

Diagonalisation of random real symmetric matrices

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Introduction

I am solving problem 27 in [1]. The problem is to implement a function that given an integer makes a $n \times n$ random real symmetric matrix with elements chosen uniformly at random in the interval $[0, 1]$. The matrix then has to be diagonalized and in the process finding the largest eigenvalue which is returned. This process is repeated for different values of n , which results in data for a plot and a fit.

Method

To fit the data I have used a simple linear fit without constant offset as in equation (1).

$$y = cx \quad (1)$$

The value of the single fitting parameter as found by *gsl_fit* is $c = 0.502276$ which is very close to being 0.5 which we would expect since the entrances of the matrix are random numbers in the range $[0, 1]$ which should converge to 0.5.

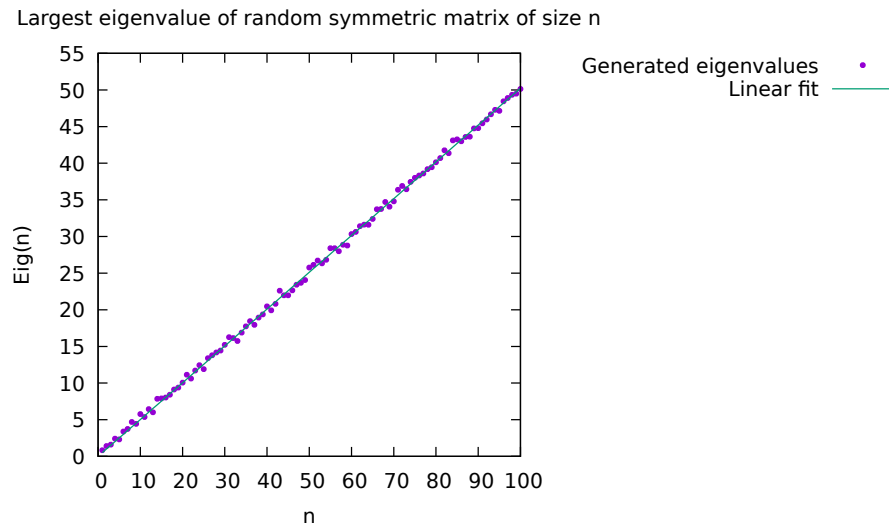


Figure 1: The largest eigenvalue as a function of matrix size n for random symmetric real matrices. The purple dots represent the found eigenvalues while the green line represent a linear fit to the data using equation (1)

Bibliography

- [1] Fedorov, D.V., Retrieved 14.03.2018, from <http://86.52.112.181/~fedorov/prog/ass/sf.pdf>.