234auswertung

April 1, 2025

```
[25]: import matplotlib.pyplot as plt
   import matplotlib.patches as mpatches
   import numpy as np
   from scipy.signal import argrelextrema
   from scipy.optimize import curve_fit
   from scipy.stats import chi2

   plt.rcParams.update({'font.size': 14})

   %run ../lib.ipynb

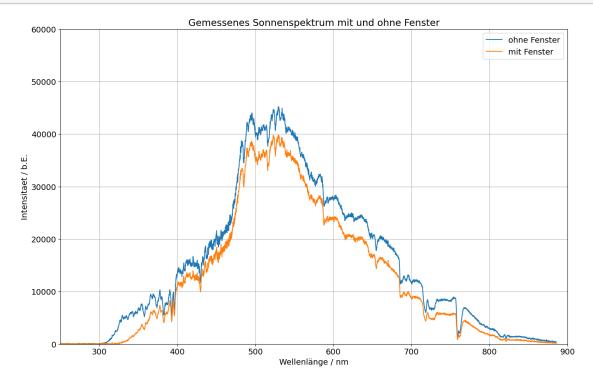
   class Consts:
      hc = 1.2398 * 10**(3) #nm eV
      E_Ry = -13.605 # eV

[26]: def comma_to_float(valstr):
      return float(valstr.replace(',','.'))
```

0.0.1 Sonnenspektrum und Fraunhoferlinien

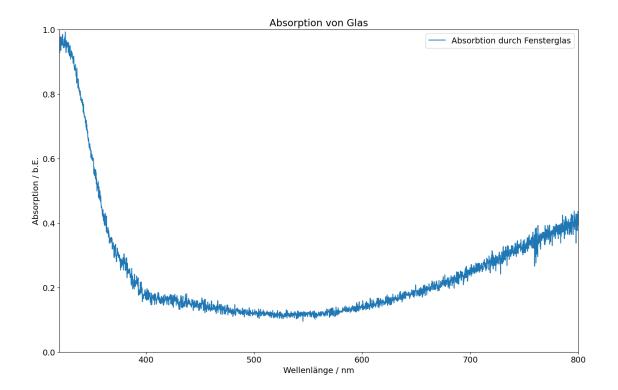
```
plt.figure(figsize=(16,10))
  plt.plot(lamb_og, inten_og, label='ohne Fenster')
  plt.plot(lamb_mg, inten_mg, label='mit Fenster')
  plt.title('Gemessenes Sonnenspektrum mit und ohne Fenster')
  plt.xlabel('Wellenlänge / nm')
  plt.ylabel('Intensitaet / b.E.')
  plt.legend()
  plt.grid()
  plt.ylim((0,60000))
  plt.xlim((250,900))
```

```
plt.savefig('out/himmel_m_o_g.png', format='png', bbox_inches='tight')
```



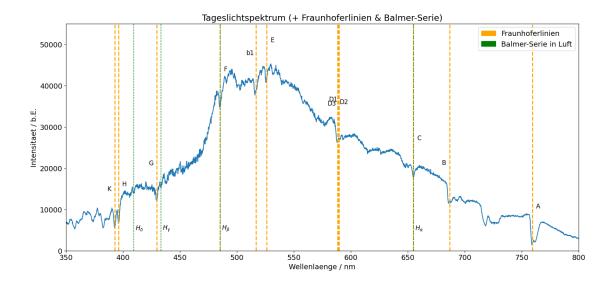
```
[29]: A = 1 - inten_mg[600:] / inten_og[600:]

plt.figure(figsize=(16,10))
plt.plot(lamb_mg[600:], A, label='Absorbtion durch Fensterglas')
plt.title('Absorption von Glas')
plt.xlabel('Wellenlänge / nm')
plt.ylabel('Absorption / b.E.')
plt.ylim((0,1))
plt.xlim((320,800))
plt.legend()
plt.savefig("out/absorption_glas.png", format='png', bbox_inches='tight')
```



```
[30]: # lokale minima, abgelesen aus textdatei:
      mins = [
          ('K', 393.0, 1, 5533.61, 393.4),
          ('H', 396.1, 1, 6619.03, 396.8),
          ('G', 429.8, 1, 11786.06, 430.8),
          ('F', 485.2, 1, 34493.94, 486.1),
          ('b1', 516.7, 1, 38450.61, 518.4),
          ('E', 526.2, 1, 41561.48, 527.0),
          ('D3', 588.4, 1, 26230.38, 587.6),
          ('D2', 589.0, 1, 26549.87, 589.0),
          ('D1', 589.7, 1, 27166.31, 589.6),
          ('C', 655.0, 1, 17813.23, 656.3),
          ('B', 686.7, 1, 11865.93, 686.7),
          ('A', 759.4, 1, 1339.37, 759.4)
      ]
      balmer_air_nist = [
          (r'$H_\lambda; 655.0, 1, 656.3),
          (r'$H_<table-cell>, 485.2, 1, 486.1),
          (r'$H_\gamma$', 433.4, 1, 434.0),
          (r'$H_\delta$', 409.5, 1, 410.1),
      ]
```

```
plt.figure(figsize=(18,8))
plt.plot(lamb_og, inten_og)
plt.title('Tageslichtspektrum (+ Fraunhoferlinien & Balmer-Serie)')
plt.xlabel('Wellenlaenge / nm')
plt.ylabel('Intensitaet / b.E.')
plt.ylim((0,55000))
plt.xlim((350,800))
i = 0
for m in mins:
    print(f'\{m[0]\}\t :: expected = \{m[4]\}nm, measured = \{m[1]\}nm, diff = 0
 plt.axvline(x=m[1], linewidth=2, linestyle='--', color='orange')
    plt.text(x=m[1] + (5 * (-1 if i % 2 == 0 else 1)), y=(m[3]+9000), s=m[0], u
  ⇔ha='center', fontsize=12)
    i = i + 1
#plt.xticks(np.arange(350, 801, 5))
for b in balmer_air_nist:
    print(f'\{b[0]\}\t :: expected = \{b[3]\}nm, measured = \{b[1]\}nm, diff = 0
  plt.axvline(x=b[1], linewidth=1, linestyle='--', color='green')
    plt.text(x=b[1] + 5, y=5000, s=b[0], ha='center', fontsize=12)
fraunhofer_patch = mpatches.Patch(color='orange', label='Fraunhoferlinien')
balmer_air_patch = mpatches.Patch(color='green', label='Balmer-Serie in Luft')
plt.legend(handles=[fraunhofer_patch, balmer_air_patch])
plt.savefig("out/spektrum_fraunhofer_balmer.png", format='png', __
  ⇔bbox_inches='tight')
K
         :: expected = 393.4nm, measured = 393.0nm, diff = 0.4
         :: expected = 396.8nm, measured = 396.1nm, diff = 0.7
Η
G
        :: expected = 430.8nm, measured = 429.8nm, diff = 1.0
F
         :: expected = 486.1nm, measured = 485.2nm, diff = 0.91
b1
         :: expected = 518.4nm, measured = 516.7nm, diff = 1.7
Ε
         :: expected = 527.0nm, measured = 526.2nm, diff = 0.8
        :: expected = 587.6nm, measured = 588.4nm, diff = 0.8
D3
D2
        :: expected = 589.0nm, measured = 589.0nm, diff = 0.0
D1
         :: expected = 589.6nm, measured = 589.7nm, diff = 0.11
        :: expected = 656.3nm, measured = 655.0nm, diff = 1.3
C
        :: expected = 686.7nm, measured = 686.7nm, diff = 0.0
         :: expected = 759.4nm, measured = 759.4nm, diff = 0.0
                :: expected = 656.3nm, measured = 655.0nm, diff = 1.3
$H_\alpha$
                :: expected = 486.1nm, measured = 485.2nm, diff = 0.91
$H_\beta$
                :: expected = 434.0nm, measured = 433.4nm, diff = 0.61
$H_\gamma$
                :: expected = 410.1nm, measured = 409.5nm, diff = 0.61
$H_\delta$
```



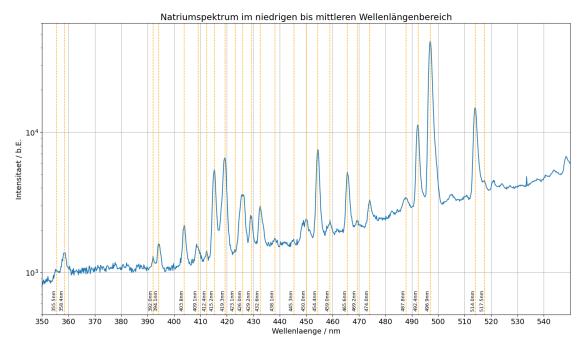
0.0.2 Auswertung des Natriumspektrums

```
[31]: # Aufgabe 3
      lamb na_a3_500, inten na_a3_500=np.loadtxt('na_a3_500nm_saett.txt', skiprows=17,
              converters= {0:comma_to_float, 1:comma_to_float},
              comments='>', unpack=True)
      plt.figure(figsize=(18,10))
      plt.plot(lamb_na_a3_500[586:], inten_na_a3_500[586:])
      plt.title('Natriumspektrum im niedrigen bis mittleren Wellenlängenbereich')
      plt.xlabel('Wellenlaenge / nm')
      plt.ylabel('Intensitaet / b.E.')
      plt.yscale('log')
      plt.ylim((500,60000))
      plt.xlim((350,550))
      plt.xticks(np.arange(350, 550, 10))
      plt.grid()
      13 = [(355.5, 1, 1039.16),
      (358.4, 1, 1367.92),
      (392.0, 1, 1295.52),
      (394.1, 1, 1598.57),
      (403.8, 1, 2159.1),
      (409.1, 1, 1526.74),
      (412.4, 1, 1418.91),
      (415.2, 1, 5372.36),
      (419.3, 1, 6594.08),
      (423.1, 1, 1462.68),
```

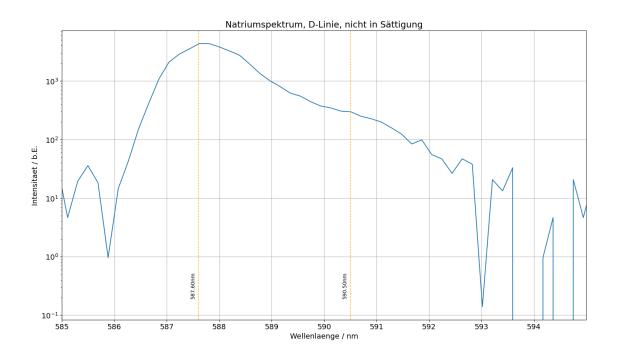
```
(426.0, 1, 3580.95),
(429.2, 1, 2424.05),
(432.6, 1, 2966.71),
(438.1, 1, 1753.96),
(445.3, 1, 1729.02),
(450.0, 1, 2404.7),
(454.4, 1, 7544.74),
(459.0, 1, 2348.89),
(465.6, 1, 5187.63),
(469.2, 1, 2338.7),
(474.0, 1, 3294.8),
(487.8, 1, 3435.13),
(492.4, 1, 11274.4),
(496.9, 2, 44422.62),
(514.0, 1, 14992.8),
(517.5, 1, 4546.21)]
for 1 in 13:
    plt.axvline(x=1[0], linewidth=1, linestyle='--', color='orange')
    #plt.axvline(x=l[0]+l[1], linewidth=0.5, linestyle=':', color='gray')
    #plt.axvline(x=l[0]-l[1], linewidth=0.5, linestyle=':', color='gray')
    plt.text(x=1[0]-1, y=540, rotation=90, s=f'{1[0]:0.1f}nm', ha='center',

    fontsize=9, color='black')

plt.savefig("out/na_spek_350_550.png", format='png', bbox_inches='tight')
```



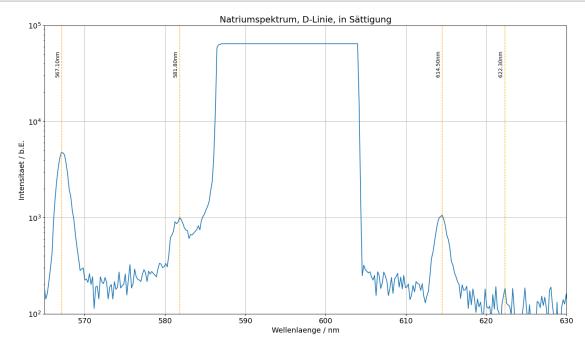
```
[32]: # Aufgabe 4, D-Linie nicht in Sättigung
      lamb_na_a4_589_ks, inten_na_a4_589_ks=np.loadtxt('na_a4_589nm_keine_saett.txt',_
       ⇔skiprows=17,
              converters= {0:comma_to_float, 1:comma_to_float},
              comments='>', unpack=True)
      plt.figure(figsize=(18,10))
      plt.plot(lamb_na_a4_589_ks, inten_na_a4_589_ks)
      plt.title('Natriumspektrum, D-Linie, nicht in Sättigung')
      plt.xlabel('Wellenlaenge / nm')
      plt.ylabel('Intensitaet / b.E.')
      plt.yscale('log')
      #plt.ylim((0,60000))
      plt.xlim((585,595))
      plt.xticks(np.arange(585, 595, 1))
      plt.grid()
      14_ks = [
          (587.6, 1, 4340.19),
          (590.5, 1, 295.86)
      ]
      for 1 in 14_ks:
          plt.axvline(x=1[0], linewidth=1, linestyle='--', color='orange')
          #plt.axvline(x=l[0]+l[1], linewidth=1, linestyle=':', color='gray')
          #plt.axvline(x=l[0]-l[1], linewidth=1, linestyle=':', color='qray')
          plt.text(x=1[0]-0.1, y=0.2, rotation=90, s=f'{1[0]:0.2f}nm', ha='center', ___
       ⇔fontsize=10, color='black')
      plt.savefig("out/na_spek_dlinie_nichtsaett.png", format='png',__
       ⇔bbox_inches='tight')
```



```
[33]: # Aufgabe 4, D-Linie in Sättigung
      lamb_na_a4_589_s, inten_na_a4_589_s=np.loadtxt('na_a4_589nm_saett.txt',u
       ⇔skiprows=17,
              converters= {0:comma_to_float, 1:comma_to_float},
              comments='>', unpack=True)
      plt.figure(figsize=(18,10))
      plt.plot(lamb_na_a4_589_s, inten_na_a4_589_s)
      plt.title('Natriumspektrum, D-Linie, in Sättigung')
      plt.xlabel('Wellenlaenge / nm')
      plt.ylabel('Intensitaet / b.E.')
      plt.yscale('log')
      plt.ylim((100,100000))
      plt.xlim((565,630))
      plt.grid()
      14 s = [
          (567.1, 1, 4787.3),
          (581.8, 1, 1004.7),
          (614.5, 1, 1062.04),
          (622.3, 1, 185.51)
      ]
      for 1 in 14_s:
          plt.axvline(x=1[0], linewidth=1, linestyle='--', color='orange')
```

```
#plt.axvline(x=l[0]+l[1], linewidth=1, linestyle=':', color='gray')
#plt.axvline(x=l[0]-l[1], linewidth=1, linestyle=':', color='gray')
plt.text(x=l[0]-0.5, y=30000, rotation=90, s=f'{l[0]:0.2f}nm', ha='center',
fontsize=10, color='black')

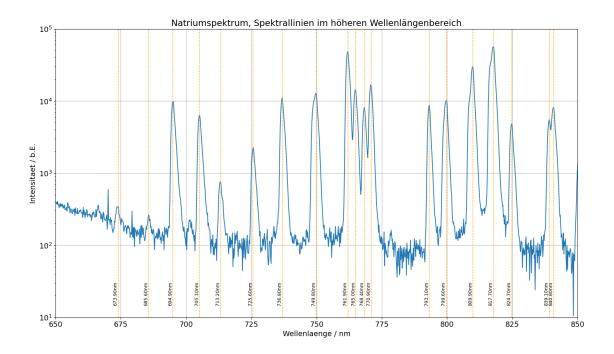
plt.savefig("out/na_spek_dlinie_saett.png", format='png', bbox_inches='tight')
```



```
(673.9, 1, 338.15),
    (685.6, 1, 264.02),
    (694.9, 1, 9924.29),
    (705.1, 1, 6364.51),
    (713.2, 1, 755.53),
    (725.6, 1, 2266.11),
    (736.8, 1, 11056.81),
    (749.8, 1, 12873.36),
    (761.9, 1, 48696.02),
    (765.0, 1, 14367.15),
    (768.4, 1, 8108.97),
    (770.9, 1, 17108.15),
    (793.1, 1, 8694.69),
    (799.6, 1, 10187.65),
    (809.9, 1, 29784.67),
    (817.7, 1, 57133.65),
    (824.7, 1, 4831.81),
    (839.1, 1, 5503.13),
    (840.8, 1, 8105.69)
]
for 1 in 1_a5:
    plt.axvline(x=1[0], linewidth=1, linestyle='--', color='orange')
    #plt.axvline(x=l[0]+l[1], linewidth=0.5, linestyle=':', color='qray')
    #plt.axvline(x=l[0]-l[1], linewidth=0.5, linestyle=':', color='gray')
    plt.text(x=1[0]-1, y=15, rotation=90, s=f'{1[0]:0.2f}nm', ha='center', __

    fontsize=9, color='black')

plt.savefig("out/na_spek_650_850.png", format='png', bbox_inches='tight')
```



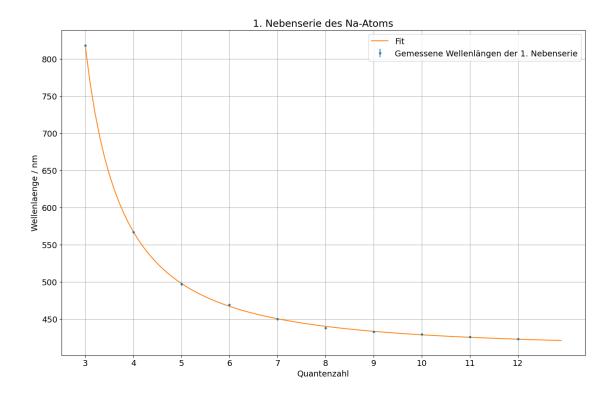
```
[35]: # Erwartete Linien für die 1. Nebenserie: md -> 3p
      lambda_3 = ValErr(817.7, 1) #nm
     E_3p = (Consts.E_Ry / 3**2) - (Consts.hc / lambda_3)
     print(E_3p.strfmtf(5,0,'E_3p'))
      meas_1ns_vals = [
          817.7,
          567.1,
          496.9,
          469.2,
          450.0,
          438.1,
          432.6,
          429.2,
          426.0,
          423.1
      ]
      meas_1ns_errs = np.array([1,1,2,1,1,1,1,1,1,1])
      for m in range(3,13):
          1= Consts.hc / ((Consts.E_Ry / m**2) - E_3p)
```

```
print(f'm = {m:2d}, lambda = {l.strfmtf(3,0)}, lambda_measured = __
       -{(meas_1ns_vals[m-3]):6.2f}, diff = {ValErr(meas_1ns_vals[m-3],_
       →meas_1ns_errs[m-3]).sigmadiff_fmt(1)}')
     E_3p = -3.02787 \pm 0.00185
     m = 3, lambda = 817.700 \pm 1.000, lambda_measured = 817.70, diff = 0.01
     m = 4, lambda = 569.353 \pm 0.485, lambda_measured = 567.10, diff = 2.03
     m = 5, lambda = 499.181 \pm 0.373, lambda_measured = 496.90, diff = 1.13
     m = 6, lambda = 467.857 \pm 0.327, lambda_measured = 469.20, diff = 1.28
     m = 7, lambda = 450.801 \pm 0.304, lambda_measured = 450.00, diff = 0.77
     m = 8, lambda = 440.381 \pm 0.290, lambda measured = 438.10, diff = 2.2
     m = 9, lambda = 433.510 \pm 0.281, lambda_measured = 432.60, diff = 0.88
     m = 10, lambda = 428.726 \pm 0.275, lambda_measured = 429.20, diff = 0.46
     m = 11, lambda = 425.254 \pm 0.270, lambda_measured = 426.00, diff = 0.72
     m = 12, lambda = 422.651 \pm 0.267, lambda_measured = 423.10, diff = 0.44
[36]: ## Erwartete Linien für die 2. Nebensetie: ms -> 3p
     E_3s = E_3p - (Consts.hc / ValErr(590.5, 1))
     Delta_s_val = 3 - np.sqrt(Consts.E_Ry / E_3s.val)
     Delta_s_{err} = (np.sqrt(np.abs(Consts.E_Ry)) / (2 * np.abs(E_3s.val) ** (3/2)))_{\sqcup}
       →* E_3s.err
     Delta_s = ValErr(Delta_s_val, Delta_s_err)
     print_all(E_3s.strfmtf(5,0, 'E_3s'), Delta_s.strfmtf(5,0, 'Delta s'))
     meas_2ns_vals = [
         622.34,
         517.5.
         474.0,
         454.4.
         445.3,
     ]
     meas_2ns_errs = np.ones(5)
     for m in range (4,10):
         1_val = Consts.hc / ((Consts.E_Ry / (m - Delta_s_val)**2) - E_3p.val)
         1_err = 1_val * np.sqrt(E_3p.relerr()**2 + (2*Delta_s.relerr())**2)
         1 = ValErr(l_val, l_err)
         if m == 4:
              print(f'm = \{m:2d\}, lambda = \{l.strfmtf(3,0)\}')
         else:
             print(f'm = {m:2d}, lambda = {l.strfmtf(3,0)}, lambda_measured = __
       →meas_2ns_errs[m-5]).sigmadiff_fmt(1)}')
```

 $E_3s = -5.12745 \pm 0.00401$

```
Delta s = 1.37108 \pm 0.00064
     m = 4, lambda = 1170.366 ± 1.302
     m = 5, lambda = 621.527 \pm 0.692, lambda measured = 622.34, diff = 0.67
     m = 6, lambda = 518.112 ± 0.577, lambda_measured = 517.50, diff = 0.53
     m = 7, lambda = 477.124 ± 0.531, lambda measured = 474.00, diff = 2.76
     m = 8, lambda = 456.100 ± 0.508, lambda_measured = 454.40, diff = 1.52
     m = 9, lambda = 443.719 \pm 0.494, lambda measured = 445.30, diff = 1.42
[37]: # Erwartete Linien für die Hauptserie: mp -> 3s
      Delta p val = 3 - np.sqrt(Consts.E Ry / E 3p.val)
      Delta_p = (np.sqrt(np.abs(Consts.E_Ry)) / (2 * np.abs(E_3p.val) ** (3/2)))_{\sqcup}
      →* E_3p.err
      Delta_p = ValErr(Delta_p_val, Delta_p_err)
      print_all(E_3s.strfmtf(5,0, 'E_3s'), Delta_p.strfmtf(5,0, 'Delta s'))
      for m in range (4,6):
          1_val = Consts.hc / ((Consts.E_Ry / (m - Delta_p_val)**2) - E_3s.val)
          l_err = l_val * np.sqrt(E_3s.relerr()**2 + (2*Delta_p.relerr())**2)
          1 = ValErr(l_val, l_err)
          print(f'm = \{m: 2d\}, lambda = \{l.strfmtf(3,0)\}')
     E_3s = -5.12745 \pm 0.00401
     Delta s = 0.88027 \pm 0.00065
     m = 4, lambda = 332.423 \pm 0.555
     m = 5, lambda = 286.603 \pm 0.478
[38]: # Bestimmung der Rydbergenergie, E 3p und Delta d für die 1. Nebenserie
      qz = np.arange(3,13)
      plt.figure(figsize=(16,10))
      plt.errorbar(qz, meas 1ns vals, meas 1ns errs, fmt='.', label='Gemessene',
       ⇒Wellenlängen der 1. Nebenserie')
      plt.xlabel('Quantenzahl')
      plt.ylabel('Wellenlaenge / nm')
      plt.title('1. Nebenserie des Na-Atoms')
      plt.xticks(qz)
      plt.grid()
      def fit_func_1ns(m, E_Ry, E_3p, D_d):
          return Consts.hc / ( E_Ry / (m-D_d)**2 - E_3p)
      start_params = [-13.6, -3, -0.02]
```

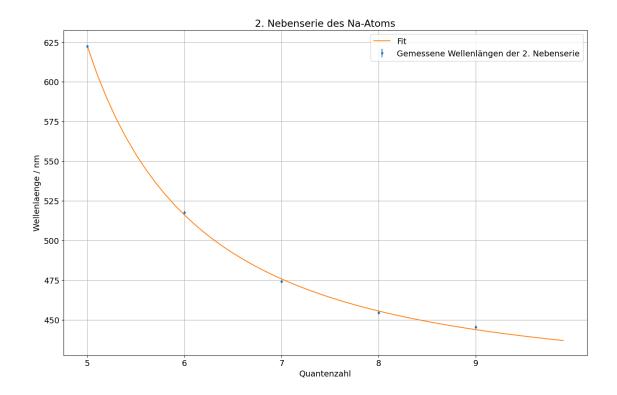
```
popt_1ns, pcov_1ns = curve_fit(fit_func_1ns, qz, meas_1ns_vals, sigma = u
 →meas_1ns_errs, p0 = start_params)
chi2_1ns = np.sum((fit_func_1ns(qz, *popt_1ns) - meas_1ns_vals)**2 /_
 →meas_1ns_errs**2)
dof_lns = len(qz) - 3 #dof:degrees of freedom, Freiheitsgrad
chi2_red_1ns = chi2_1ns / dof_1ns
print("chi2 = ", chi2_1ns)
print("chi2_red = ", chi2_red_1ns)
prob_1ns = round(1 - chi2.cdf(chi2_1ns, dof_1ns), 2) * 100
print("Wahrscheinlichkeit:", prob_1ns, "%")
plt.plot(np.arange(3,13, 0.1), fit_func_1ns(np.arange(3,13, 0.1), *popt_1ns),_
 ⇔label='Fit')
plt.legend()
plt.savefig("out/na_1ns_fit.png", format='png', bbox_inches='tight')
E_Ry_1ns = ValErr.fromFit(popt_1ns, pcov_1ns, 0)
E_3p_1ns = ValErr.fromFit(popt_1ns, pcov_1ns, 1)
D_d_1ns = ValErr.fromFit(popt_1ns, pcov_1ns, 2)
print_all(
    E_Ry_1ns.strfmtf(4, 0, 'E_Ry'),
    E_Ry_1ns.sigmadiff_fmt(ValErr(Consts.E_Ry, 0)),
    E_3p_1ns.strfmtf(4, 0, 'E_3p'),
    E_3p_1ns.sigmadiff_fmt(E_3p),
    D_d_1ns.strfmtf(4, 0, '\Delta_d'))
chi2 = 10.526902292499985
chi2\_red = 1.503843184642855
Wahrscheinlichkeit: 16.0 %
E Ry = -12.9778 \pm 0.4102
1.53
E_3p = -3.0233 \pm 0.0059
0.75
\Delta_d = 0.0655 \pm 0.0419
```



```
[39]: # Bestimmung der Rydbergenergie, E_3p und Delta_d für die 2. Nebenserie
      qz = np.arange(5,10)
      plt.figure(figsize=(16,10))
     plt.errorbar(qz, meas_2ns_vals, meas_2ns_errs, fmt='.', label='Gemessene_
       ⇒Wellenlängen der 2. Nebenserie')
      plt.xlabel('Quantenzahl')
      plt.ylabel('Wellenlaenge / nm')
      plt.title('2. Nebenserie des Na-Atoms')
      plt.xticks(qz)
      plt.grid()
      def fit_func_2ns(m, E_Ry, E_3p, D_s):
          return Consts.hc / (E_Ry / (m-D_s)**2 - E_3p)
      start_params = [-13.6, -3, 1.5]
      popt_2ns, pcov_2ns = curve_fit(fit_func_2ns, qz, meas_2ns_vals, sigma =_

meas_2ns_errs, p0 = start_params)
      chi2_2ns = np.sum((fit_func_2ns(qz, *popt_2ns) - meas_2ns_vals)**2 /_
       ⊶meas_2ns_errs**2)
```

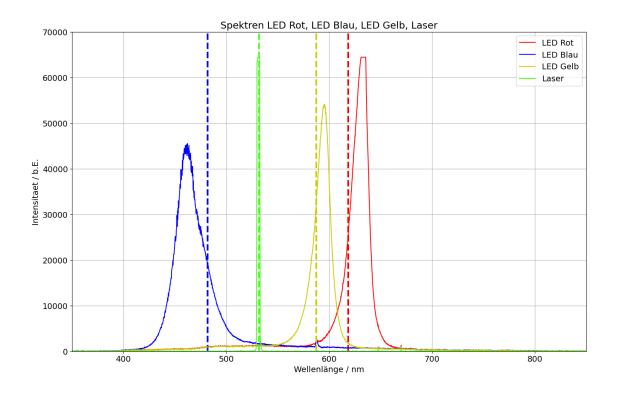
```
dof_2ns = len(qz) - 3 #dof:degrees of freedom, Freiheitsgrad
chi2_red_2ns = chi2_2ns / dof_2ns
print("chi2 = ", chi2_2ns)
print("chi2_red = ", chi2_red_2ns)
prob_2ns = round(1 - chi2.cdf(chi2_2ns, dof_2ns), 2) * 100
print("Wahrscheinlichkeit:", prob_2ns, "%")
plt.plot(np.arange(5,10, 0.1), fit_func_2ns(np.arange(5,10, 0.1), *popt_2ns),__
  →label='Fit')
plt.legend()
plt.savefig("out/na_2ns_fit.png", format='png', bbox_inches='tight')
E_Ry_2ns = ValErr.fromFit(popt_2ns, pcov_2ns, 0)
E_3p_2ns = ValErr.fromFit(popt_2ns, pcov_2ns, 1)
D_s_2ns = ValErr.fromFit(popt_2ns, pcov_2ns, 2)
print_all(
    E_Ry_2ns.strfmtf(4, 0, 'E_Ry'),
    E_Ry_2ns.sigmadiff_fmt(ValErr(Consts.E_Ry, 0)),
    E_3p_2ns.strfmtf(4, 0, 'E_3p'),
    E_3p_2ns.sigmadiff_fmt(E_3p),
    D_s_2ns.strfmtf(4, 0, '\Delta_s'),
    D_s_2ns.sigmadiff_fmt(Delta_s))
chi2 = 8.553390527826295
chi2\_red = 4.2766952639131475
Wahrscheinlichkeit: 1.0 %
E Ry = -11.5866 \pm 2.0081
1.01
E_{3p} = -3.0068 \pm 0.0313
0.68
\Delta_s = 1.6217 \pm 0.2454
1.03
```

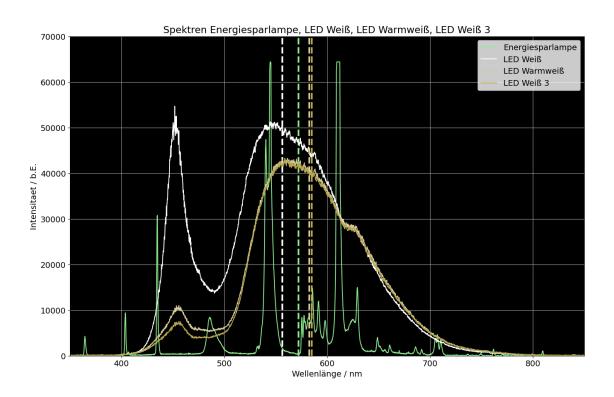


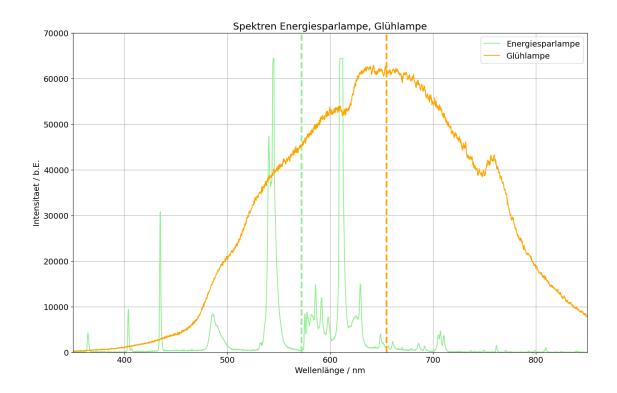
0.0.3 LED Spektren

```
[40]: all_spectra = [
          ('LED Weiß', 'spektrum_led_weiss.txt', 'white'),
          ('LED Warmweiß', 'spektrum_led_warmweiss.txt', '#d6cb9a'),
          ('LED Weiß 3', 'spektrum_led_weiss3.txt', '#b8a651'),
          ('LED Rot', 'spektrum_led_rot.txt', 'red'),
          ('LED Blau', 'spektrum_led_blau.txt', 'blue'),
          ('LED Gelb', 'spektrum_led_gelb.txt', '#cccc00'),
          ('LED Orange', 'spektrum_led_orange.txt', 'orange'),
          ('Energiesparlampe', 'energiesparlampe.txt', 'lightgreen'),
          ('Glühlampe', 'gluehlampe.txt', 'orange'),
          ('Laser', 'laser.txt', '#47fb18'),
      ]
      def draw_spectra(spectra):
          plt.figure(figsize=(16,10))
          for spec in spectra:
              spec_lam, spec_int = np.loadtxt(spec[1], skiprows=17,
                                          converters= {0:comma_to_float, 1:
       ⇔comma_to_float},
                                          comments='>', unpack=True)
```

```
plt.plot(spec_lam, spec_int, color=spec[2], label=spec[0])
       wavelen_sum = 0
       inten_sum = 0
       for si in zip(spec_lam, spec_int):
            if si[1] > 0:
                wavelen_sum = wavelen_sum + si[0] * si[1]
                inten_sum = inten_sum + si[1]
       wavelen_mean = wavelen_sum / inten_sum
       plt.axvline(x=wavelen_mean, linewidth=3, linestyle='--', color=spec[2])
   plt.title('Spektren ' + ', '.join([s[0] for s in spectra]))
   plt.xlabel('Wellenlänge / nm')
   plt.ylabel('Intensitaet / b.E.')
   plt.legend()
   plt.grid()
   plt.ylim((0,70000))
   plt.xlim((350,850))
draw_spectra(all_spectra[3:6] + all_spectra[9:10])
plt.savefig('out/led_vergleich.png', format='png', bbox_inches='tight')
draw_spectra(all_spectra[7:8] + all_spectra[0:3])
ax = plt.gca()
ax.set_facecolor('black')
plt.savefig('out/led_und_energiespar.png', format='png', bbox_inches='tight')
draw_spectra(all_spectra[7:9])
plt.savefig('out/energiespar_und_glueh.png', format='png', bbox_inches='tight')
```







[]: