The optimal

$$a_t = \frac{\int_{x_{t-1}}^{x_t} q dI(q)}{\int_{x_{t-1}}^{x_t} dI(q)} \tag{1}$$

with

$$x_t = \frac{a_t + a_{t+1}}{2}. \tag{2}$$