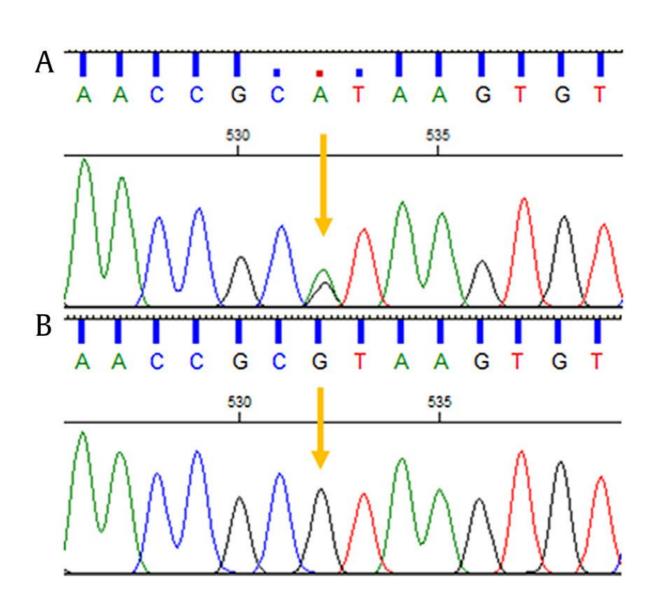
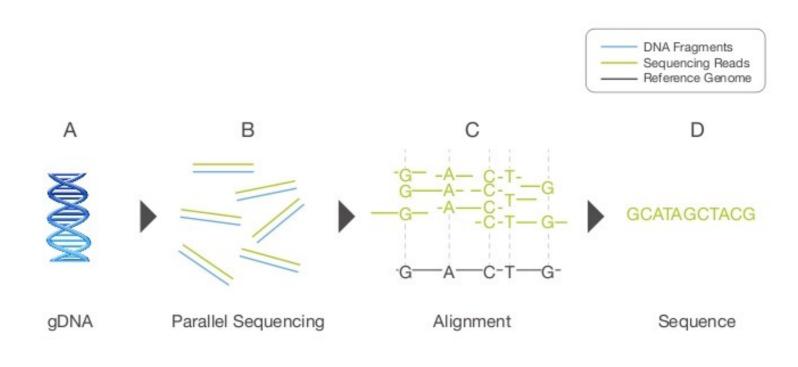


### Sanger Sequencing



### Next Generation Sequencing (NGS)

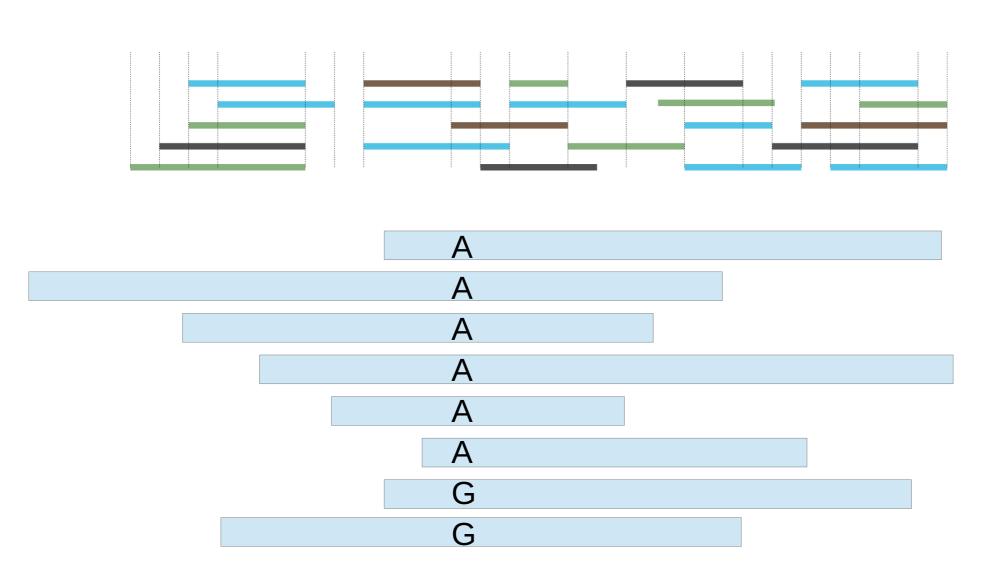


- A. Extracted gDNA
- B. gDNA is fragmented into a library of small segments that are each sequenced in parallel.
- C. Individual sequence reads are reassembled by aligning to a reference genome
- D. The whole-genome sequence is derived from the consensus of aligned reads.

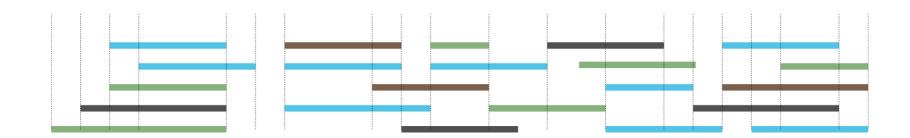
www.illumina.com

- However NGS has drawbacks:
  - High error rates
  - Shorter reads

# Sequencing depth / coverage

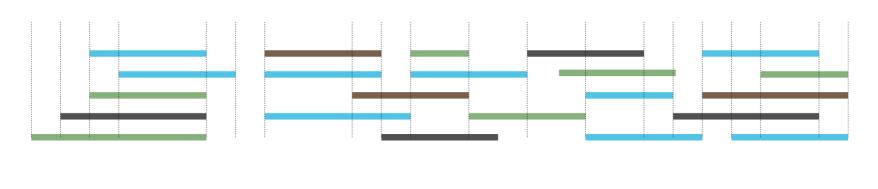


# Is the site variable in the sample?



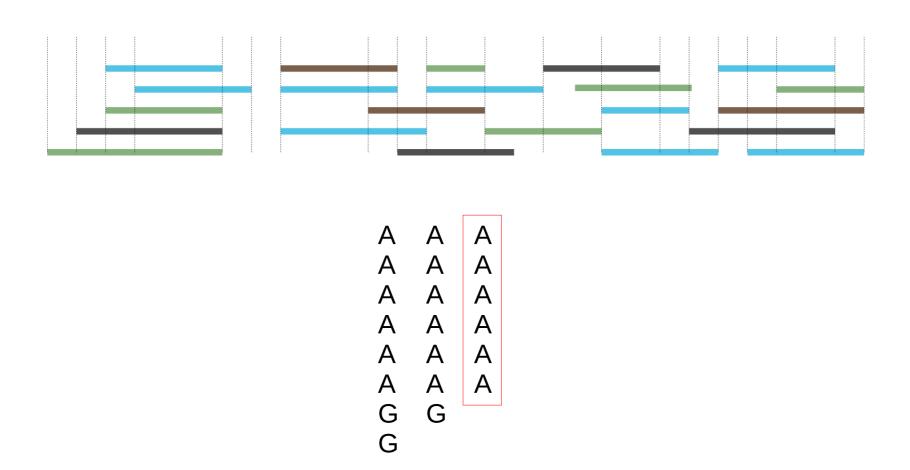
AAAAAGG

### Is the site <u>still</u> variable in the sample?

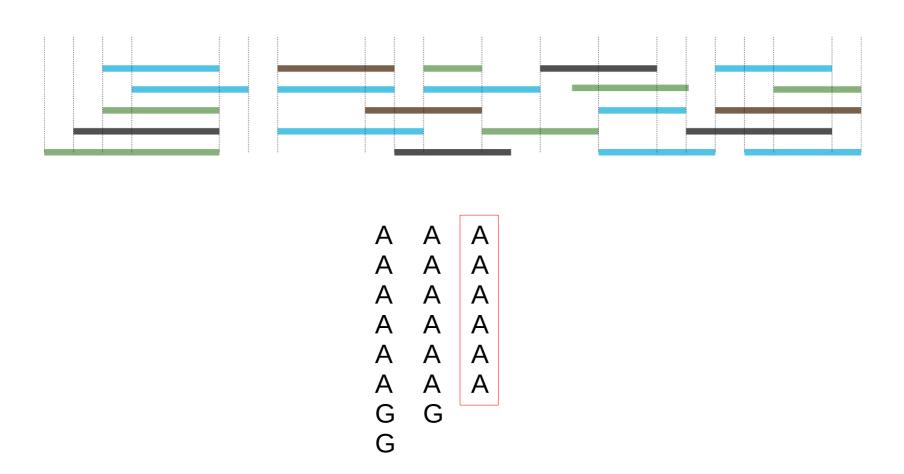


A A A A A A G G

### Is the site still variable in the sample/individual?



#### Is the site <u>still</u> variable in the sample/<u>individual</u>?

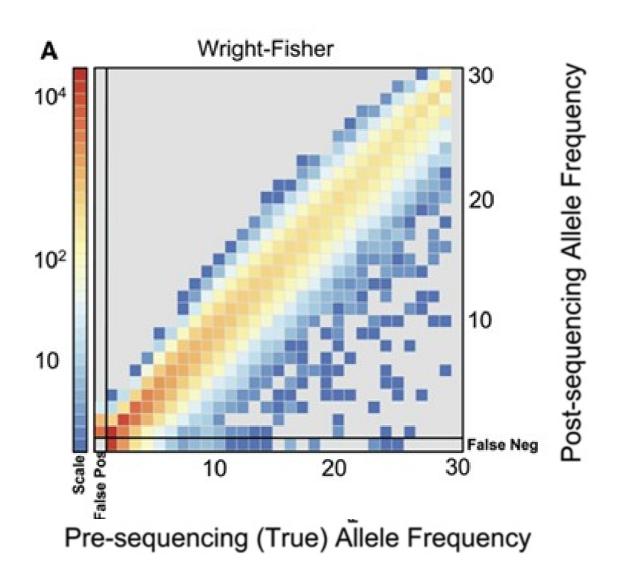


Common errors introduced here:

**SNP calling:** identification of variable sites.

Genotype calling: determination of the genotype for each site for each individual.

### Bias in allele frequencies



Crawford and Lazzaro 2012

### Possible solutions



#### Possible solutions





More sequencing depth?

More samples?

### It depends...

### Fixed budget

- Balance between <u>sample size</u> and <u>coverage</u> (uncertainty)
- Depends on objective
  - Reference genome (high coverage)
  - Rare variants (large sample sizes at high coverage)
  - Population genetics (large sample sizes)
- How low can we go?

# How to deal with uncertainty?

- Stricter filtering → Loss of data
- Probabilistic framework (genotype likelihoods)
  - Increased analytical power
  - Associated measure of statistical uncertainty
  - Incorporation of prior information

### Objective

- 1) What are **genotype likelihoods** (GL)?
- 2) How to do **SNP calling** from GL?
- 3) How to do **genotype calling** from GL?
- 4) What is the **error** in population genetic inferences using naïve strategies for **SNP** and **genotype** calling?
- 5) What is the optimal **sequencing design** for population genetics purposes?

### Objective

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### Genotype likelihoods

Probability of observing the read data, given a particular genotype

$$p(X|G=bh) = \frac{1}{2^r} \prod_{i=1}^r (L_b^{(i)} + L_h^{(i)})$$

Likelihood of observing allele *b* at read *i* 

### Genotype likelihoods – an example

-A-

$$\begin{split} P(X|AA) &= (\frac{L_A^{(1)}}{2} + \frac{L_A^{(1)}}{2}) * (\frac{L_A^{(2)}}{2} + \frac{L_A^{(2)}}{2}) * (\frac{L_A^{(3)}}{2} + \frac{L_A^{(3)}}{2}) * (\frac{L_A^{(4)}}{2} + \frac{L_A^{(4)}}{2}) \\ L_A^{(1)} &= L_A^{(2)} = 1 - \epsilon \qquad L_A^{(3)} = L_A^{(4)} = \frac{\epsilon}{3} \qquad (1 - \epsilon) + (\frac{\epsilon}{3}) + (\frac{\epsilon}{3}) + (\frac{\epsilon}{3}) + (\frac{\epsilon}{3}) = 1 \\ P(X|AC) &= (\frac{L_A^{(1)}}{2} + \frac{L_C^{(1)}}{2}) * (\frac{L_A^{(2)}}{2} + \frac{L_C^{(2)}}{2}) * (\frac{L_A^{(3)}}{2} + \frac{L_C^{(3)}}{2}) * (\frac{L_A^{(4)}}{2} + \frac{L_C^{(4)}}{2}) \\ L_A^{(1)} &= L_A^{(2)} = L_C^{(3)} = 1 - \epsilon \qquad L_C^{(1)} = L_C^{(2)} = L_A^{(3)} = L_A^{(4)} = L_C^{(4)} = \frac{\epsilon}{3} \end{split}$$

### Posterior probabilities of genotypes

**Prior** is derived assuming **HWE** from the estimated Minor Allele Frequency.

Genotype likelihood
$$P(G_{s}^{(i)}|X_{s}^{(i)}) = \frac{P(X_{s}^{(i)}|G_{s}^{(i)})P(G_{s}^{(i)})}{\sum_{G=0}^{2}P(X_{s}^{(i)}|G_{s}^{(i)})P(G_{s}^{(i)})}$$

$$P(A \mid B) = \frac{P(B \mid A)P(A)}{P(B)}$$

Nielsen et al 2012

#### **Priors**

### Model organisms

- Reference genome
- SNP databases
- Patterns of LD
- Known allele or genotype frequencies

- ...

### Non-model organisms

- Expected genotype frequencies under a model (e.g. HWE)
  - Works for most case, if population follows HWE
  - Exceptions:
    - Inbreeding (e.g. self-polinatign plans)
    - Asexual reproduction

### Objective

1) What are genotype likelihoods (GL)?

#### 2) How to do **SNP calling** from GL?

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### Objective

Sample	True genotype	Reads allele A	Read allele G
1	AA	7	0
2	AA	25	1
3	AG	5	3
4	AG	4	4
5	GG	0	2
6	GG	0	4
Total		41	14

What is the true frequency?

What is the estimated frequency?

What is the problem with that estimate?

### Estimating Allele Frequencies - ML

$$P(D|f) = \prod_{i=1}^{N} \sum_{g \in \{0,1,2\}} P(D|G = g)P(G = g|f)$$

- Likelihood function
- What is?
  - P(D | G) = P(X | G)
  - P(G = g | f)
- Estimate f, by optimizing the likelihood function through (e.g.) EM

$$- f = 0.46$$

#### **Priors**

- ANGSD uses the minor allele frequency (MAF) to call SNPs
  - Naive:
    - t > t (e.g., t = 1/2N)
  - Likelihood Ratio Test (LRT), comparing the goodness of fit (chi2) between:
    - Null model: *f* = 0
    - Alternative model: *f* <> 0

### Objective

- 1) What are genotype likelihoods (GL)?
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# Calling genotypes – 10 GL

Genotype	Likelihood (log10)	
AA	-2.49	
AC	-3.38	
AG	-1.22	
AT	-3.38	
CC	-9.91	
CG	-7.74	
CT	-9.91	
GG	-7.44	What is the genotype?
GT	-7.74	genotype:
TT	-9.91	

### Calling genotypes – 3 GL

Genotype	Likelihood
AA	-5.73
AG	-2.80
GG	-17.12

What is the genotype?

### Calling genotypes – GL ratio

$$\log_{10} \frac{L_{G(1)}}{L_{G(2)}} > t$$

i.e. t = 1 meaning that the most likely genotype is 10 times more likely than the second most likely one

**Pros and Cons?** 

**Genotype Quality?** 

Missing data?

### Calling genotypes – Posterior Probabilities (PP)

AAAG (A,G alleles)

 $\varepsilon = 0.01$ 

Genotype	Likelihood (log)	Prior	Posterior
AA	-5.73	1/3	0.05
AG	-2.80	1/3	0.95
GG	-17.12	1/3	0

### Calling genotypes – PP (reference prior)

AAAG (A,G alleles)

 $\varepsilon = 0.01$ 

A is reference  $\rightarrow$  P(AA) > P(AG) > P(GG)

Genotype	Likelihood (log)	Prior	Posterior
AA	-5.73	0.80	0.22
AG	-2.80	0.15	0.78
GG	-17.12	0.05	0

### Calling genotypes – PP (HWE prior)

AAAG (A,G alleles)

 $\varepsilon = 0.01$ 

f(a) = 0.7 (from a reference panel)

$$P(AA) = ?; P(AG) = ?; P(GG) = ?$$

Genotype	Likelihood (log)	Prior	Posterior
AA	-5.73	0.49	0.06
AG	-2.80	0.42	0.94
GG	-17.12	0.09	0

Can we assume HWE?

### Calling genotypes – PP (HWE prior)

AAAG (A,G alleles)

 $\varepsilon = 0.01$ 

f(a) = 0.7 (from the data itself)

$$P(AA) = ?; P(AG) = ?; P(GG) = ?$$

Genotype	Likelihood (log)	Prior	Posterior
AA	-5.73	0.49	0.06
AG	-2.80	0.42	0.94
GG	-17.12	0.09	0

Can we assume HWE?

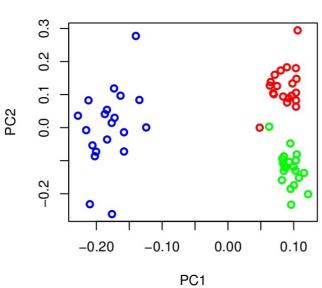
Can we estimate frequencies accurately?

### Objective

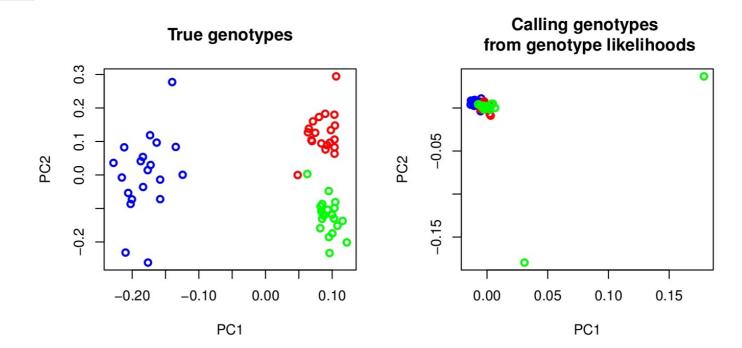
- 1) What are genotype likelihoods (GL)?
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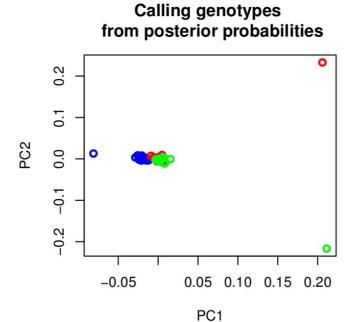
# Population structure - PCA



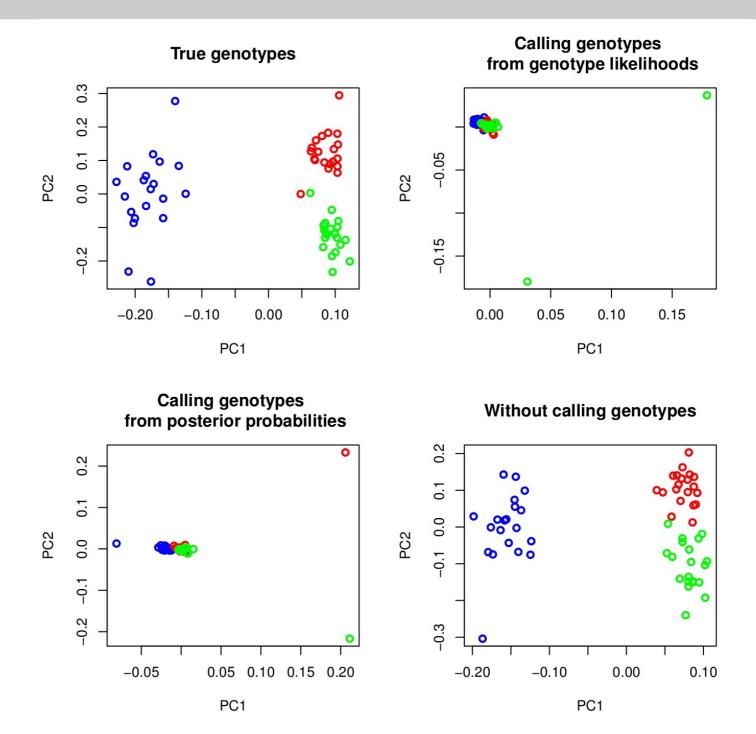


### Population structure - PCA

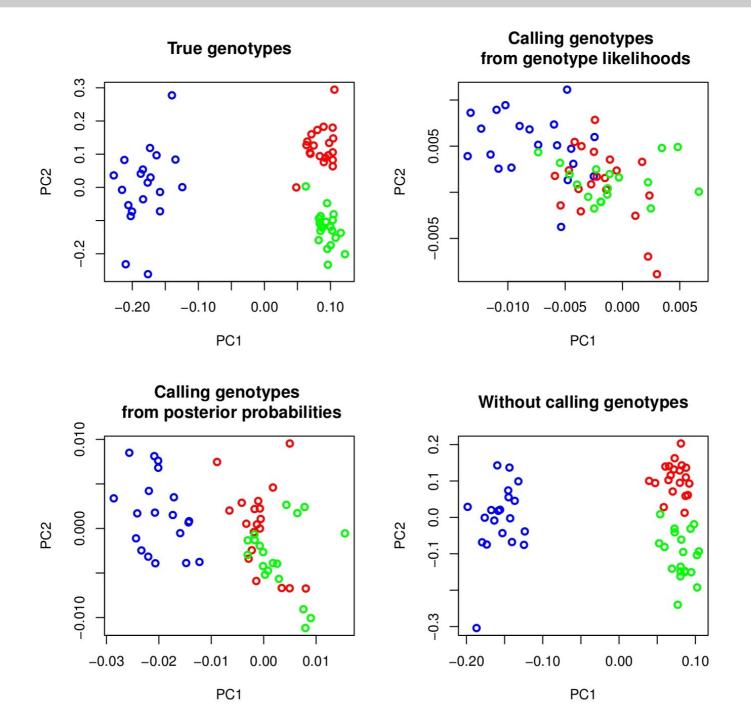




### Population structure - PCA



### Population structure – PCA (no outliers)



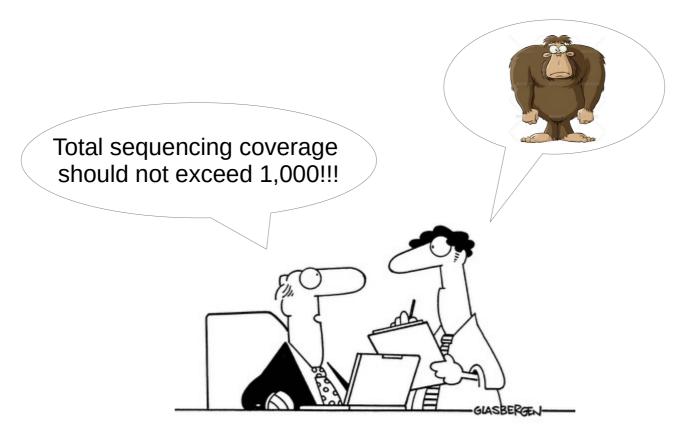
### Objective

- 1) What are genotype likelihoods (GL)?
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### Discovery of a "new" species/population

Population is comprised of **1,000 individuals**.

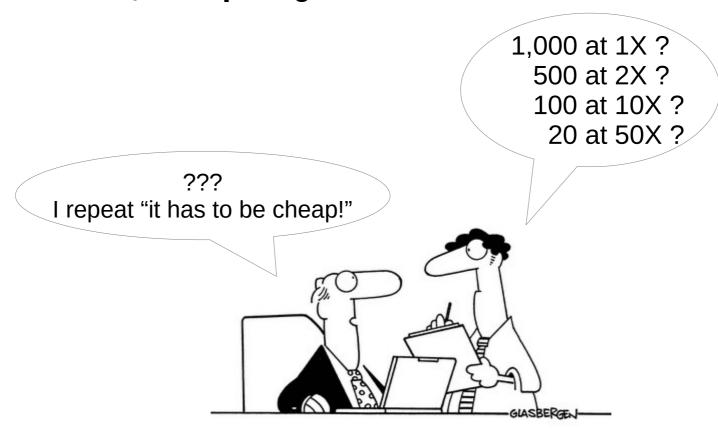
Genome is **100,000 bp** long.



### Planning the experiment

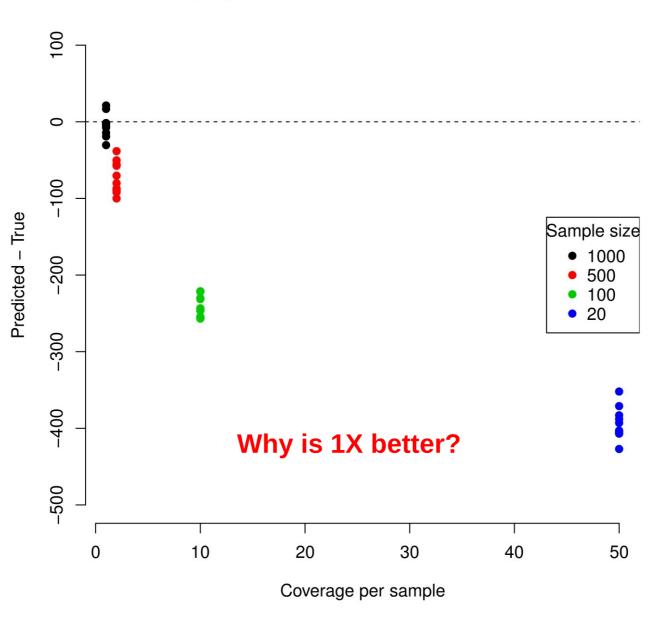
Population is comprised of **1,000 individuals**.

Genome is 100,000 bp long.

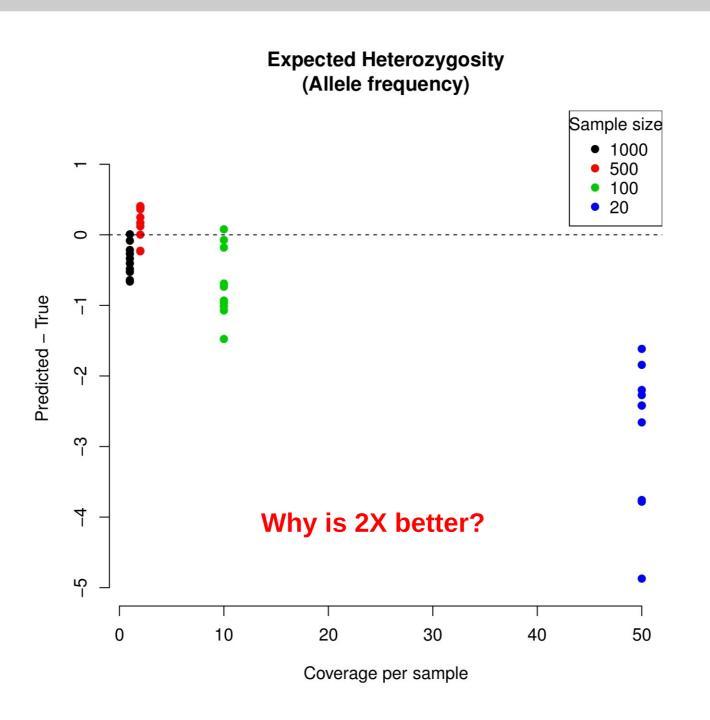


### How many polymorphic sites?

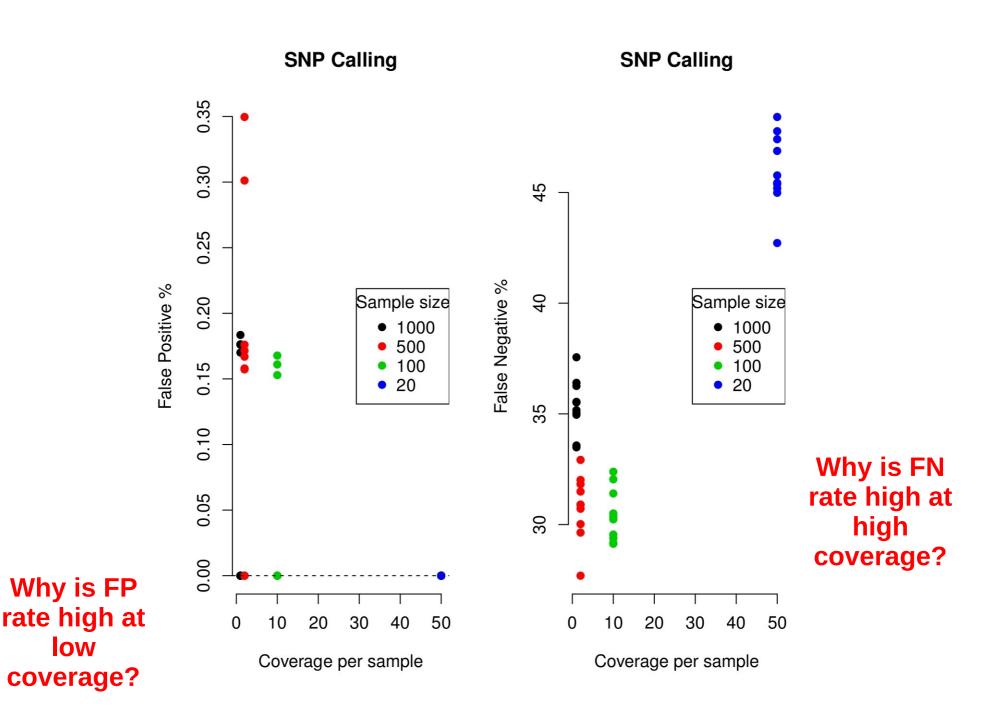




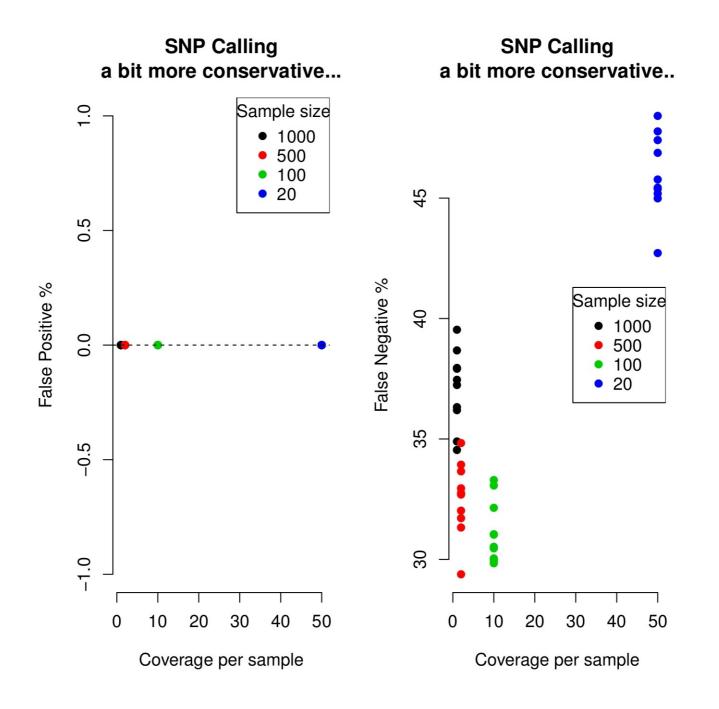
### How about the allele frequencies?



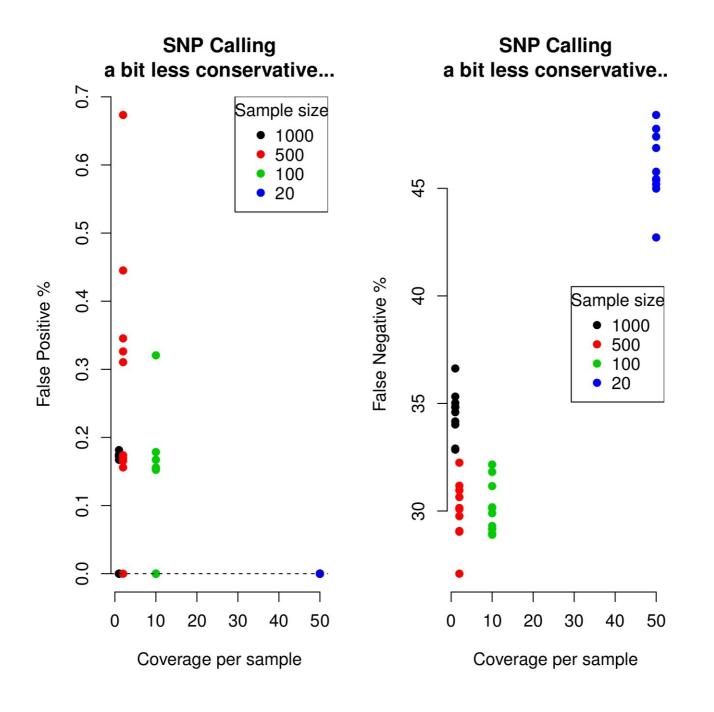
### Do you get the right SNPs?



### Do you get the right SNPs (more strict)?



### Do you get the right SNPs (less strict)?



#### Conclusions

It is important to take **statistical uncertainty** into account, specially for low coverage samples.

The methods presented provide **tools** for investigating population genetic variation for multiple populations on a large scale.

The great improvement in accuracy for low coverage data can be explained by the fact that we **do not call SNPs or genotypes**.

#### Acknowledgments



Rasmus Nielsen



Thorfinn Korneliussen
Anders Albrechtsen



Matteo Fumagalli

#### Software available at:

http://popgen.dk/software/angsd.html

https://github.com/fgvieira

https://github.com/mfumagalli/ngsTools

#### Performance of PCA

