PAU 2016

Criteris de correcció

Electrotècnia

SÈRIE 1

Primera part

Exercici 1

Q1 d

Q2 a

Q3 c

Q4 c

Q5 b

Exercici 2

a)
$$A_1 = \frac{\frac{U}{\sqrt{3}}}{R_1} = \frac{\frac{400}{\sqrt{3}}}{280} = 0.825 \text{ A}$$

b)
$$R_2 = \frac{\frac{U}{\sqrt{3}}}{A_2} = \frac{\frac{400}{\sqrt{3}}}{1,2} = 192,45 \,\Omega$$

c)
$$A_3 = A_1 + A_2 = 0.825 + 1.2 = 2.025 \text{ A}$$

d)
$$Q = 0$$
 var; $S = \sqrt{3} \cdot U \cdot I = \sqrt{3} \cdot 400 \cdot 2,025 = 1,4$ kVA; $P = 1,4$ kW

OPCIÓ A

Exercici 3

a)
$$P = \sqrt{3} U I \cos \varphi = \sqrt{3} \cdot 690 \cdot 18,88 \cdot 0,79 = 17,83 \text{ kW}$$

 $Q = \sqrt{3} U I \sin \varphi = \sqrt{3} \cdot 690 \cdot 18,88 \cdot \sqrt{1 - 0,79^2} = 13,83 \text{ kvar}$
 $S = \sqrt{3} U I = \sqrt{3} \cdot 690 \cdot 18,88 = 22,56 \text{ kVA}$
Alternativament,
 $P = \sqrt{3} U I \cos \varphi = \sqrt{3} \cdot 400 \cdot 32.7 \cdot 0.79 = 17.9 \text{ kW}$

$$P = \sqrt{3} U I \cos \varphi = \sqrt{3} \cdot 400 \cdot 32,7 \cdot 0,79 = 17,9 \text{ kW}$$

$$Q = \sqrt{3} U I \sin \varphi = \sqrt{3} \cdot 400 \cdot 32,7 \cdot \sqrt{1 - 0,79^2} = 13,89 \text{ kvar}$$

$$S = \sqrt{3} U I = \sqrt{3} \cdot 400 \cdot 32,7 = 22,66 \text{ kVA}$$

b)
$$p = 4$$

c)
$$\Gamma = \frac{P}{\omega} = \frac{15000}{732\frac{2\pi}{1000}} = 195,68 \text{ Nm}$$

d) 400 V,
$$I_{Linia} = 32.7 \text{ A}$$

Exercici 4

a)
$$\begin{cases} R_1 I_1 + R_2 (I_1 + I_2) = U_1 \\ R_3 I_2 + R_2 (I_1 + I_2) = U_2 \end{cases} \rightarrow \begin{cases} (R_1 + R_2)I_1 + R_2 I_2 = U_1 \\ R_2 I_1 + (R_2 + R_3)I_2 = U_2 \end{cases}$$

$$\begin{cases} (10 + 20)I_1 + 20I_2 = 48 \\ 20I_1 + (20 + 10)I_2 = 36 \end{cases} \rightarrow \begin{cases} 30I_1 + 20I_2 = 48 \\ 20I_1 + 30I_2 = 36 \end{cases} \rightarrow \begin{cases} I_1 = 1,44 \text{ A} \\ I_2 = 0,24 \text{ A} \end{cases}$$

b)
$$P(R_2) = R_2(I_1 + I_2)^2 = 20(1,44 + 0,24)^2 = 56,448 \text{ W}$$

c)
$$I_1 = \frac{U_1}{R_1} = \frac{48}{10} = 4.8 \text{ A}; I_2 = \frac{U_2}{R_3} = \frac{36}{10} = 3.6 \text{ A}$$

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OPCIÓ B

Exercici 3

a)
$$A_1 = \frac{V_1}{R} = \frac{230}{115} = 2 \text{ A}$$

b)
$$X_L = \omega L = 2\pi f L = 2\pi 150 \cdot 3 \cdot 10^{-3} = 2,8274 \Omega$$

$$X_{\text{C1}} = \frac{1}{\omega C_1} = \frac{1}{2\pi f C_2} = \frac{1}{2\pi 150 \cdot 250 \cdot 10^{-6}} = 4,2441 \ \Omega$$

$$A_2 = I_L - I_{C1} = \frac{V_1}{X_L} - \frac{V_1}{X_{C1}} = \frac{230}{2,8274} - \frac{230}{4,2441} = 27,1539 \text{ A}$$

c)
$$A_3 = \sqrt{A_1^2 + A_2^2} = \sqrt{2^2 + 27,1539^2} = 27,2275 \text{ A}$$

d)
$$A_3 = A_1 \rightarrow A_2 = 0 = (I_L - I_{C1}) - I_{C2} \rightarrow I_{C2} = (I_L - I_{C1}) = 27,1539 \text{ A}$$

$$I_{C2} = 27,1539 = \frac{V_1}{X_{C2}} = \frac{230}{X_{C2}} \rightarrow X_{C2} = \frac{230}{27,1539} = 8,4702 \Omega$$

$$C_2 = \frac{1}{\omega X_{C2}} = \frac{1}{2\pi 150 \cdot 8,4702} = 125,27 \ \mu\text{F}$$

També es pot fer:

$$f_{\rm r} = \frac{1}{2\pi\sqrt{LC}} \rightarrow C = \frac{1}{(2\pi f_{\rm r})^2 L} = \frac{1}{(2\pi 150)^2 \cdot 3 \cdot 10^{-3}} = 375,26 \,\mu\text{F}$$

$$C = C_1 + C_2 \rightarrow C_2 = C - C_1 = 375,26 - 250 = 125,26 \,\mu\text{F}$$

Exercici 4

a)
$$\Delta U_{\text{max}} = 230 \frac{3}{100} = 6.9 \text{ V}$$
 $R_{\text{escalfador}} = \frac{U_{\text{N}}^2}{P_{\text{N}}} = \frac{230^2}{1800} = 29.39 \Omega$

$$U=230=\Delta U_{\mathrm{max}}+R_{\mathrm{escalfador}}\cdot I=6.9+29.39\cdot I \quad \rightarrow \quad I=7.591\,\mathrm{A}$$

$$\Delta U_{\mathrm{max}} = 2 \cdot R_{\mathrm{conductor}} \cdot I \rightarrow R_{\mathrm{conductor}} = \frac{\Delta U_{\mathrm{max}}}{2 \cdot I} = \frac{6.9}{2 \cdot 7.591} = 0.4545 \,\Omega$$

$$R_{\rm conductor} = \rho \frac{l}{S_{\rm minima}} \rightarrow S_{\rm minima} = \rho \frac{l}{R_{\rm conductor}} = 16.8 \cdot 10^{-9} \frac{50}{0.4545} = 1.85 \text{ mm}^2$$

S'escull, doncs, la secció dels conductors de 2,5 mm².

b)
$$R_c = \rho \frac{l}{s} = 16.8 \cdot 10^{-9} \frac{50}{2.5 \cdot 10^{-6}} = 0.336 \Omega$$

$$I = \frac{U_{\text{N}}}{2 \cdot R_{\text{c}} + R_{\text{escalfador}}} = \frac{230}{2 \cdot 0.336 + 29.39} = 7,65 \text{ A}$$

$$P_{\text{escalfador}} = R_{\text{escalfador}} \cdot I^2 = 29,39 \cdot 7,65^2 = 1720 \text{ W}$$

c)
$$I_{cc} = \frac{U_{N}}{2 \cdot R_{c}} = \frac{230}{2 \cdot 0.336} = 342.3 \text{ A}$$