## Quiz 1 Formula Sheet - Important Formulas for Statistical Inference

## **One Sample**

$$H_0: \mu = \mu_0 \quad z = \frac{\overline{x} - \mu_0}{\sigma / \sqrt{n}}$$

$$t = \frac{\overline{x} - \mu_0}{s / \sqrt{n}}$$

$$H_0: p = p_0 \quad z = \frac{\hat{p} - p_0}{\sqrt{\frac{p_0 q_0}{n}}}$$

$$n = \frac{\left(z_{\alpha/2} + z_{\beta}\right)^2 \sigma^2}{\Delta^2}$$

$$n = \left[\frac{z_{\alpha/2}\sqrt{p_0q_0} + z_{\beta}\sqrt{p_aq_a}}{\Delta}\right]^2$$

## Two Samples

$$\mathbf{H}_{0}: \mu_{1} - \mu_{2} = \mu_{0} \quad z = \frac{\left(\overline{x}_{1} - \overline{x}_{2}\right) - \mu_{0}}{\sqrt{\frac{\sigma_{1}^{2}}{n_{1}} + \frac{\sigma_{2}^{2}}{n_{2}}}}$$

$$t = \frac{\left(\overline{x}_1 - \overline{x}_2\right) - \mu_0}{\sqrt{\frac{s_p^2}{n_1} + \frac{s_p^2}{n_2}}}$$

where 
$$s_p^2 = \frac{(n_1 - 1)s_1^2 + (n_2 - 1)s_2^2}{n_1 + n_2 - 2}$$

$$t = \frac{\left(\overline{x}_1 - \overline{x}_2\right) - \mu_0}{\sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}}}$$

$$\begin{aligned} \mathbf{H}_{0}: \mu_{d} &= \mu_{d_{0}} & t &= \frac{\overline{d} - \mu_{d_{0}}}{s_{d} / \sqrt{n}} \\ \mathbf{H}_{0}: p_{1} - p_{2} &= 0 & z &= \frac{\left(\hat{p}_{1} - \hat{p}_{2}\right) - 0}{\sqrt{\frac{\overline{p}\overline{q}}{n_{1}} + \frac{\overline{p}\overline{q}}{n_{2}}}} \end{aligned}$$

$$n = \frac{\left(z_{\alpha/2} + z_{\beta}\right)^{2} \left(\sigma_{1}^{2} + \sigma_{2}^{2}\right)}{\Delta^{2}}$$

$$n = \frac{\left[z_{\alpha/2}\sqrt{2\,\overline{p}\overline{q}} + z_{\beta}\sqrt{p_1q_1 + p_2q_2}\right]^2}{\Delta^2}$$