## **Option: Partial Computations & Handling Errors without Exceptions**

This exercise set assumes that you have read chapters 1–4 of [Chiusano, Bjarnason 2014]. This is a mandatory hand-in. See detailed rules on the course website. Hand in only the file Exercises.scala. No zip files are accepted.

This week we start to use the implementation of standard library Lists.<sup>1</sup>

We start with few simple exercises on ADTs and traits (Chapter 3).

**Exercise 1.** This exercise is about traits (a feature of Scala that is independent of functional programming). We will use it to obtain a simple form of dependency injection. We will extend an existing class java.awt.Point with a new set of operators (comparisons).

Define a trait OrderedPoint extending the generic scala.math.Ordered[Point]. Implement the missing method compare from Ordered[Point], using the lexicographic ordering, i.e. (x,y) < (x',y') iff x < x' or  $x = x' \land y < y'$ . The method should return +1 if the left argument is larger, -1 if the right argument is larger, and zero if both sides are equal.

You will need to restrict the trait to only be allowed to be mixed into subclassess of java.awt.Point to access the x and y components of the objects. This is done by inserting the following constraint in the beginning of the trait block: "this: java.awt.Point =>" (Google for trait's self-types if you want to know more about these constraints).

Now mix the new java.awt.Point into java.awt.Point and create some ad hoc point objects using this trait. Test the extension in the Scala REPL by comparing some point instances using the less than (<) operator.<sup>2</sup>

Reflect on what has just happened: We can use infix comparison operators with classes that were defined in the java. awt package. These classes existed long before Scala existed, but we did not need to modify their source or to recompile them.

**Exercise 2.** Write a function size that counts nodes (leaves and branches) in a tree.<sup>3</sup> Use recursion explicitly.

Exercise 3. Write a function maximum that returns the maximum element in a Tree[Int]. Note: In Scala, you can use x.max(y) or x max y to compute the maximum of two integers x and y.<sup>4</sup> Use recursion explicitly.

Exercise 4. Write a function map, analogous to the function of the same name on List, that modifies each element in a tree with a given function.<sup>5</sup>

**Exercise 5.** Generalize size, maximum, and map, writing a new function fold that abstracts over their similarities. Reimplement them in terms of this more general function.<sup>6</sup>

Exercise 6. Implement map, get0rElse, flatMap, filter on Option (Chapter 4). This time, just

<sup>&</sup>lt;sup>1</sup>https://www.scala-lang.org/api/2.13.3/scala/collection/immutable/List.html

<sup>&</sup>lt;sup>2</sup>A variation of Exercise 10.2 [Horstmann 2012]

<sup>&</sup>lt;sup>3</sup>Exercise 3.25 [Chiusano, Bjarnason 2014]

<sup>&</sup>lt;sup>4</sup>Exercise 3.26 [Chiusano, Bjarnason 2014]

<sup>&</sup>lt;sup>5</sup>Exercise 3.28 [Chiusano, Bjarnason 2014]

<sup>&</sup>lt;sup>6</sup>Exercise 3.29 [Chiusano, Bjarnason 2014]

to train the difference, we implement them as methods (member functions), not as static functions. As you implement each function, think what it means and in what situations you'd use it. Refer to the book's Chapter 4, and Exercise 4.1 for hints and context information. In this exercise, you shall use pattern matching (so that its use can be reduced in the exercises below).<sup>7</sup>

**Note:** Now that you had implemented a monadic API for Option, you should not need to use pattern matching much below.

**Exercise 7.** A grading sheet with exam results is a list of pairs, where the first component in each pair is a String storing a name, and the second component in each pair is an integer representing the exam result. For example: List[("Alice", 12), ("Bob", 12), ("Charles", 12)]. Write a function headGrade that, given such a list, returns the grade of the first person on the list, or fails with None:

```
def headGrade (results: List[(String,Int)]): Option[Int]
```

Use the helper function headOption provided in the exercise Scala file. You can use map or a for comprehension, but not pattern matching.

Exercise 8. Implement the variance function in terms of flatMap. If the mean of a sequence is m, the variance is the mean of math.pow(x - m, 2) for each element x in the sequence.

A variance computation is something that you could need to implement in a machine learning or a data analytics application. Don't use pattern matching. You should also be able to avoid isEmpty. This is likely your first experience of a computation in a monad.

Once the function works with flatMap, rewrite it with for-yield comprehensions without using flatMap. Reflect on the differences between the two implementations, and think which one you find easier to understand.

**Exercise 9.** Section 4.3.2 in the text book recasts the map function as a general lifter that can change any function of type A =>B into a function of type Option[A] =>Option[B]. This only works for unary functions. This exercise tries to achieve a similar effect for binary functions. Write a generic function map2 that combines two Option values using a binary function:

```
def map2[A,B,C] (ao: Option[A], bo: Option[B]) (f: (A,B) =>C): Option[C]
```

If either Option value is None, then the return value is None, too. Do not use pattern matching. Use map/flatMap or for-yield comprehensions. 9

Besides being a lifter of binary functions to the Option universe, the map2 function can also be seen as a sequencer: it combines (sequences) the result of a fallible execution producing ao with the result of a fallible execution producing ab. The combination itself happens if both results are successful, and is done using f.

**Exercise 10.** This exercise attempts to generalize map2 from two to arbitrary many values. Imagine that we have a list of employees and we had retrieved salary rate for each of them. If the database connection failed for an employee, we received a None otherwise a Some object carrying the value. Thus we get a list of options. We would like to abort the entire computation and return None if at least one values on the list is None — if the database failed at least once we should report to the caller

<sup>&</sup>lt;sup>7</sup>Exercise 4.1 [Chiusano, Bjarnason 2014]

<sup>&</sup>lt;sup>8</sup>Exercise 4.2 [Chiusano, Bjarnason 2014]

<sup>&</sup>lt;sup>9</sup>Exercise 4.3 [Chiusano, Bjarnason 2014]

that there was an error and stop. To do this, we need sequence not a pair of results but an entire list. Write a function sequence that combines a list of Options into one Option containing a list of all the Some values in the original list:

```
def sequence[A] (aos: List[Option[A]]): Option[List[A]]
```

If the original list contains None even once, the result of the function should be None; otherwise the result should be Some with a list of all the values. Do not use pattern matching, and recall that you have foldRight available on lists.

**NB.** This is an example, where it seems inappropriate to define the function as a method in the object-oriented style. The function sequence likely should not be a method on a List, as this would tangle List to Option, which appears not very natural. Sequencing partial computations belongs better with Option, which is concerned with partial computations. However, sequence cannot be a method on Option as its argument is List! Thus we put it in companion object of Option.<sup>10</sup>

## **Exercise 11.** Implement a function traverse:

```
def traverse[A,B] (a: List[A]) (f: A =>Option[B]): Option[List[B]]
```

The function behaves like map executed sequentially on the list a, where the mapped function f can fail. If at least one application fails, then the entire computation of the mapping (traversal) fails. The traverse function does not increase the power of what we can do, but it can be implemented more efficiently than using map and sequence in combination. This is because map, being a polymorphic structure-preserving function oblivious to the types of transformed values, will not see by itself that it should stop on the first None.<sup>11</sup>

<sup>&</sup>lt;sup>10</sup>Exercise 4.4 [Chiusano, Bjarnason 2014]

<sup>&</sup>lt;sup>11</sup>Exercise 4.5 [Chiusano, Bjarnason 2014]