists in tree do
8:          $\hat{a}^\tau \leftarrow \text{ExploreAction}(\hat{s}^\tau)$ 
9:          $\hat{s}^{\tau+1} \sim \mathcal{T}(\cdot \mid \hat{s}^\tau, \hat{a}^\tau)$ 
10:         $\hat{r}^\tau \leftarrow \mathcal{R}(\hat{s}^\tau, \hat{a}^\tau, \hat{s}^{\tau+1})$ 
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12:        if  $\hat{s}^\tau$ -node does not exist in tree then
13:           $\text{InitializeNode}(\hat{s}^\tau)$  ▷ Expand tree
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15:           $\tau \leftarrow \tau - 1$ 
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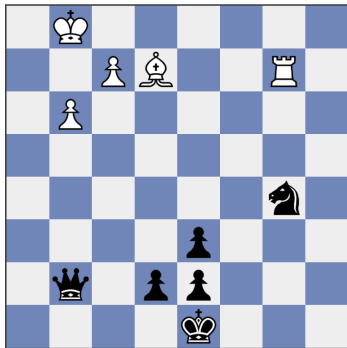
Can learn estimates of these functions from data to simulate possible outcomes of the game.

Self-Play Monte Carlo Tree Search

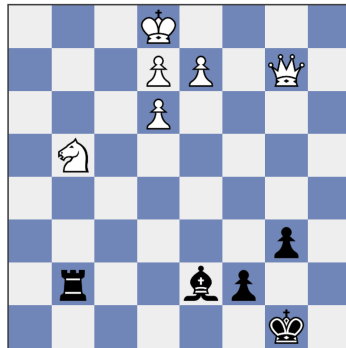
In zero-sum games with symmetrical roles and egocentric observations, agents can use the same policy to control both players

Self-Play Monte Carlo Tree Search

In zero-sum games with symmetrical roles and egocentric observations, agents can use the same policy to control both players → learn a policy in **self-play**



(a) Agent 1 perspective



(b) Agent 2 perspective

AlphaZero – Self-Play MCTS with Deep Learning

AlphaZero: combine self-play MCTS with deep learning to learn value estimates and policies → reached superhuman performance in Go, chess, and shogi!



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Learn functions with parameters θ conditioned on state s :

- Value estimate $V(s; \theta)$
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For each episode, a triplet (s, π, z) of data is stored where

- s are the states
- π are policy distributions computed by *BestAction*
- z is the game outcome (+1 for win, -1 for loss, 0 for draw)



AlphaZero – Self-Play MCTS with Deep Learning

The network is randomly initialized and trained using sampled batches of data to minimise the following combined loss:

$$\begin{aligned}\mathcal{L}(\theta) &= \mathcal{L}_{\text{value}} + \mathcal{L}_{\text{policy}} + c \|\theta\|^2 \\ \mathcal{L}_{\text{value}} &= \mathbb{E}_{(s, \pi, z) \sim \mathcal{D}} \left[(V(s; \theta) - u)^2 \right] \\ \mathcal{L}_{\text{policy}} &= \mathbb{E}_{(s, \pi, z) \sim \mathcal{D}} \left[\pi^\top \log \pi(\cdot \mid s; \theta) \right]\end{aligned}$$

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For exploration, AlphaZero combines a UCB policy with the learned policy:

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with the additional exploration rate $C(\hat{s}^\tau)$.

Population-Based Training

Population-Based Training – Self-Play for General-Sum Games

Problem

With MCTS, we focused on policy self-play in **two-agent zero-sum** games. Can we extend the idea of self-play to **general-sum** games with **more than two agents**?

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Population-based training is a generalisation of self-play to general-sum games:

- Maintain a **population of policies** representing possible strategies of the agent
- Evolve populations so they become more effective against the populations of other agents
- We denote the population of policies for agent i at generation k as Π_i^k .

Population-Based Training – Overview

First, initialize a population of policies for each agent (e.g. random policies).

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1. Initialize populations of random policies for each agent
2. Construct a **meta-game** M^k at generation k from the populations of all agents as a (non-repeated) normal-form game with
 - Actions: policies of agent populations, i.e.
 $A_i = \Pi_i^k$
 - Rewards: returns of joint policies $\langle \pi_1, \dots, \pi_n \rangle$, i.e. $\mathcal{R}_i(\pi_1, \dots, \pi_n) = U_i(\pi_1, \dots, \pi_n)$.

M^k	$\pi_2^{(1)}$	$\pi_2^{(2)}$	\dots	$\pi_2^{(k)}$
$\pi_1^{(1)}$	0, 1	1, 2	\dots	0, 3
$\pi_1^{(2)}$	2, 1	0, 1	\dots	1, 1
\vdots	\vdots	\vdots	\cdot	\vdots
$\pi_1^{(k)}$	5, 1	0, 1	\dots	4, 3

Policy Space Response Oracles – Construct Meta-Game

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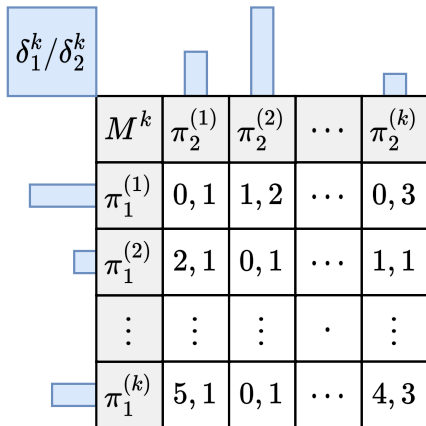
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Need to compute the expected returns of each agent for any joint policy $\langle \pi_1, \dots, \pi_n \rangle$ in the meta-game. How can we do this?

Solution

Compute average returns of each agent over multiple episodes of the underlying game with respective joint policy \rightarrow converges to expected returns in the limit.

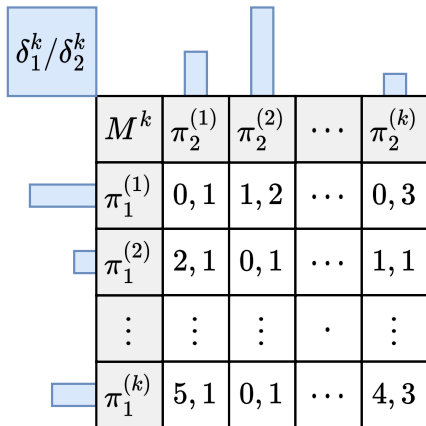
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δ_1^k / δ_2^k					
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Solution to the meta-game: distributions δ_i^k over policies in the population of agent i (for each agent $i \in I$).

Policy Space Response Oracles – Add Best-Response Policies

Each agent i determines an effective **oracle policy** π'_i against the solution distribution of the other agents and adds this policy to its population:

$$\Pi_i^{k+1} = \Pi_i^k \cup \{\pi'_i\}$$

M^k	$\pi_2^{(1)}$	$\pi_2^{(2)}$	\dots	$\pi_2^{(k)}$	π'_2
$\pi_1^{(1)}$	0, 1	1, 2	\dots	0, 3	?
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For example, agent i might determine its best-response policy

$$\pi'_i \in \arg \max_{\pi_i} \mathbb{E}_{\pi_{-i} \sim \delta_{-i}^k} [U_i(\langle \pi_i, \pi_{-i} \rangle)]$$

by training a policy π'_i using RL against sampled policies of the other agents.

Policy Space Response Oracles – Pseudocode

Algorithm Policy space response oracles (PSRO)

- 1: Initialize populations Π_i^1 for all $i \in I$ (e.g., random policies)
 - 2: **for** each generation $k = 1, 2, 3, \dots$ **do**
 - 3: Construct meta-game M^k from current populations $\{\Pi_i^k\}_{i \in I}$
 - 4: Use meta-solver on M^k to obtain distributions $\{\delta_i^k\}_{i \in I}$
 - 5: **for** each agent $i \in I$ **do** ▷ Train best-response policies
 - 6: **for** each episode $e = 1, 2, 3, \dots$ **do**
 - 7: Sample policies for other agents $\pi_{-i} \sim \delta_{-i}^k$
 - 8: Use single-agent RL to train π'_i wrt. π_{-i} in underlying game G
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Repeat this process until policy populations converge (new best-response policies are already in the respective populations), or for a fixed number of generations.

Policy Space Response Oracles in Rock-Paper-Scissors

If PSRO computes exact Nash equilibria solutions to the meta-game, and computes exact best-response policies, then the population distributions of PSRO converge to the Nash equilibrium of the underlying game.

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For example for rock-paper-scissors for two agents, with initial populations deterministically choosing rock and paper, respectively:

k	Π_1^k	Π_2^k	δ_1^k	δ_2^k	π'_1	π'_2
1	<u>R</u>	<u>P</u>	1	1	S	P
2	R, <u>S</u>	P	(0, 1)	1	S	R
3	R,S	<u>R</u> ,P	$(\frac{2}{3}, \frac{1}{3})$	$(\frac{2}{3}, \frac{1}{3})$	P	R/P
4	R, <u>P</u> ,S	R,P	$(0, \frac{2}{3}, \frac{1}{3})$	$(\frac{1}{3}, \frac{2}{3})$	R	S
5	R,P,S	R,P, <u>S</u>	$(\frac{1}{3}, \frac{1}{3}, \frac{1}{3})$	$(\frac{1}{3}, \frac{1}{3}, \frac{1}{3})$	R/P/S	R/P/S

AlphaStar – GrandMaster in StarCraft II

StarCraft II is a real-time strategy game for two or more players in which players have to collect resources, build infrastructure and armies to defeat their opponents.

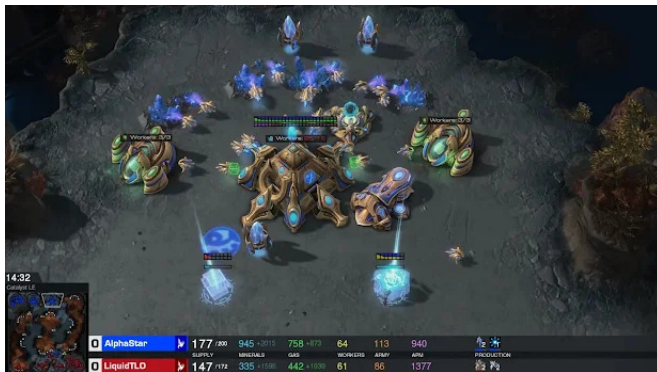


Figure: StarCraft II game, image source: <https://deepmind.google/discover/blog/alphastar-mastering-the-real-time-strategy-game-starcraft-ii/>.

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- **Partial observability:** players only observe a limited view of the game state
- **Diversity of strategies:** players choose between three available races offering many units and possible strategies

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- **Main agents**: largely trained in self-play and against any prior policy

AlphaStar – GrandMaster in StarCraft II

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Agents of each type are added to the league whenever they become effective (measured by win rates) against their respective opponents.

AlphaStar – GrandMaster in StarCraft II

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→ reached “GrandMaster” level in StarCraft II (top 0.2% of ranked human players).

We covered:

- Agent modelling with deep learning
- Parameter and experience sharing
- Policy self-play in zero-sum games
- Population-based training