

# Day 1

**\*\* Concepts relevant from Assignment 0 and 1 \*\***

## 1. Assignment 0:

1. Memory allocation (non continuous in our code), and correct freeing: In assignment 0 we learned the advantages and disadvantages of each type of memory allocation: stack allocation is faster but one has to be certain that an array fits on the stack, and heap is used in the opposite case. Heap allocation can be structured to be “flexible” which is generally slower than allocating the whole array at the same time, but it allows to allocate and free memory in a more tailored way for our program. This flexible approach to allocate memory can allow us to “create” and free a specific row to write the results of the Newton method in a memory efficient way. We will test between continuous and non continuous memory allocation for the arrays that will store the root ids, and number of iterations, and decide which, if any, improve our benchmark.
2. fopen, fwrite (faster than fprintf). In assignment 0 we learned the difference between writing characters, or writing bits directly to a file, and understood that for speed purposes the correct choice is to write bits directly using fwrite. This approach is going to be used from the beginning since we are certain that fwrite command is much faster than fprintf and satisfies our needs.
3. Parsing command line arguments In assignment 0 we learned how to write a program that accepts or needs arguments to function, we learned and understood the syntax to create an efficient way of parsing arguments in a way that it recognizes every pattern, i.e. -arg1, arg1... We have found that using the function opt simplifies this task.
4. Make files Make files are an amazing tool to save time in the compilation process of a “big” project, because it allows to perform changes and compile them avoiding small syntax mistakes, like forgetting to link a library, or use the correct optimization flag.

## 2. Assignment 1: 1. Correct benchmarking In assignment 1 we learned that the correct way to perform benchmarking was to run the specific task many times and then get the mean in order to have a realistic result not subject to small volatilities. In this assignment benchmarking is a must, and so the process has to be optimal. Among other things, we use the benchmarking techniques to compare our power function with cpow, in order to be sure that our implementation was faster, and should be used in our code.

2. Inline code to make it faster, small functions. In assignment 1 we learned that inlining a function, specially if it is small, can improve the performance of a program, if the function is called iteratively many times.

3. Use static inline to explicitly suggest the compiler to inline a function. We use static inline to “suggest” to the compiler to inline certain functions that we consider would be better placed in the main code at compilation. As an example we wrote our own power function, optimizing it to be faster than cpow and we use static inline for it, because it is called many times when solving

Newton's method.

4. Locality, computing initial points moving through the rows. We learned in assignment 1 that accessing memory is faster if we access addresses that are close or adjacent, and not jump from one place to another in memory, in our program we implemented this concept by letting each thread compute the roots for a whole row before jumping to the next.

6. Use of valgrind and GDB to analyze code and check for improvement options. Finally we learned in assignment 1 that these tools can be good allies in order to understand the performance of our code. With Valgrind we check for memory leaks or incorrect allocation and freeing procedures, and with GDB we can go to the origin of a bug, or a line where the code crashes or does something unexpected, and check what is happening in there, and the actual value of the variables at that point.

## Day 2

**\*\* Program Layout & List of Subtasks \*\***

1. Initialization Setup: Argument Parser, setup global variables
2. Implement synchronization and threading for : compute thread and write thread
3. compute\_main Function: Check  $x_k$  for convergence
4. compute\_next Function: Compute  $x_{k+1}$
5. Setup color mapping and write to file.

## Day 3-4

**\*\* Implementation & Revision of Subtasks \*\***

1. Argument Parsing & Global variables
  1. Check if all needed values are available.
  2. Value of 'l' should not exceed 1000.
  3. Value of 'd' should not exceed 9 and must be greater than 0.
  4. Study "Assignment 0: Parsing command line arguments" for motivation.
  5. Study global variables and setup mutex.
2. compute\_next function
  1. Objective: Find  $x_{k+1}$  in the most effective way.
  2. Implementation 1:  $x_{k+1} = x_k - (\text{cpow}(x_k, d) - 1) / (d * \text{cpow}(x_k, d - 1))$
  3. Remark for Implementation 1: VERY SLOW
  4. Implementation 2:
    1. compute\_next is implemented as inline function
    2. Compute  $\theta = \text{atan}(\text{imaginary}(x_k), \text{real}(x_k))$
    3. Compute  $r = \text{real}(x_k) \text{real}(x_k) + \text{imaginary}(x_k) \text{imaginary}(x_k)$

4. Using De Moivre's theorem we get  $z^n = r^n * \text{cis}(n\theta)$  Compute  $z = (\text{pow}(r,d) * (\cos(d\theta) + i\sin(d\theta))) / (d * \text{pow}(r,d-1) * (\cos((d-1)\theta) + i\sin((d-1)\theta)))$
5.  $x_{k+1} = x_k - z$

### 3. compute\_main function

1. Objective: Check if the given point ( $x_k$ ) is converging to a root or no.
2. Store roots for the given function with all possible values of  $d=1,2,\dots,9$  in a  $9 \times 9$  matrix.
3. Norm of a complex number is defined as  $\sqrt{R^2 + I^2} = \text{epsilon}$ , where  $R$  and  $I$  are real and imaginary coefficients of the complex number.
4. Instead of using `csqrt()` and `cabs()`, defined in `complex.h` we implement norm in a different way. This is done by squaring the equation in above given equation. Therefore,  $R^2 + I^2 = \text{epsilon}^2$ . Which helps us avoid time consuming functions like `csqrt()` and `cabs()`.
5. Setup initial matrix  $A$  having  $r$  rows and  $c$  columns where  $r = c$ .
6. Run a Loop\_1 from  $k = A[0][0] \dots A[r][c]$ 
  1. Set a variable `converged = False`, to keep track of whether  $x_k$  has converged.
  2. If  $k = 1 \Rightarrow x_k = x_0$
  3. Criteria 1: Check if Absolute value of  $\text{real}(x_k)$  and  $\text{imaginary}(x_k)$  both must be  $\leq 10000000000$ .
  4. Criteria 2: Check if norm of  $x_k$  must be  $\leq (10^{-3})^2$ .
  5. Criteria 3: Run a Loop\_2 from  $i = 1 \dots d$  difference =  $x_1 - \text{root}[d-1][i]$  Check if the norm of difference  $\leq (10^{-3})^2$
  6. If any of the above criteria is true at any point we set `converged = True`  $\Rightarrow$  break Loop\_2 iteration and pass the value to write thread; If it is False we compute  $x_{k+1} = \text{compute\_next}(x_k)$ .

## Day 5

### \*\* Functional Program \*\*

1. We achieved a function program which prints a PPM file same as the sample newton file.
2. Currently we are working on methods to reduce the execution time of our program in half.