

1. Solve the system of equations using the method of elimination and select the correct answer.

1 / 1 point

$$\begin{cases} x + y = 4 \\ -6x + 2y = 16 \end{cases}$$

- ☐ The system has infinitely many solutions.
- ☐ $x = 1, y = 3$
- ☒ $x = -1, y = 5$
- ☐ $x = 0, y = 0$
- ☐ The system has no solution.

✔ Correct

Correct! The solution for the system of equations is a unique point at x = -1, y = 5, as shown: $\begin{cases} -1 + 5 = 4 \\ -6(-1) + 2 * 5 = 16 \end{cases}$

2. For the questions 2-3, calculate the determinant of the matrices and determine if the matrices are singular or non-singular:

1 / 1 point

$$\begin{bmatrix} 4 & -3 \\ 7 & -8 \end{bmatrix}$$

- ☒ -11, Non-singular
- ☐ -53, Singular
- ☐ -53, Non-singular
- ☐ -11, Singular

✔ Correct

Correct! You can compute the determinant of a two-by-two matrix using the formula $ad - bc$, as explained in the video: [“Singular vs Non-singular Matrices”](#) [↗](#).

3.

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$$\begin{bmatrix} -3 & 8 & 1 \\ 2 & 2 & -1 \\ -5 & 6 & 2 \end{bmatrix}$$

- ☐ 36, Non-singular
- ☐ -80, Non-singular
- ☐ -20, Non-singular
- ☐ 0, Non-singular
- ☒ 0, Singular

✔ Correct

Correct! As explained in the video “Determinant for larger matrices”, you can use the formula $aei + bfg + cdh - afh - bdi - ceg$ to calculate the determinant of a three-by-three matrix. If the determinant is zero, then the matrix is singular.

4. Determine if the provided matrix has linearly dependent or independent rows (a, b, c, d, e, f are any real numbers):

1 / 1 point

$$\begin{bmatrix} a & b & c \\ d & e & f \\ 2a - d & 2b - e & 2c - f \end{bmatrix}$$

Hint: Can one row in the matrix be obtained as a result of operations on the other rows?

- ☒ Dependent
- ☐ It cannot be determined.
- ☐ Independent

✔ Correct

Great work! Row 3 can be obtained by adding (2 * row 1) + (-1 * row 2).

5. Which of the following operations, when applied to the rows of the matrix, do not change the singularity (or non-singularity) of the matrix:

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- ☒ Switching rows.

✔ Correct

Well done!

- ☒ Adding a row to another one.

✔ Correct

Correct!

- ☒ Multiplying a row by a nonzero scalar.

✔ Correct

Correct!

- ☐ Adding a nonzero fixed value to every entry of the row.

6. In the following matrix:

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$$\begin{bmatrix} a & a \\ b & c \end{bmatrix}$$

a, b, and c are non-zero real numbers. If the matrix is non-singular, which of the following must be true:

- ☐ c = b
- ☐ c = a only if a = b
- ☒ a = b only if c ≠ a

✔ Correct

Correct! You can compute the determinant of a matrix using the formula $ad - bc$. Please double-check if you did the calculation correctly.

- ☒ c ≠ b

✔ Correct

Correct! You can compute the determinant of a matrix using the formula $ad - bc$. Use this formula and the fact that the matrix is non-singular to solve this question.

7. Luis went yesterday to the bank to find out the interest rate of three different financial instruments. He received the following information:

0 / 1 point

Financial instrument	Savings account	Certificate of Deposit (CD)	Bonds
Annual interest	2%	3%	4%

He wants to invest his USD \$10,000 savings in these three accounts. By doing so, he knows that after a year he would receive a total of US \$ 260 in interest if he put twice as much money in the savings account as in the CDs, and “z” money in bonds.

Calculate the value of “z” , in USD, using the elimination method explained in the lectures.

- ☒ It cannot be determined.
- ☐ $z = \text{USD } \$1600$
- ☐ $z = \text{USD } \$5600$
- ☐ $z = \text{USD } \$2800$

✘ Incorrect

Not quite, please review your answer. If you have problems solving the system of equations please refer to the video: “Row-reduction for larger systems of equations”.