

255auswertung

April 9, 2025

```
[37]: import matplotlib.pyplot as plt
import matplotlib.patches as mpatches
import numpy as np
from scipy.signal import argrelextrema
from scipy.optimize import curve_fit
from scipy.stats import chi2
```

```
plt.rcParams.update({'font.size': 18})
```

```
%run ../lib.ipynb
```

```
LibFormatter.OutputType = 'latex'
```

```
class Consts:
```

```
    hc = 1.2398 * 10**(3) #nm eV
```

```
    E_Ry = -13.605 # eV
```

```
    E_inf = 3.2898 * 10**(15) # Hz
```

```
    c = 2.9979 * 10**(8) # m/s
```

```
    e = 1.6022 * 10**(-19) # C
```

```
    h = 6.6261 * 10**(-34) # Js
```

```
    N_A = 6.0221 * 10**(23)
```

```
[38]: def comma_to_float(valstr):
return float(valstr.replace(',', '.'))
```

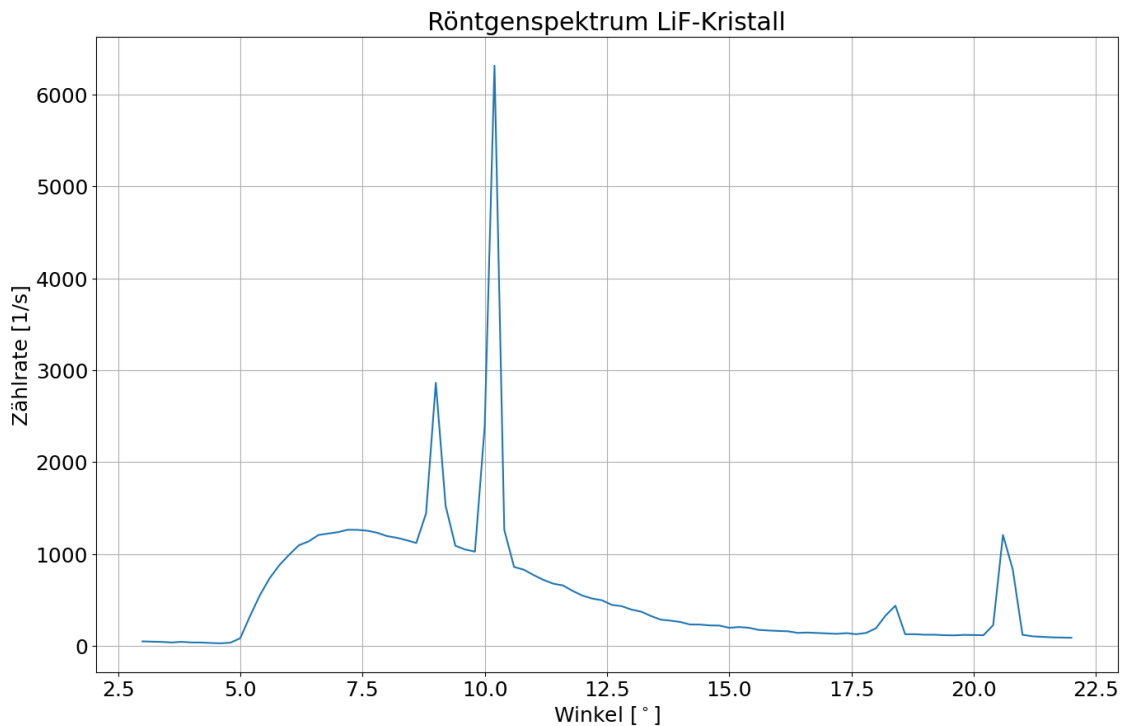
```
def countrate_error(ctrt, t):
return [np.sqrt(x*t) / t for x in ctrt]
```

```
[39]: # fit functions
def gauss_func(x, A, mu, sig, c):
return A/(np.sqrt(2 * np.pi)*sig)*np.exp(-(x-mu)**2 / (2 * sig**2)) + c

def linear_func(x, a, b):
return a * x + b
```

```
[40]: lif_ang, lif_countrate = np.loadtxt('aufgabe1.txt', skiprows=0,
converters= {0:comma_to_float, 1:comma_to_float},
comments='>', unpack=True)
```

```
[41]: plt.figure(figsize=(16,10))
plt.plot(lif_ang, lif_countrate)
plt.title('Röntgenspektrum LiF-Kristall')
plt.xlabel(r'Winkel [ $^{\circ}$ ]')
plt.ylabel(r'Zählrate [1/s]')
plt.grid()
plt.savefig('out/spektrum_lif_komplett.png', format='png', bbox_inches='tight')
```



0.0.1 Aufgabe 1

```
[42]: plt.figure(figsize=(16,10))

lowlim = 10
uplim = 17

lif_countrate_errs = countrate_error(lif_countrate[lowlim:uplim], 5)

plt.errorbar(lif_ang[lowlim:uplim], lif_countrate[lowlim:uplim],
             yerr=lif_countrate_errs)
plt.title('Röntgenspektrum LiF - Fit an kurzwelliges Ende')
plt.xlabel(r'Winkel [ $^{\circ}$ ]')
plt.ylabel(r'Zählrate [1/s]')
#plt.ylim((0,3000))
```

```

plt.grid()

start_params = [0, 0]
popt_lif_lgrenz_lin, pcov_lif_lgrenz_lin = curve_fit(linear_func,
    ↳lif_ang[lowlim:uplim], lif_countrate[lowlim:uplim], sigma =
    ↳lif_countrate_errs, p0 = start_params)
lif_lin_a = ValErr.fromFit(popt_lif_lgrenz_lin, pcov_lif_lgrenz_lin, 0)
lif_lin_b = ValErr.fromFit(popt_lif_lgrenz_lin, pcov_lif_lgrenz_lin, 1)

#  $0 = a x + b \Leftrightarrow x = -b/a$ 
lif_lin_nullst = (-1) * (lif_lin_b / lif_lin_a)

plt.plot(lif_ang[lowlim:uplim], linear_func(lif_ang[lowlim:uplim],
    ↳*popt_lif_lgrenz_lin))
plt.savefig('out/spektrum_lif_linear_fit.png', format='png',
    ↳bbox_inches='tight')

plt.figure(figsize=(16,10))
plt.plot(lif_ang, lif_countrate)
plt.plot(lif_ang[lowlim-4:uplim+4], linear_func(lif_ang[lowlim-4:uplim+4],
    ↳*popt_lif_lgrenz_lin))
plt.axvline(x=lif_lin_nullst.val, linewidth=2, linestyle='--', color='green')
plt.axvline(x=lif_lin_nullst.val+lif_lin_nullst.err, linewidth=1,
    ↳linestyle='--', color='#56b300')
plt.axvline(x=lif_lin_nullst.val-lif_lin_nullst.err, linewidth=1,
    ↳linestyle='--', color='#56b300')
plt.ylim((-100,3000))
plt.xlim((2.5,10))
plt.xlabel(r'Winkel [ $^\circ$ ]')
plt.ylabel(r'Zählrate [1/s]')
plt.grid()

plt.savefig('out/spektrum_lif_linear_fit_wide.png', format='png',
    ↳bbox_inches='tight')

#  $2d \sin(\theta) = n \lambda \Leftrightarrow \lambda = 2d \sin(\theta) / n$  ( $n = 1$ )
#  $\theta = \arcsin(n \lambda / 2 d)$ 

lif_d = 201.4 * 10**(-12)

lif_lam_grenz_val = 2 * lif_d * np.sin(np.deg2rad(lif_lin_nullst.val))
lif_lam_grenz_err = 2 * lif_d * np.cos(np.deg2rad(lif_lin_nullst.val)) * np.
    ↳deg2rad(lif_lin_nullst.err)
lif_lam_grenz = ValErr(lif_lam_grenz_val, lif_lam_grenz_err)

```

```

#  $l_{\text{grenz}} = hc / Ue \Leftrightarrow h = l_{\text{grenz}} U e / c$ 
U_a1 = 35 * 10**3
h_a1 = lif_lam_grenz * (U_a1 * Consts.e / Consts.c)

#  $\theta(n=2) = \arcsin(\lambda/d)$ 

lif_ang_2ord_val = np.rad2deg(np.arcsin(lif_lam_grenz.val / lif_d))
lif_ang_2ord_err = (lif_lam_grenz.err / lif_d) * (1 / np.sqrt(1 - (lif_lam_grenz.val**2/lif_d**2)))
lif_ang_2ord = ValErr(lif_ang_2ord_val, lif_ang_2ord_err)

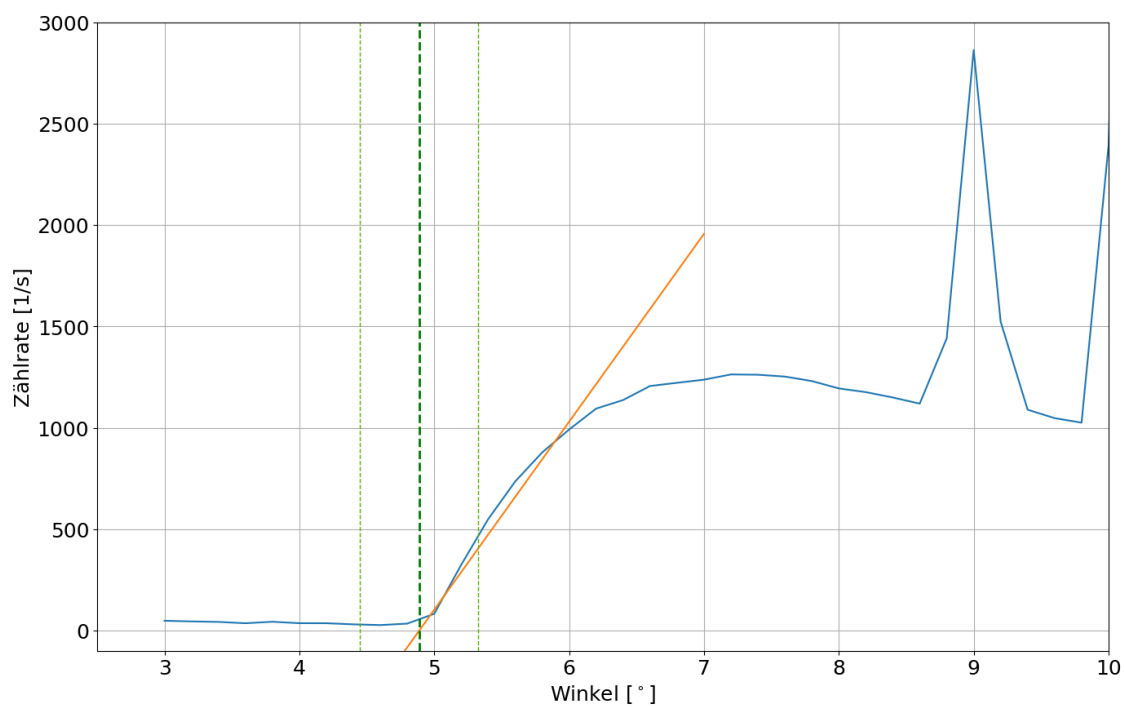
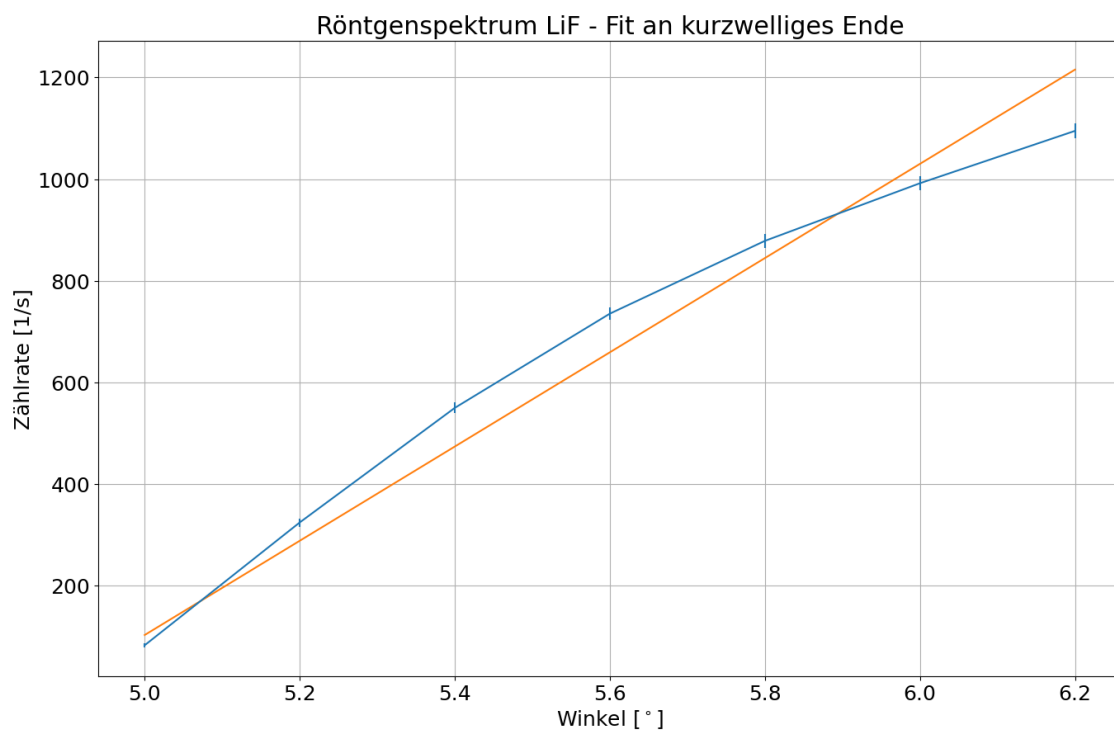
print_all(
    lif_lin_a,
    lif_lin_b,
    lif_lin_nullst.strfmtf2(6, 0, 'beta'),
    lif_lam_grenz.strfmtf2(6, -12, ' _grenz'),
    h_a1.strfmtf2(6, -34, ' h'),
    h_a1.sigmadiff_fmt(ValErr(Consts.h, 0)),
    lif_ang_2ord.strfmtf2(6, 0, ' beta, 2. ord'))

```

```

ValErr(926.9388981212614, 56.62078398042604)
ValErr(-4531.531907160432, 297.4967190001228)
beta = 4.888706 \pm 0.438383
_grenz = (34.326828 \pm 3.070703) \cdot 10^{-12}
h = (6.420980 \pm 0.574388) \cdot 10^{-34}
0.36
beta, 2. ord = 9.813464 \pm 0.015473

```



0.0.2 Aufgabe 2

```
[43]: lif_kalph1_ang, lif_kalph1_countrate = np.loadtxt('aufgabe2/kalpha1.txt',  
↳ skiprows=0,  
        converters= {0:comma_to_float, 1:comma_to_float},  
        comments='>', unpack=True)  
  
lif_kbeta1_ang, lif_kbeta1_countrate = np.loadtxt('aufgabe2/kbeta1.txt',  
↳ skiprows=0,  
        converters= {0:comma_to_float, 1:comma_to_float},  
        comments='>', unpack=True)  
  
lif_kalph2_ang, lif_kalph2_countrate = np.loadtxt('aufgabe2/kalpha2.txt',  
↳ skiprows=0,  
        converters= {0:comma_to_float, 1:comma_to_float},  
        comments='>', unpack=True)  
  
lif_kbeta2_ang, lif_kbeta2_countrate = np.loadtxt('aufgabe2/kbeta2.txt',  
↳ skiprows=0,  
        converters= {0:comma_to_float, 1:comma_to_float},  
        comments='>', unpack=True)  
  
def find_peak(peak_ang, peak_countrate, peak_order, offset, title, fname):  
    pf_lowlim = 0 + offset  
    pf_uplim = len(peak_ang) - offset  
  
    peak_countrate_errs = countrate_error(peak_countrate[pf_lowlim:pf_uplim],  
↳ 20)  
  
    plt.figure(figsize=(16,10))  
    plt.errorbar(peak_ang[pf_lowlim:pf_uplim], peak_countrate[pf_lowlim:  
↳ pf_uplim], yerr=peak_countrate_errs)  
    plt.title(title)  
    plt.xlabel(r'Winkel [ $^\circ$ '])  
    plt.ylabel(r'Zählrate [1/s]')  
    plt.grid()  
  
    start_params = [500, np.mean(peak_ang[pf_lowlim:pf_uplim]), np.  
↳ std(peak_ang[pf_lowlim:pf_uplim]), np.min(peak_countrate[pf_lowlim:  
↳ pf_uplim])]  
    #print(start_params)  
  
    popt_peak, pcov_peak = curve_fit(  
        gauss_func,  
        peak_ang[pf_lowlim:pf_uplim],  
        peak_countrate[pf_lowlim:pf_uplim],  
        sigma = peak_countrate_errs,
```

```

p0 = start_params)

peak_A = ValErr.fromFit(popt_peak, pcov_peak, 0)
peak_mu = ValErr.fromFit(popt_peak, pcov_peak, 1)
peak_sig = ValErr.fromFit(popt_peak, pcov_peak, 2)
peak_c = ValErr.fromFit(popt_peak, pcov_peak, 3)

peak_fwhm = 2 * np.sqrt(2 * np.log(2)) * peak_sig

print(peak_fwhm.val, peak_fwhm.val / 2, peak_sig.val, peak_sig.val / np.
↪sqrt(len(peak_ang[pf_lowlim:pf_uplim])))

angle_err = peak_sig.val / np.sqrt(len(peak_ang[pf_lowlim:pf_uplim]))

contin_angle = np.arange(peak_ang[pf_lowlim], peak_ang[pf_uplim-1], 0.01)
plt.plot(contin_angle, gauss_func(contin_angle, *popt_peak))
#plt.axvline(x=peak_mu.val, linewidth=2, linestyle='--', color='green')
#plt.axvline(x=peak_mu.val + angle_err, linewidth=1, linestyle='--', ↪
↪color='#56b300')
#plt.axvline(x=peak_mu.val - angle_err, linewidth=1, linestyle='--', ↪
↪color='#56b300')

plt.savefig(f'out/{fname}.png', format='png', bbox_inches='tight')

peak_lam_val = (2 * 201.4 * 10**(-12) / peak_order) * np.sin(np.
↪deg2rad(peak_mu.val))
peak_lam_err = (2 * 201.4 * 10**(-12) / peak_order) * np.cos(np.
↪deg2rad(peak_mu.val)) * np.deg2rad(angle_err)
peak_lam = ValErr(peak_lam_val, peak_lam_err)

print_all(title,
          peak_A.strfmtf(4, 0, 'A'),
          peak_mu.strfmtf(4, 0, ' '),
          peak_sig.strfmtf(4, 0, ' '),
          peak_fwhm.strfmtf(4, 0, 'fwhm'),
          peak_lam.strfmtf2(6, -12, ' '),
          '')

return (peak_A, peak_mu, peak_sig, peak_c, peak_lam)

peak_dat_kalpha1 = find_peak(lif_kalph1_ang, lif_kalph1_countrate, 1, 1, ↪
↪r'Röntgenspektrum (LiF), $K_{\alpha}$-Linie 1. Ordnung', 'lif_kalpha_1ord')
peak_dat_kbeta1 = find_peak(lif_kbeta1_ang, lif_kbeta1_countrate, 1, 1, ↪
↪r'Röntgenspektrum (LiF), $K_{\beta}$-Linie 1. Ordnung', 'lif_kbeta_1ord')

```

```

peak_dat_kalpha2 = find_peak(lif_kalph2_ang, lif_kalph2_countrate, 2, 0,
    ↳r'Röntgenspektrum (LiF), $K_{\alpha}$-Linie 2. Ordnung', 'lif_kalpha_2ord')
peak_dat_kbeta2 = find_peak(lif_kbeta2_ang, lif_kbeta2_countrate, 2, 0,
    ↳r'Röntgenspektrum (LiF), $K_{\beta}$-Linie 2. Ordnung', 'lif_kbeta_2ord')

kalpha_mean_lit = ValErr(71.1 * 10**(-12))
kbeta_mean_lit = ValErr(63.1 * 10**(-12))

kalpha_mean = (peak_dat_kalpha1[4] + peak_dat_kalpha2[4]) / 2
kbeta_mean = (peak_dat_kbeta1[4] + peak_dat_kbeta2[4]) / 2

print_all('Mittelwerte', kalpha_mean.strfmtf2(6, -12, ' K_ '), kalpha_mean.
    ↳sigmadiff_fmt(kalpha_mean_lit), kbeta_mean.strfmtf2(6, -12, ' K_ '),
    ↳kbeta_mean.sigmadiff_fmt(kbeta_mean_lit))

```

0.2449426466010601 0.12247132330053005 0.1040175647892622 0.0268572197427909

Röntgenspektrum (LiF), \$K_{\alpha}\$-Linie 1. Ordnung

A = 1417.9660 \pm 64.8681

= 10.1912 \pm 0.0049

= 0.1040 \pm 0.0045

fwhm = 0.2449 \pm 0.0105

= (71.268530 \pm 0.185832) \cdot 10^{-12}

0.2598405224074471 0.12992026120372355 0.11034411013943615 0.03678137004647872

Röntgenspektrum (LiF), \$K_{\beta}\$-Linie 1. Ordnung

A = 503.0489 \pm 37.1957

= 9.0377 \pm 0.0064

= 0.1103 \pm 0.0075

fwhm = 0.2598 \pm 0.0176

= (63.273447 \pm 0.255370) \cdot 10^{-12}

0.29438118966863097 0.14719059483431549 0.12501218099014522 0.03608790817332128

Röntgenspektrum (LiF), \$K_{\alpha}\$-Linie 2. Ordnung

A = 390.5916 \pm 10.7041

= 20.6648 \pm 0.0033

= 0.1250 \pm 0.0031

fwhm = 0.2944 \pm 0.0074

= (71.074234 \pm 0.118691) \cdot 10^{-12}

0.2556687909958171 0.12783439549790854 0.10857253892301431 0.028033309006952733

Röntgenspektrum (LiF), \$K_{\beta}\$-Linie 2. Ordnung

A = 93.8456 \pm 9.1049

= 18.3110 \pm 0.0106

= 0.1086 \pm 0.0104

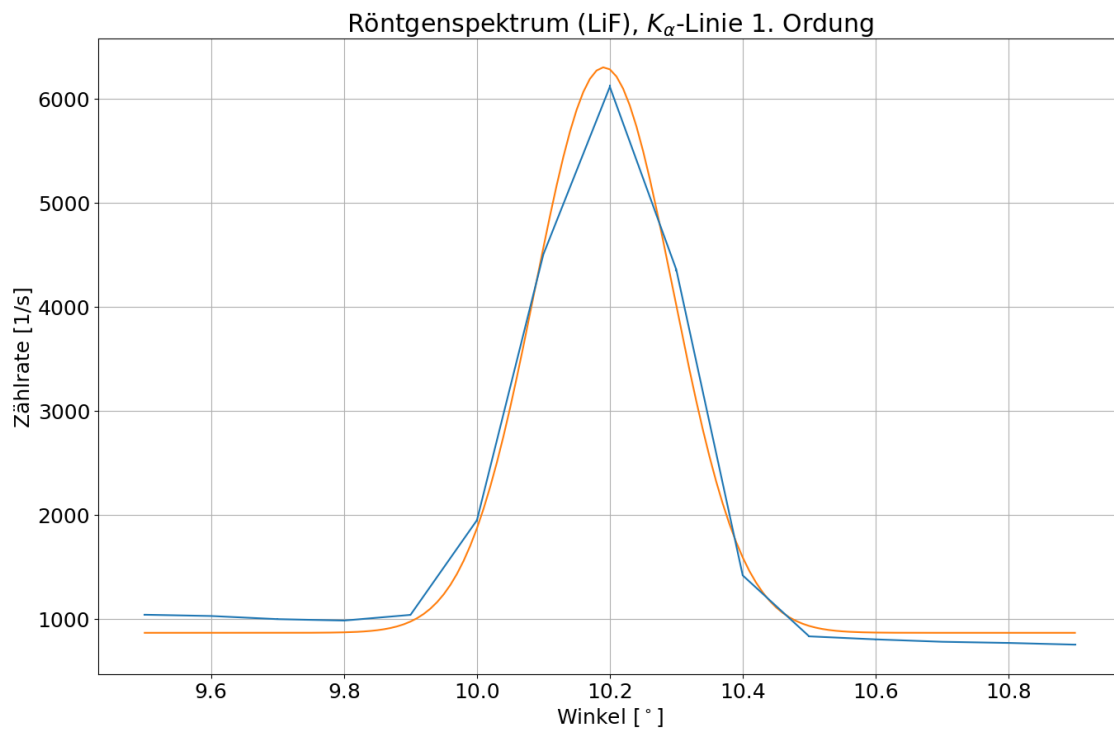
fwhm = 0.2557 \pm 0.0246

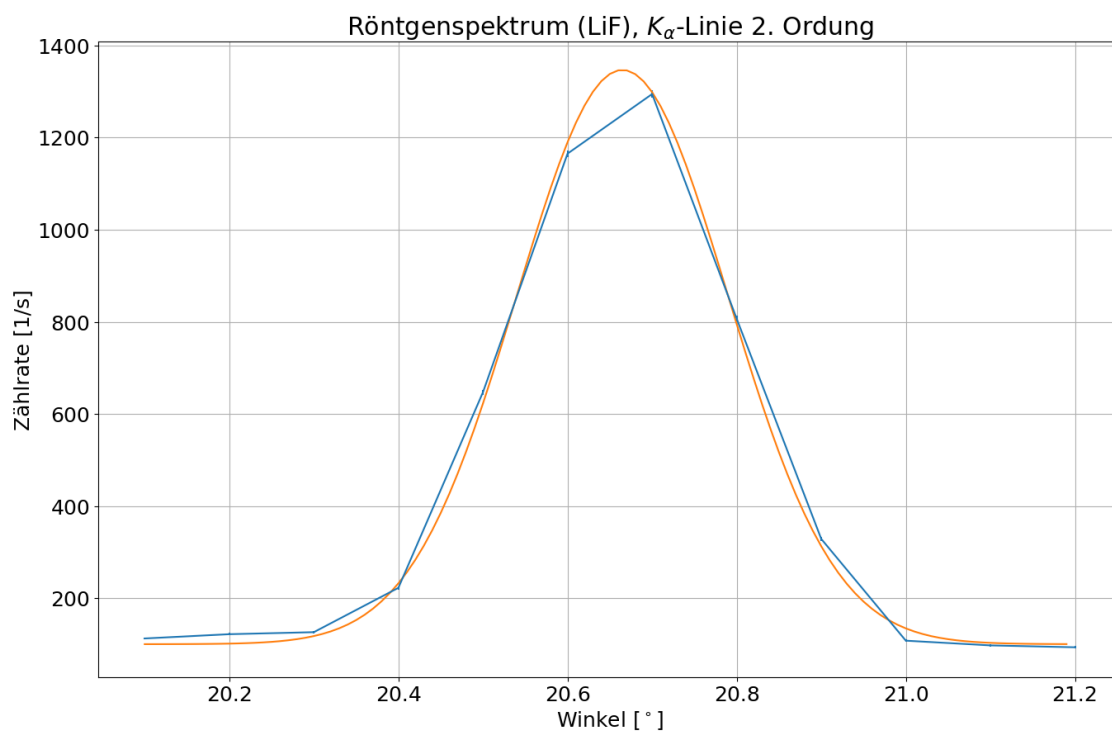
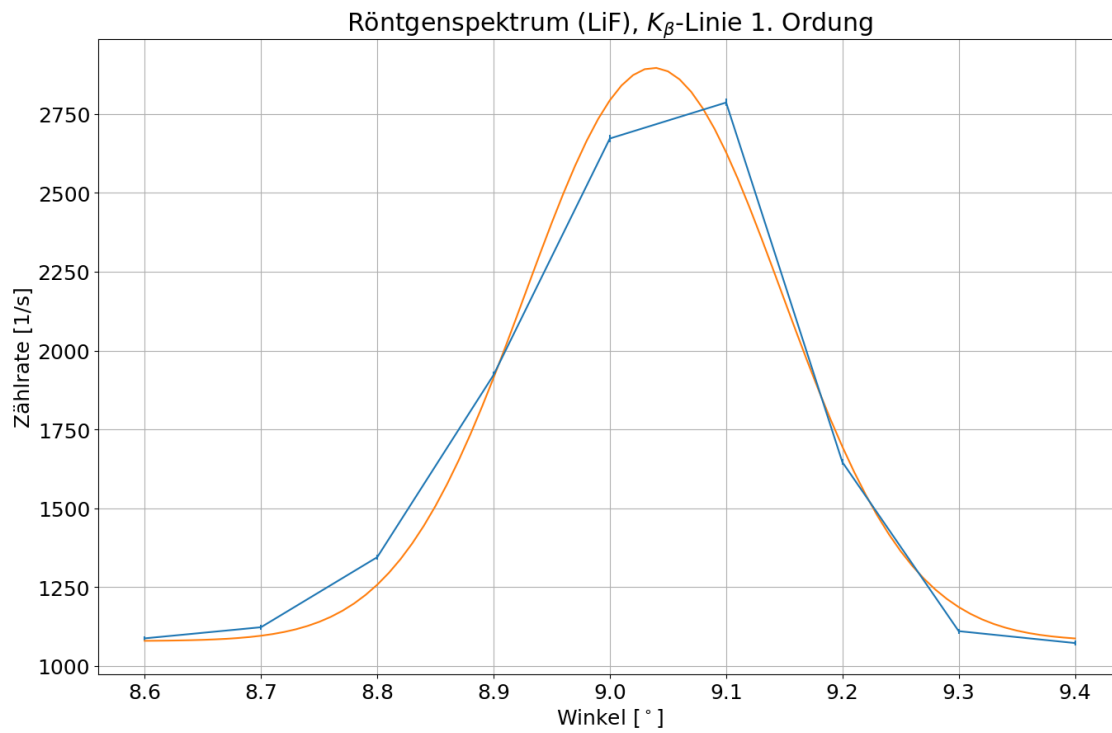
= (63.274851 \pm 0.093550) \cdot 10^{-12}

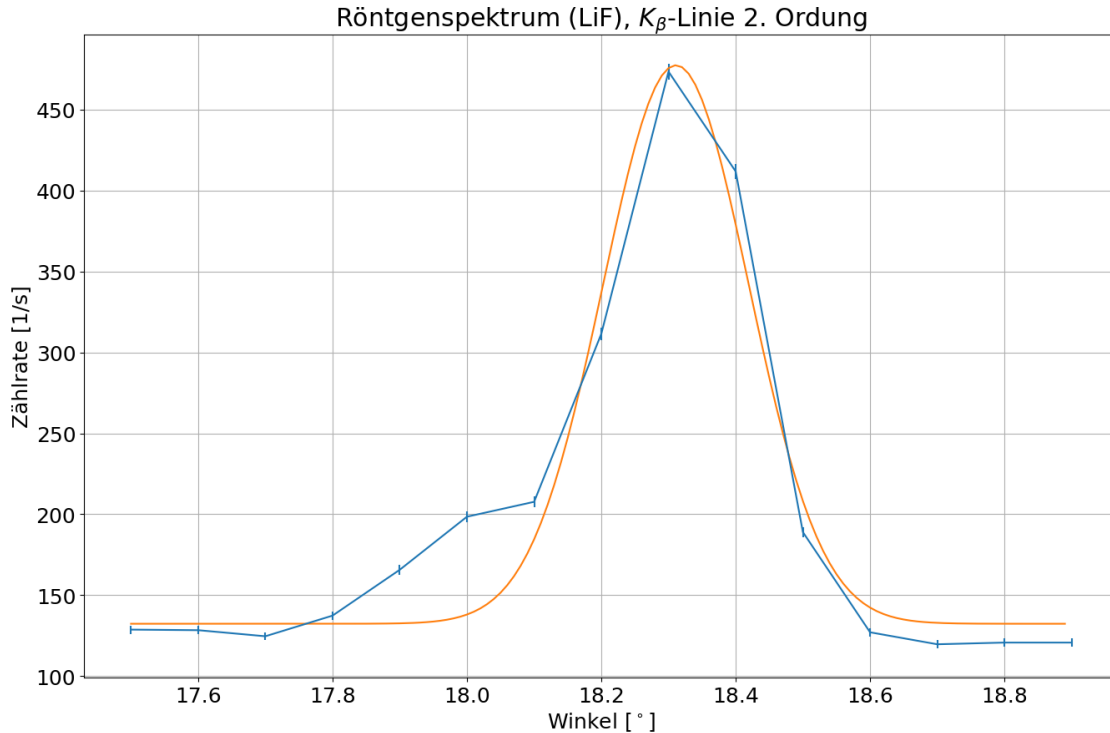
Mittelwerte

$K_- = (71.171382 \pm 0.110251) \cdot 10^{-12}$
0.65

$K_+ = (63.274149 \pm 0.135983) \cdot 10^{-12}$
1.29







0.0.3 Aufgabe 3

```
[44]: lif_ang75_volt, lif_ang75_countrate = np.loadtxt('aufgabe3.txt', skiprows=0,
           converters= {0:comma_to_float, 1:comma_to_float},
           comments='>', unpack=True)
```

```
[45]: lowlim_einsp = 3
      uplin_einsp = len(lif_ang75_volt)

      lif_ang75_countrate_errs = countrate_error(lif_ang75_countrate, 20)

      plt.figure(figsize=(16,10))
      plt.errorbar(lif_ang75_volt, lif_ang75_countrate, yerr=lif_ang75_countrate_errs)
      #plt.title(title)
      plt.xlabel(r'Spannung [kV]')
      plt.ylabel(r'Zählrate [1/s]')
      plt.grid()

      start_params = [0, 0]
      popt_lif_einsp, pcov_lif_einsp = curve_fit(
          linear_func,
          lif_ang75_volt[lowlim_einsp:uplin_einsp],
          lif_ang75_countrate[lowlim_einsp:uplin_einsp],
```

```

sigma = lif_ang75_countrate_errs[lowlim_einsp:uplin_einsp],
p0 = start_params)

lif_einsp_a = ValErr.fromFit(popt_lif_einsp, pcov_lif_einsp, 0)
lif_einsp_b = ValErr.fromFit(popt_lif_einsp, pcov_lif_einsp, 1)

plt.plot(lif_ang75_volt, linear_func(lif_ang75_volt, *popt_lif_einsp))

#  $0 = a x + b \Leftrightarrow x = -b/a$ 
lif_einsp_nullst = (-1) * (lif_einsp_b / lif_einsp_a)

plt.axvline(x=lif_einsp_nullst.val, linewidth=2, linestyle='--', color='green')
plt.axvline(x=lif_einsp_nullst.val+lif_einsp_nullst.err, linewidth=1,
    ↪linestyle='--', color='#56b300')
plt.axvline(x=lif_einsp_nullst.val-lif_einsp_nullst.err, linewidth=1,
    ↪linestyle='--', color='#56b300')

plt.savefig(f'out/lif_ang75_volt_fit.png', format='png', bbox_inches='tight')

#  $2d \sin(\theta) = n \lambda \Leftrightarrow \lambda = 2d \sin(\theta) / n \ (n = 1)$ 

lif_einsp_lam_val = 2 * 201.4 * 10**(-12) * np.sin(np.deg2rad(7.5))
lif_einsp_lam_err = 2 * 201.4 * 10**(-12) * np.cos(np.deg2rad(7.5)) * np.
    ↪deg2rad(0.05)
lif_einsp_lam = ValErr(lif_einsp_lam_val, lif_einsp_lam_err)

#  $l_{\text{grenz}} = hc / Ue \Leftrightarrow h = l_{\text{grenz}} U e / c$ 
U_a3 = lif_einsp_nullst * 10**3
h_a3 = lif_einsp_lam * (U_a3 * Consts.e / Consts.c)

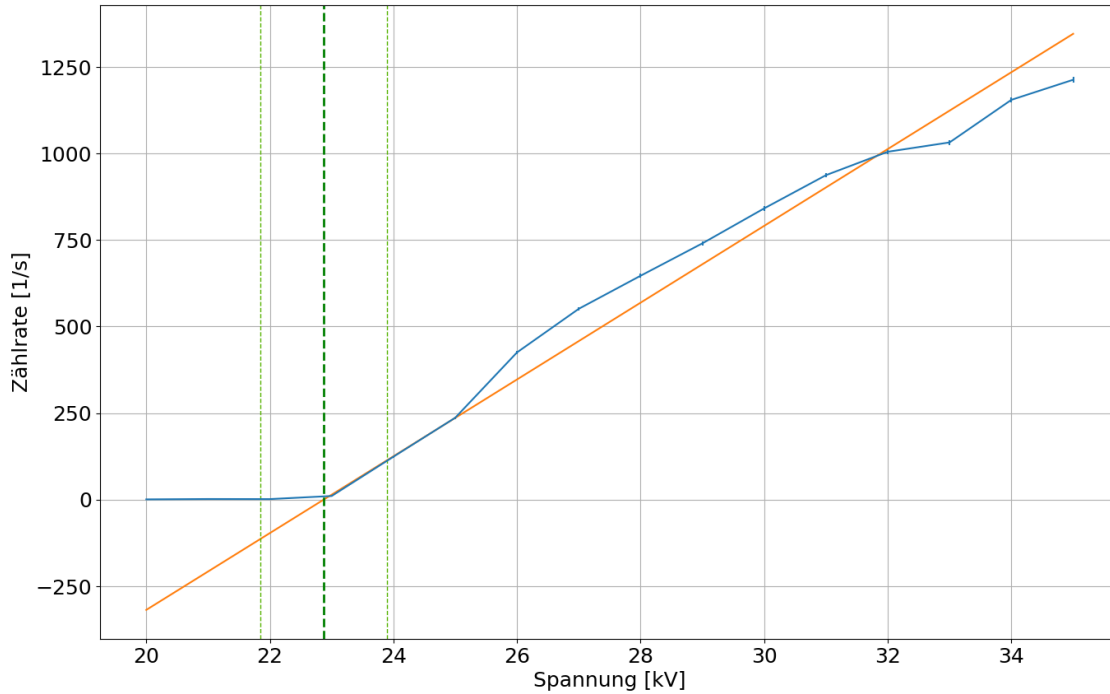
print_all(lif_einsp_a,
          lif_einsp_b,
          lif_einsp_nullst.strfmtf2(6, 0, 'U'),
          lif_einsp_lam.strfmtf2(6, -12, ' '),
          h_a3.strfmtf2(6, -34, 'h'),
          h_a3.sigmadiff_fmt(ValErr(Consts.h, 0)))

```

```

ValErr(110.96963341748018, 3.434413817817252)
ValErr(-2538.133262327901, 82.21087923807104)
U = 22.872323 \pm 1.024665
  = (52.575950 \pm 0.348502) \cdot 10^{-12}
h = (6.426833 \pm 0.291052) \cdot 10^{-34}
0.69

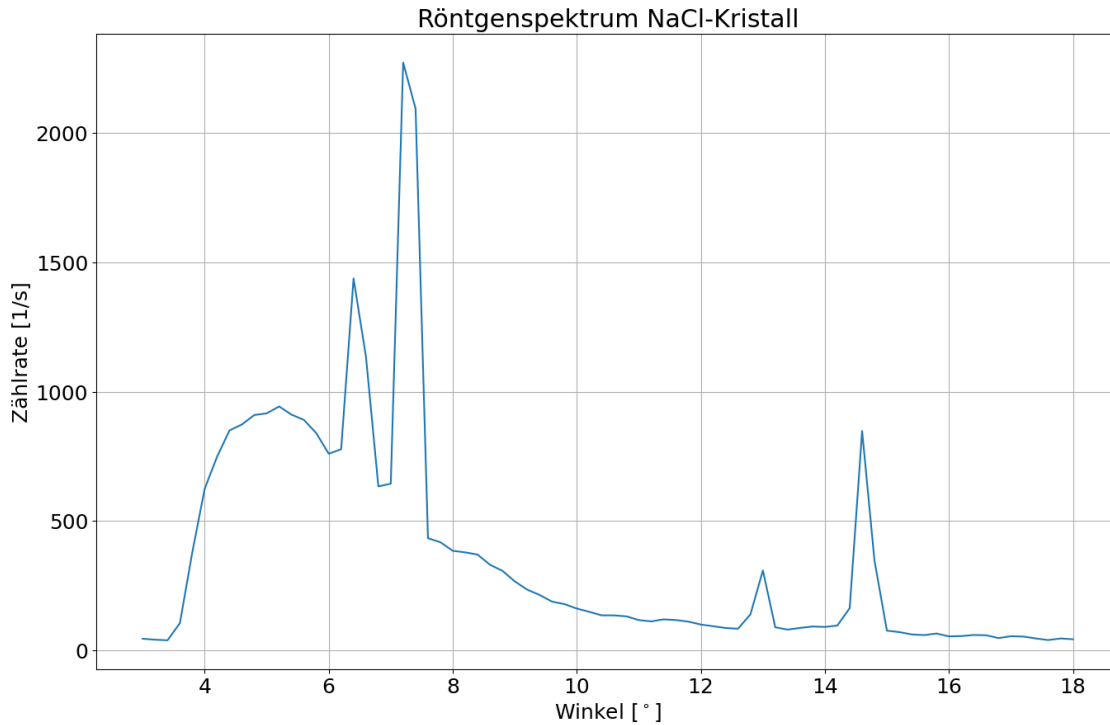
```



0.0.4 Aufgabe 4

```
[46]: nacl_ang, nacl_countrate = np.loadtxt('aufgabe4.txt', skiprows=0,
                                             converters= {0:comma_to_float, 1:comma_to_float},
                                             comments='>', unpack=True)

plt.figure(figsize=(16,10))
plt.plot(nacl_ang, nacl_countrate)
plt.title(r'Röntgenspektrum NaCl-Kristall')
plt.xlabel(r'Winkel [$^\circ$'])
plt.ylabel(r'Zählrate [1/s]')
plt.grid()
plt.savefig('out/spektrum_nacl_komplett.png', format='png', bbox_inches='tight')
```



```
[47]: nacl_lowlim = 15
nacl_uplim = 25

plt.figure(figsize=(16,10))
plt.plot(nacl_ang[nacl_lowlim:nacl_uplim], nacl_countrate[nacl_lowlim:
    ↪nacl_uplim])
plt.title(r'Röntgenspektrum NaCl, $K_{\beta}$, $K_{\alpha}$ 1. Ordnung')
plt.xlabel(r'Winkel [$^{\circ}$'])
plt.ylabel(r'Zählrate [1/s]')
plt.xticks(np.arange(nacl_ang[nacl_lowlim], nacl_ang[nacl_uplim-1], 0.1))
plt.grid()
#plt.savefig('out/himmel_m_o_g.png', format='png', bbox_inches='tight')

def find_nacl_peak(nacl_peak_low, nacl_peak_up):

    peak_countrate_errs = countrate_error(nacl_countrate[nacl_peak_low:
    ↪nacl_peak_up], 5)

    start_params = [500, np.mean(nacl_ang[nacl_peak_low:nacl_peak_up]), np.
    ↪std(nacl_ang[nacl_peak_low:nacl_peak_up]), 500]

    popt_nacl_k_peak, pcov_nacl_k_peak = curve_fit(
        gauss_func,
```

```

    nacl_ang[nacl_peak_low:nacl_peak_up],
    nacl_countrate[nacl_peak_low:nacl_peak_up],
    sigma=peak_countrate_errs,
    p0 = start_params)

    contin_angle = np.arange(nacl_ang[nacl_peak_low], nacl_ang[nacl_peak_up-1],
↪0.01)
    plt.plot(contin_angle, gauss_func(contin_angle, *popt_nacl_k_peak))

    peak_mu = ValErr.fromFit(popt_nacl_k_peak, pcov_nacl_k_peak, 1)
    peak_sig = ValErr.fromFit(popt_nacl_k_peak, pcov_nacl_k_peak, 2)

    angle_err = peak_sig.val / np.sqrt(len(nacl_ang[nacl_peak_low:
↪nacl_peak_up]))
    #plt.axvline(x=peak_mu.val, linewidth=2, linestyle='--', color='green')
    #plt.axvline(x=peak_mu.val + angle_err, linewidth=1, linestyle='--',
↪color='#56b300')
    #plt.axvline(x=peak_mu.val - angle_err, linewidth=1, linestyle='--',
↪color='#56b300')

    return ValErr(peak_mu.val, angle_err)

nacl_kbeta1_angle = find_nacl_peak(15, 21)
nacl_kalpha1_angle = find_nacl_peak(19, 25)

plt.savefig(f'out/nacl_k_lord_fit.png', format='png', bbox_inches='tight')

#  $2d \sin(\theta) = n \lambda \Rightarrow d = n \lambda / 2 \sin(\theta)$ 

def calc_d(lam, ang):
    lam_val = lam.val
    lam_err = lam.err

    ang_val = np.deg2rad(ang.val)
    ang_err = np.deg2rad(ang.err)

    sin_ang_val = np.sin(ang_val)
    cos_ang_val = np.cos(ang_val)

    d_val = (1/2) * (lam_val / sin_ang_val)
    d_err = (1/2) * np.sqrt((lam_err / sin_ang_val) ** 2 + ((lam_val *
↪cos_ang_val * ang_err) / sin_ang_val ** 2) ** 2)
    return ValErr(d_val, d_err)

nacl_d_kbeta = calc_d(kbeta_mean, nacl_kbeta1_angle)
nacl_d_kalpha = calc_d(kalpha_mean, nacl_kalpha1_angle)

```

```

nacl_d_mean = (nacl_d_kbeta + nacl_d_kalpha) / 2

nacl_M_Mol = 58.44 # g
nacl_rho = 2.164 * 100**(3) # g / m^3

# N_A = 1/2 * M_{Mol} / d^3

N_A_val = (1/2) * (nacl_M_Mol / nacl_rho) * (1 / nacl_d_mean.val**3)
N_A_err = (1/2) * (nacl_M_Mol / nacl_rho) * (3 * nacl_d_mean.err / nacl_d_mean.
    ↪val**4)
N_A = ValErr(N_A_val, N_A_err)

# NaCl a, https://de.wikipedia.org/wiki/Natriumchlorid-Struktur
nacl_a_lit = 0.564 * 10**(-9)

print_all(
    kalpha_mean.strfmtf2(6, -12, ',K_ '),
    kbeta_mean.strfmtf2(6, -12, ',K_ '), '',
    nacl_kalpha1_angle.strfmtf2(6, 0, ',K_ '),
    nacl_kbeta1_angle.strfmtf2(6, 0, ',K_ '), '',
    nacl_d_kalpha.strfmtf2(6, -12, 'd,K_ '),
    nacl_d_kbeta.strfmtf2(6, -12, 'd,K_ '),
    nacl_d_mean.strfmtf2(6, -12, 'd'),
    (nacl_d_mean * 2).strfmtf2(6, -12, 'a'),
    (nacl_d_mean * 2).sigmadiff_fmt(ValErr(nacl_a_lit, 0)),
    N_A.strfmtf2(6, 23, 'N_A'),
    N_A.sigmadiff_fmt(ValErr(Consts.N_A, 0)))

```

,K_ = (71.171382 \pm 0.110251) \cdot 10^{-12}

,K_ = (63.274149 \pm 0.135983) \cdot 10^{-12}

,K_ = 7.291215 \pm 0.044213

,K_ = 6.459243 \pm 0.050100

d,K_ = (280.395432 \pm 1.746003) \cdot 10^{-12}

d,K_ = (281.227410 \pm 2.254563) \cdot 10^{-12}

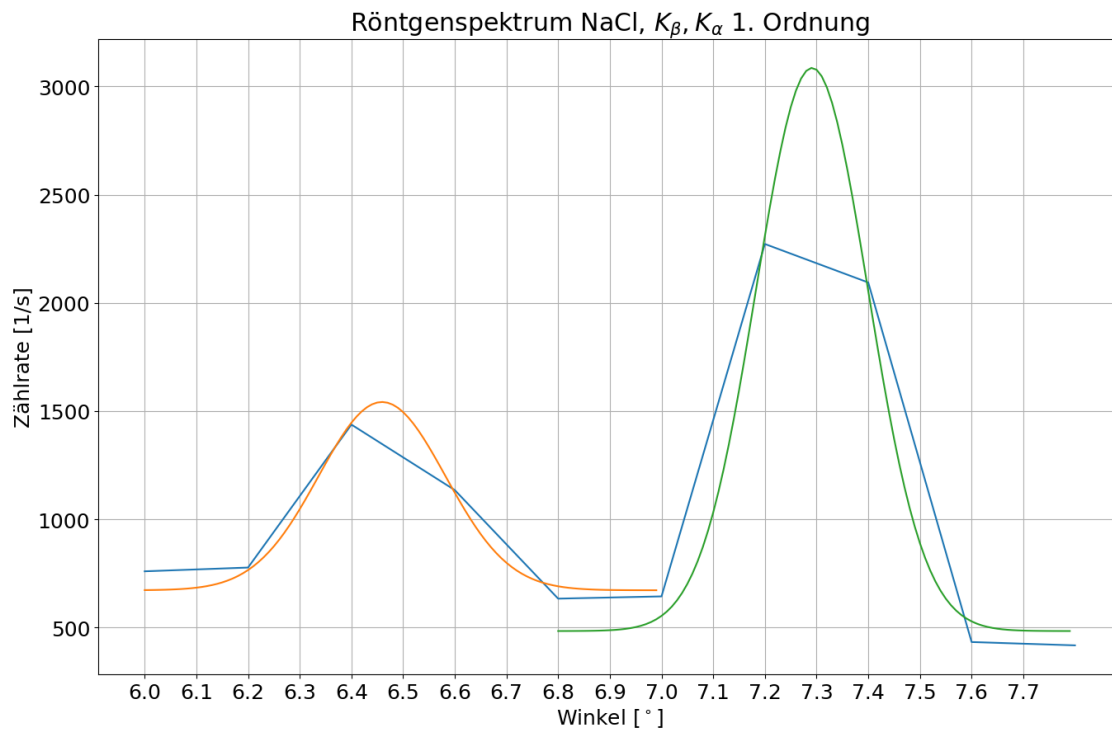
d = (280.811421 \pm 1.425796) \cdot 10^{-12}

a = (561.622843 \pm 2.851593) \cdot 10^{-12}

0.84

N_A = (6.097877 \pm 0.092884) \cdot 10^{23}

0.82



[]: