



Digital Image Processing

Third Edition

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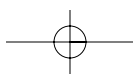
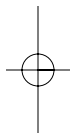
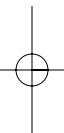
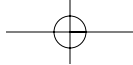
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*To Samantha
and
To Janice, David, and Jonathan*



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