



# Rendering Handwritten Equations



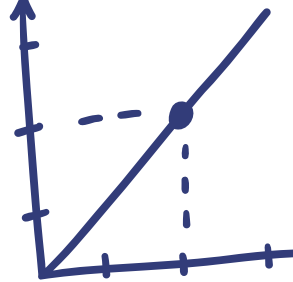
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Capstone Project Presentation  
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$$\sqrt{\frac{3}{4}} = (a^2)$$



# Problem Statement



Develop a tool that can render handwritten equations in digital format.

**Input:** an image containing an equation

**Output:** the equation in digital format, using LaTeX math notation





# For example..

$$\log_2 8 + \log_3 9 + \log_4 16$$



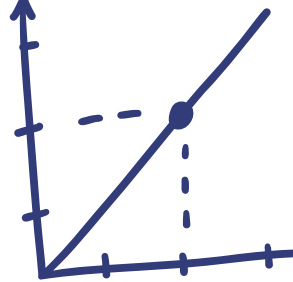
$$\text{\textbackslash}\log\_2 8 + \text{\textbackslash}\log\_3 9 + \text{\textbackslash}\log\_4 16\text{\textbackslash}$$



How we evaluate performance



$$\log_2 8 + \log_3 9 + \log_4 16$$



# Why is this complicated?

**Symbols are not  
just read  
left-to-right**

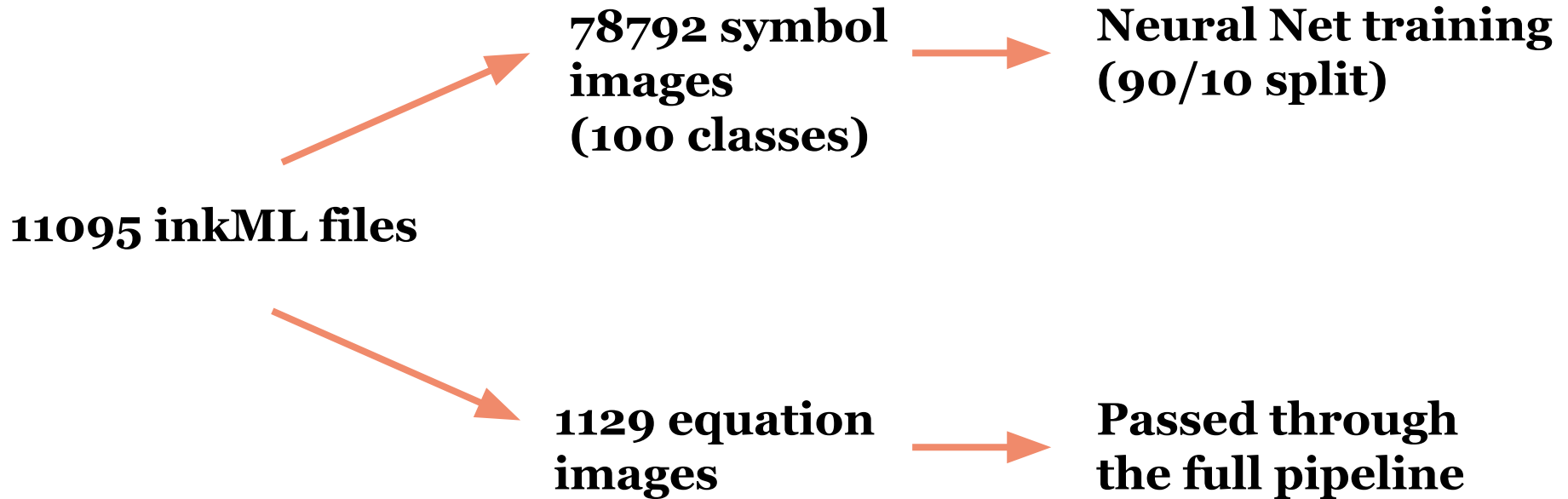
$$\int_{\log 3}^0 \frac{1}{e^t + 1} dt$$

# Data

- CROHME
- 'inkML' format
- Full equation label
- Labels for each symbol
- 100 different symbols

A handwritten mathematical equation is shown, illustrating the CROHME data format. The equation is  $A = \sqrt{a + \frac{1}{\sqrt{a + \frac{1}{\sqrt{a}}}}} + \sqrt{b}$ . The symbols are color-coded: 'A' is blue, '=' is green, 'a' is brown, '1' is pink, 'a' is cyan, '1' is green, 'a' is orange, '+' is pink, and 'b' is cyan. Dashed lines of corresponding colors represent the inkML labels for each symbol, showing how the structure of the equation is encoded.

# Data Processing



# Pipeline Overview



## 1. Image thresholding

Change image into black/white values

## 2. Resolving Symbols

Figure out the symbol on the image and their order

## 3. Model Prediction

Use an EfficientNetBo CNN to predict labels

## 4. Rendering the equation

Stitch the predictions together into an equation

# 1) Image Tresholding

$$\gamma(x) = \lim_{n \rightarrow \infty} \frac{n! \cdot n^x}{x^{(n+1)}}$$

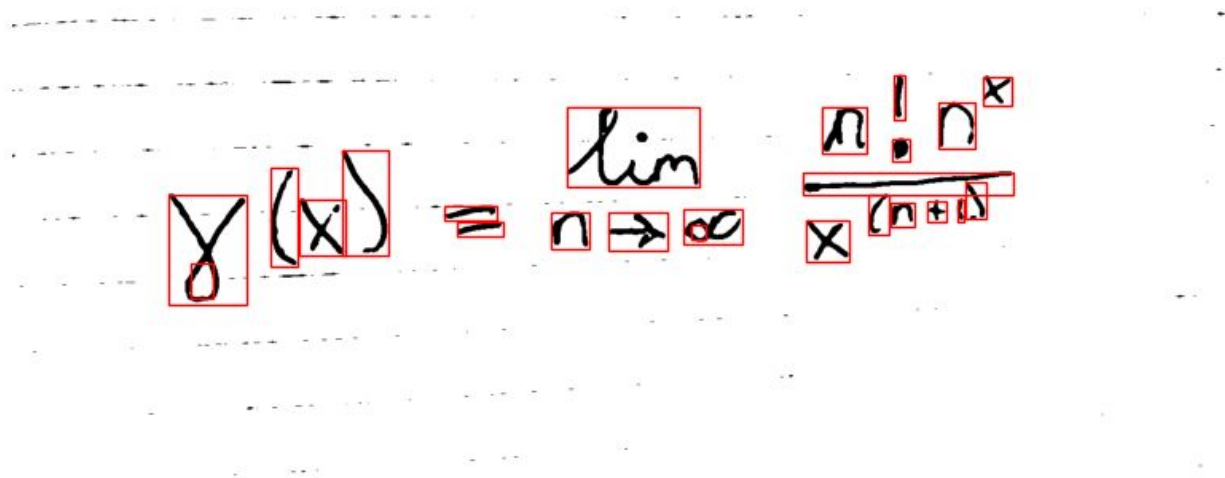
$$\gamma(x) = \lim_{n \rightarrow \infty} \frac{n! \cdot n^x}{x^{(n+1)}}$$

Adaptive Gaussian Tresholding



## 2) Resolving Symbols

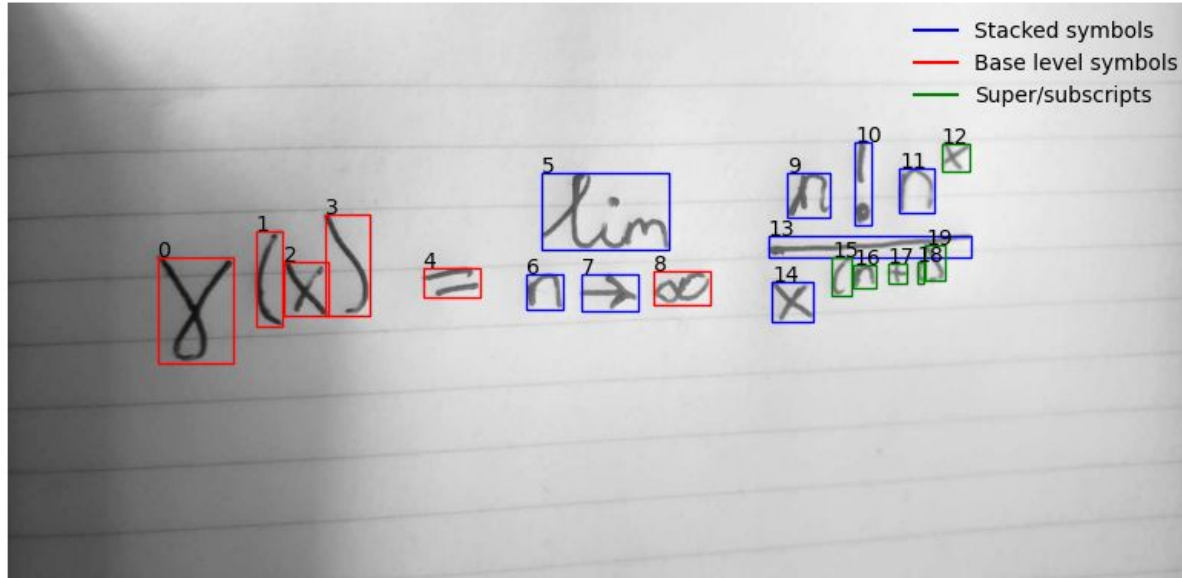
Find Contours and Bounding Boxes



- i) Remove Inner Contours
- ii) Merge Boxes

- iii) Determine Symbol order
- iv) Determine Script level

## 2) Resolving Symbols



- i) Remove Inner Contours
- ii) Merge Boxes

- iii) Determine Symbol order
- iv) Determine Script level

# 3) Model Predictions

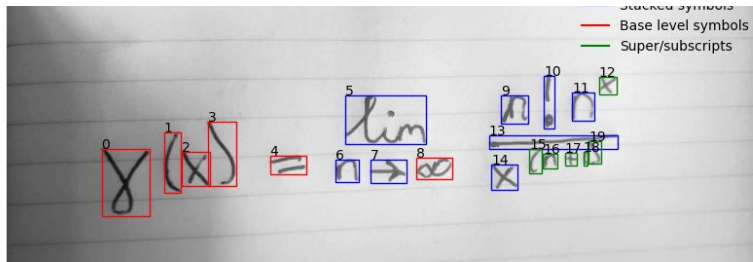
**Model:** EfficientNetBo CNN

95% accuracy on validation data  
(*individual symbol images*)

**Prediction Step:**

Symbol Images ->  
List of class labels

# 4) Render the Equation



$\gamma(X) = \lim_{n \rightarrow \infty} \frac{n!n^k}{\times^{(n+1)'}}$

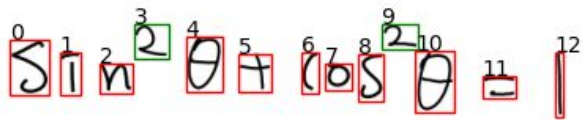


$$\gamma(X) = \lim_{n \rightarrow \infty} \frac{n!n^k}{\times^{(n+1)'}}$$

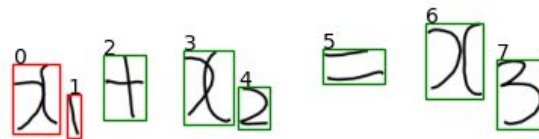
# Two more examples

- Stacked symbols
- Base level symbols
- Super/subscripts

- Stacked symbols
- Base level symbols
- Super/subscripts



Prediction:  $\sin^2 \theta + \cos^2 \theta = 1$



Prediction:  $x_1 + x_2 = x_3$

# Overall Pipeline Performance

## Damerau-Levenshtein distance

Actual: ' $x_{\{i\}} - x_{\{i+1\}} + x_{\{i+2\}}$ '

Predicted: ' $\mathbf{1}x_{\{\mathbf{1}\}} - x_{\{\mathbf{1}+1\}} + x_{\{\mathbf{1}+2\}}$ '

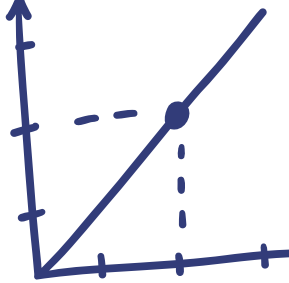
1 deletion, 3 substitutions

Normalize by actual string length:

Distance =  $4/21 \approx 0.477$

DL distance	% of equations
0	<b>15.7%</b>
< 0.10	<b>20.9%</b>
< 0.50	<b>65.9%</b>

# Final thoughts..



This is a difficult problem to solve!

Errors compound through the 4 pipeline steps

Different linewidths seem to make the predictions less accurate than the 95% accuracy in NN

Multiple Object Detection algorithms

