# Multi-Agent Reinforcement Learning

Multi-Agent Reinforcement Learning in Games: First Steps and Challenges

Stefano V. Albrecht, Filippos Christianos, Lukas Schäfer Slides by: Leonard Hinckeldey

#### The MARL Book

This lecture is based on

Multi-Agent Reinforcement Learning: Foundations and Modern Approaches

by Stefano V. Albrecht, Filippos Christianos and Lukas Schäfer

MIT Press, 2024

Download book, slides, and code at: www.marl-book.com

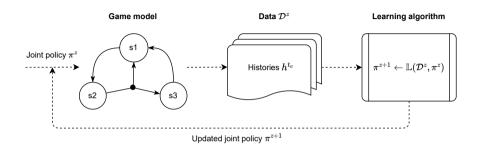


## Lecture Outline

- Learning framework for MARL
- Independent learning
- Central learning
- Modes of learning
- Challenges of MARL

# MARL Learning Framework

## **MARL Learning Process**



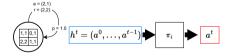
- The game model defines the learning environment
- Interaction data from joint policy  $\pi^z$  are collected as  $\mathcal{D}^z = \{h^{t_e} \mid e=1,\dots,z\}, z\geq 0$
- A learning algorithm updates the joint policy as  $\pi^{z+1} = \mathbb{L}(\mathcal{D}^z, \pi^z)$
- The learning goal is a chosen solution concept, e.g. Nash equilibrium



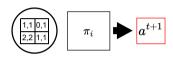
Normal-form games



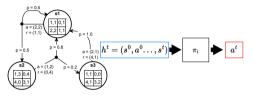
Normal-form games



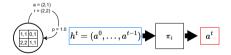
Repeated normal-form games



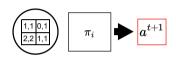
Normal-form games



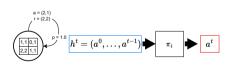
Stochastic games



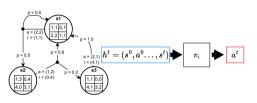
Repeated normal-form games



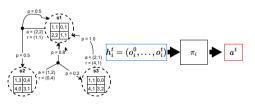
Normal-form games



Repeated normal-form games



Stochastic games



Partially observable stochastic games

## Convergence

To evaluate the learning algorithm, we typically assess whether the learnt joint policy has **converged** to an optimal joint policy:

$$\lim_{\mathsf{Z}\to\infty}\pi^{\mathsf{Z}}=\pi^*$$

- Optimal joint policies may differ depending on the solution concept
- There may be many valid solutions  $\Rightarrow$  e.g. multiple Nash equilibria
- ullet In practice, we cannot collect infinite data  $z o \infty$ 
  - ⇒ Learning typically stops after a predefined 'budget' (e.g. training steps)

## Single-Agent RL Reductions

The simplest way to apply RL algorithms in multi-agent settings is to reduce them to single-agent problems.

## Single-Agent RL Reductions

The simplest way to apply RL algorithms in multi-agent settings is to reduce them to single-agent problems.

#### Central learning:

- Apply one single-agent RL algorithm to control all agents centrally
  - $\Rightarrow$  A central policy is learned over the joint action space

## Single-Agent RL Reductions

The simplest way to apply RL algorithms in multi-agent settings is to reduce them to single-agent problems.

#### Central learning:

- Apply one single-agent RL algorithm to control all agents centrally
  - $\Rightarrow$  A central policy is learned over the joint action space

## Independent learning:

- Apply single-agent RL algorithms to each agent independently
  - $\Rightarrow$  Agents do not explicitly consider or represent each other

Central learning: learn a single central policy  $\pi_c$  which receives observations of all agents and selects an action for each agent (i.e. joint action  $(a_1, ..., a_n)$ ).

• Requires transforming the joint reward  $(r_1, \ldots, r_n)$  into a single scalar reward r

7

Central learning: learn a single central policy  $\pi_c$  which receives observations of all agents and selects an action for each agent (i.e. joint action  $(a_1, ..., a_n)$ ).

- Requires transforming the joint reward  $(r_1, \ldots, r_n)$  into a single scalar reward r
- This can be easy in some settings, e.g. in games with common rewards  $r=r_i$ , but difficult in zero-sum or general-sum games

Central learning: learn a single central policy  $\pi_c$  which receives observations of all agents and selects an action for each agent (i.e. joint action  $(a_1, ..., a_n)$ ).

- Requires transforming the joint reward  $(r_1, \ldots, r_n)$  into a single scalar reward r
- This can be easy in some settings, e.g. in games with common rewards  $r=r_i$ , but difficult in zero-sum or general-sum games
- Mays not scale well with the number of agents, as the joint action space may grow exponentially with the number of agents

Central learning: learn a single central policy  $\pi_c$  which receives observations of all agents and selects an action for each agent (i.e. joint action  $(a_1, ..., a_n)$ ).

- Requires transforming the joint reward  $(r_1, \ldots, r_n)$  into a single scalar reward r
- This can be easy in some settings, e.g. in games with common rewards  $r = r_i$ , but difficult in zero-sum or general-sum games
- Mays not scale well with the number of agents, as the joint action space may grow exponentially with the number of agents
- May also not be suitable in environments that require agents to act independently based on local observations

#### Algorithm Central Q-learning

- 1: Initialize: Q(s, a) = 0 for all  $s \in S$  and  $a \in A = A_1 \times ... \times A_n$
- 2: Repeat for every episode:
- 3: **for**  $t = 0, 1, 2, \dots$  **do**
- 4: Observe current state  $s^t$
- 5: With probability  $\epsilon$ : choose random joint action  $a^t \in A$
- 6: Otherwise: choose joint action  $a^t \in \arg \max_a Q(s^t, a)$
- 7: Apply joint action  $a^t$ , observe rewards  $r_1^t, \ldots, r_n^t$  and next state  $s^{t+1}$
- 8: Transform  $r_1^t, \ldots, r_n^t$  into scalar reward  $r^t$
- 9:  $Q(s^t, a^t) \leftarrow Q(s^t, a^t) + \alpha[r^t + \gamma \max_{a'} Q(s^{t+1}, a') Q(s^t, a^t)]$

**Independent Learning** 

## **Independent Learning**

Independent learning: each agent i learns its policy  $\pi_i$  using only its local history of observations.

• From the perspective of each agent *i*, the environment transition function looks like this:

$$\mathcal{T}_i(s^{t+1}|s^t, a_i) \propto \sum_{a_{-i} \in A_{-i}} \mathcal{T}(s^{t+1}|s^t, \langle a_i, a_{-i} \rangle) \prod_{j \neq i} \pi_j(a_j|s^t)$$

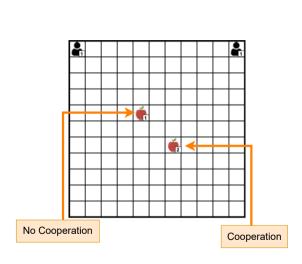
- ullet As each agent j's policies are updated, the action probabilities  $\pi_j$  change
  - $\Rightarrow$  From agent *i*'s perspective, the transition function  $\mathcal{T}_i$  appears non-stationary!

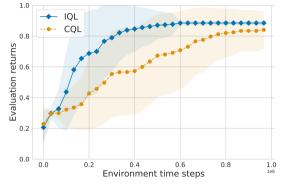
## Independent Q-learning

## Algorithm Independent Q-learning (IQL) for stochastic games

- 1: // Algorithm controls agent i
- 2: Initialize:  $Q_i(s, a_i) = 0$  for all  $s \in S$ ,  $a_i \in A_i$
- 3: Repeat for every episode:
- 4: **for**  $t = 0, 1, 2, \dots$  **do**
- 5: Observe current state  $s^t$
- 6: With probability  $\epsilon$ : choose random action  $a_i^t \in A_i$
- 7: Otherwise: choose action  $a_i^t \in \arg \max_{a_i} Q_i(s^t, a_i)$
- 8: (meanwhile, other agents  $j \neq i$  choose their actions  $a_i^t$ )
- 9: Observe own reward  $r_i^t$  and next state  $s^{t+1}$
- 10:  $Q_i(s^t, a_i^t) \leftarrow Q_i(s^t, a_i^t) + \alpha[r_i^t + \gamma \max_{a_i'} Q_i(s^{t+1}, a_i') Q_i(s^t, a_i^t)]$

## IQL and CQL in Level-Based Foraging





 IQL can learn more quickly, as CQL needs to explore 6<sup>2</sup> = 36 actions in each state

## Modes of Operation in MARL

Modes of operation in MARL:

## Self-play:

- Algorithm self-play: all agents use the same learning algorithm (and parameters)
- Policy self-play: agent's policy is trained directly against itself

## Mixed-play

• Agents use different learning algorithms



## **MARL Challenges**

#### Singe-Agent RL Challenges

- Unknown environment dynamics
- Exploration-exploitation dilemma
- Non-stationarity from bootstrapping
- Temporal credit assignment

## MARL Challenges

#### Singe-Agent RL Challenges

- Unknown environment dynamics
- Exploration-exploitation dilemma
- Non-stationarity from bootstrapping
- Temporal credit assignment

#### Multi-Agent RL Challenges

- Non-stationarity from multiple learning agents
- Equilibrium selection
- Multi-agent credit assignment
- Scaling to many agents

## A stochastic process $X^{t}_{t \in \mathbb{N}^{0}}$ is stationary if:

- The probability distribution of  $X^{t+\tau}$  does not depend on  $\tau \in \mathbb{N}^0$ , where t and  $t+\tau$  are time indices
- This means that the dynamics of the process do not change over time

## A stochastic process $X^t_{t \in \mathbb{N}^0}$ is stationary if:

- The probability distribution of  $X^{t+\tau}$  does not depend on  $\tau \in \mathbb{N}^0$ , where t and  $t+\tau$  are time indices
- This means that the dynamics of the process do not change over time

## Consider: $X^t$ samples the state $s^t$ at each time step t:

• In a MDP,  $X^t$  is completely defined by the state transition function  $\mathcal{T}(s^t|s^{t-1},a^{t-1})$  and the agent's policy  $\pi$  which selects an action  $a \sim \pi(.|s)$ 

## A stochastic process $X^t_{t \in \mathbb{N}^0}$ is stationary if:

- The probability distribution of  $X^{t+\tau}$  does not depend on  $\tau \in \mathbb{N}^0$ , where t and  $t+\tau$  are time indices
- This means that the dynamics of the process do not change over time

## Consider: $X^t$ samples the state $s^t$ at each time step t:

- In a MDP,  $X^t$  is completely defined by the state transition function  $\mathcal{T}(s^t|s^{t-1},a^{t-1})$  and the agent's policy  $\pi$  which selects an action  $a\sim\pi(.|s)$
- If  $\pi$  does not change, then this process is stationary (i.e. independent of t) because  $s^t$  depends only on  $s^{t-1}$ ,  $a^{t-1}$  and  $a^{t-1}$  depends only on  $s^{t-1}$  via  $\pi(.|s^{t-1})$

## A stochastic process $X^t_{t \in \mathbb{N}^0}$ is stationary if:

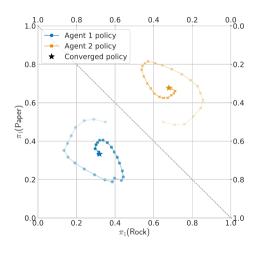
- The probability distribution of  $X^{t+\tau}$  does not depend on  $\tau \in \mathbb{N}^0$ , where t and  $t+\tau$  are time indices
- This means that the dynamics of the process do not change over time

## Consider: $X^t$ samples the state $s^t$ at each time step t:

- In a MDP,  $X^t$  is completely defined by the state transition function  $\mathcal{T}(s^t|s^{t-1},a^{t-1})$  and the agent's policy  $\pi$  which selects an action  $a\sim\pi(.|s)$
- If  $\pi$  does not change, then this process is stationary (i.e. independent of t) because  $s^t$  depends only on  $s^{t-1}$ ,  $a^{t-1}$  and  $a^{t-1}$  depends only on  $s^{t-1}$  via  $\pi(.|s^{t-1})$
- However, in RL the policy does change over time through the learning  $\pi^{z+1} = \mathbb{L}(\mathcal{D}^z, \pi^z)$ , which leads to **non-stationarity** in  $X^t$

## Non-Stationarity in Multi-Agent Settings

In MARL, non-stationarity is exacerbated by multiple agents changing their policies!



- $\pi^{z+1} = \mathbb{L}(\mathcal{D}^z, \pi^z)$  updates an *entire* joint policy  $\pi^z = (\pi_1^z, ..., \pi_n^z)$
- Environment is non-stationary from each agent's perspective
- Can cause cyclic learning dynamics where agents co-adapt to each other's changing policies

- Example: Stag Hunt matrix game
- Two hunters choose: cooperate to hunt stag (S) or go solo for hare (H)

	S	Н
S	4,4	0,3
Н	3,0	2,2

- Example: Stag Hunt matrix game
- Two hunters choose: cooperate to hunt stag (S) or go solo for hare (H)
- Nash equilibria: reward-dominant (S,S) maximizes reward, risk-dominant (H,H) minimizes risk

	S	Н
S	4,4	0,3
Н	3,0	2,2

- Example: Stag Hunt matrix game
- Two hunters choose: cooperate to hunt stag (S) or go solo for hare (H)
- Nash equilibria: reward-dominant (S,S) maximizes reward, risk-dominant (H,H) minimizes risk
- (S,S) requires trust; (H,H) offers a safe, lower reward

	S	Н
S	4,4	0,3
Н	3,0	2,2

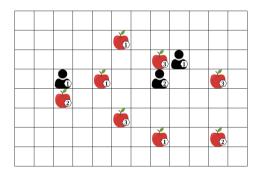
- Example: Stag Hunt matrix game
- Two hunters choose: cooperate to hunt stag (S) or go solo for hare (H)
- Nash equilibria: reward-dominant (S,S) maximizes reward, risk-dominant (H,H) minimizes risk
- (S,S) requires trust; (H,H) offers a safe, lower reward

	S	Н
S	4,4	0,3
Н	3,0	2,2

- Indep. Q-learning may bias towards (H,H) due to initial action uncertainty
- Early random actions can reinforce
   (H,H) since deviating from H is
   penalized if the other agent chooses H

## Multi-Agent Credit Assignment

Multi-agent credit assignment: which agent's actions contributed to receved rewards?



- At time step t all agents perform collect, each receiving reward +1
- Whose actions led to the reward?
- The agent on the left did not contribute
- For a learning agent that only observes s<sup>t</sup>, a<sup>t</sup>, r<sup>t</sup>, s<sup>t+1</sup>, disentangling the action contributions is difficult

	R	Р	S
R	0,0	-1,1	1,-1
Р	1,-1	0,0	-1,1
S	-1,1	1,-1	0,0

Joint actions can help disentangle agent contributions. Consider the RPS game:

	R	Р	S
R	0,0	-1,1	1,-1
Р	1,-1	0,0	-1,1
S	-1,1	1,-1	0,0

1. Agents choose actions  $(a_1, a_2) = (R, S)$   $\Rightarrow$  agent 1 receives reward +1

	R	Р	S
R	0,0	-1,1	1,-1
Р	1,-1	0,0	-1,1
S	-1,1	1,-1	0,0

- 1. Agents choose actions  $(a_1, a_2) = (R, S)$   $\Rightarrow$  agent 1 receives reward +1
- 2. Then agents choose  $(a_1, a_2) = (R, P)$   $\Rightarrow$  agent 1 receives reward -1

	R	Р	S
R	0,0	-1,1	1,-1
Р	1,-1	0,0	-1,1
S	-1,1	1,-1	0,0

- 1. Agents choose actions  $(a_1, a_2) = (R, S)$   $\Rightarrow$  agent 1 receives reward +1
- 2. Then agents choose  $(a_1, a_2) = (R, P)$   $\Rightarrow$  agent 1 receives reward -1
- 3. Action value  $Q(a_1)$  does not model agent 2, value for action R appears to be 0

	R	Р	S
R	0,0	-1,1	1,-1
Р	1,-1	0,0	-1,1
S	-1,1	1,-1	0,0

- 1. Agents choose actions  $(a_1, a_2) = (R, S)$   $\Rightarrow$  agent 1 receives reward +1
- 2. Then agents choose  $(a_1, a_2) = (R, P)$   $\Rightarrow$  agent 1 receives reward -1
- 3. Action value  $Q(a_1)$  does not model agent 2, value for action R appears to be 0
- 4. Joint action value model  $Q_1(a_1, a_2)$  can represent the effect of agent 2:  $Q_1(R, S) = +1$  and  $Q_1(R, P) = -1$

## Scaling to Many Agents

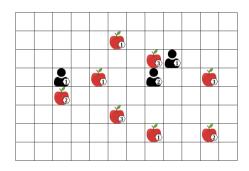
#### Problem

• Joint action space can grow exponentially with number of agents:

$$|A| = |A_1| \cdot ... \cdot |A_n|$$

- ullet If agents have associated features in s (e.g. agent position) then |S| also increases exponentially
  - $\Rightarrow$  How to scale efficiently to many agents?

## Scaling to Many Agents



Changing number of agents from 3 to 5 increases the number of joint actions from 216 to 7776!

## Summary

#### We covered:

- MARL learning process
- Independent and central learning
- Modes of operation in MARL
- Challenges of MARL

#### Next we'll cover:

• Foundational algorithms in MARL