

TP6

1) Partialbruch

$$Y(s) = \frac{(s^2+1)(s^2+5)(s^2+20)}{s(s^2+10)(s^2+2)}$$

$$Y(s) = \frac{K_0}{s} + \frac{2K_1 s}{s^2+10} + \frac{2K_2 s}{s^2+2} + K_\infty s$$

$$\lim_{s \rightarrow 0} Y(s) = \lim_{s \rightarrow 0} \frac{K_0}{s} \rightarrow K_0 = \lim_{s \rightarrow 0} s \cdot Y(s) = \lim_{s \rightarrow 0} \frac{(s^2+1)(s^2+5)(s^2+20)}{s \cdot (s^2+10)(s^2+2)}$$

$$K_0 = \frac{1 \cdot 5 \cdot 20}{10 \cdot 2} = 5$$

$$2K_1 = \lim_{s^2 \rightarrow -10} Y(s) = \lim_{s^2 \rightarrow -10} \frac{2K_1 s}{s^2+10}$$

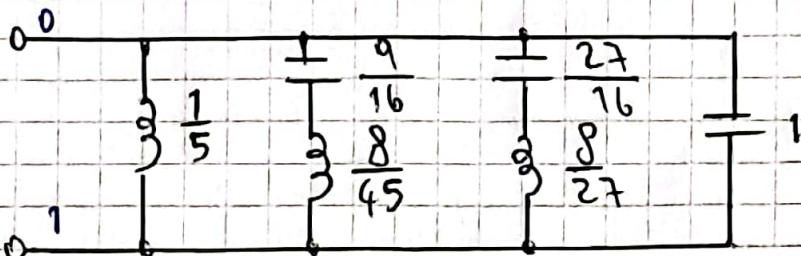
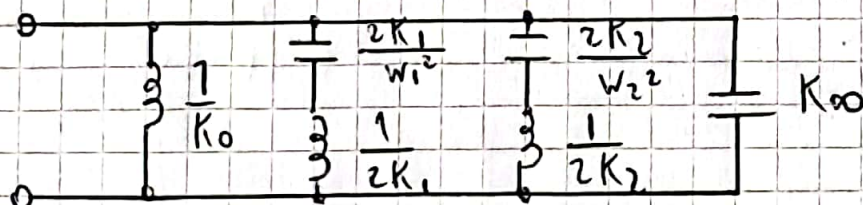
$$2K_1 = \lim_{s^2 \rightarrow -10} \frac{s^2+10}{s} \cdot Y(s) = \lim_{s^2 \rightarrow -10} \frac{s^2+10}{s} \cdot \frac{(s^2+1)(s^2+5)(s^2+20)}{s(s^2+10)(s^2+2)}$$

$$2K_1 = \frac{(-9)(-5)(10)}{(-10)(-8)} = \frac{45}{8}$$

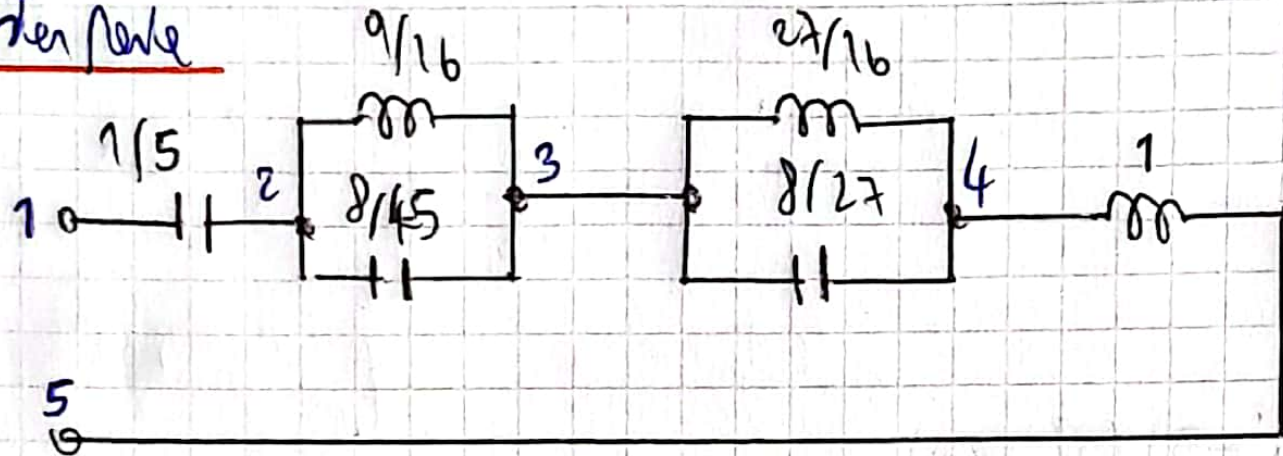
$$2K_2 = \lim_{s^2 \rightarrow -2} \frac{s^2+2}{s} \cdot \frac{(s^2+1)(s^2+5)(s^2+20)}{s(s^2+10)(s^2+2)} = \frac{(-1)(3)(20)}{(-2)(8)}$$

$$2K_2 = \frac{27}{8}$$

$$K_\infty = \lim_{s \rightarrow \infty} \frac{Y(s)}{s} = \lim_{s \rightarrow \infty} \frac{(s^2+1)(s^2+5)(s^2+20)}{s^2(s^2+10)(s^2+2)} = 1$$



Foster Netz



$$Y = \begin{pmatrix} +\frac{1}{5}s & -\frac{1}{5}s & 0 & 0 & 0 \\ +\frac{-1}{5}s & \frac{1}{5}s + \frac{8}{45}s + \frac{1}{59\frac{16}{16}} & \frac{-8}{45}s - \frac{1}{59\frac{16}{16}} & 0 & 0 \\ +0 & \frac{-8}{45}s - \frac{1}{59\frac{16}{16}} & \frac{8}{45}s + \frac{16}{59} + \frac{8}{27}s + \frac{16}{27s} & \frac{-8}{27}s - \frac{16}{27s} & 0 \\ +0 & 0 & \frac{-8}{27}s - \frac{16}{27s} & \frac{8}{27}s + \frac{1}{5} + \frac{16}{27s} & -\frac{1}{5} \\ 0 & 0 & 0 & -\frac{1}{5} & \frac{1}{5} \end{pmatrix}$$

$$Z_{15} = \frac{Y_{15}}{Y_{11}} \rightarrow \text{Major reduziert per Jupyter}$$