

$$V_t = e^{-r(T-t)} E_t^Q [\Phi(S(T)) | S(t) = S]$$

$$\Phi(S_T) = 1_{S_T \geq K}$$

$$\Rightarrow E_t^Q [\Phi(S(T)) | S(t) = S]$$

$$= E_t^Q [1_{S_T \geq K} | S(t) = S]$$

$$S_T = S \cdot \exp\left((r - \frac{\sigma^2}{2})t + \sigma W_t^Q\right)$$

$$S_T \geq K$$

$$\Rightarrow S \exp\left((r - \frac{\sigma^2}{2})t + \sigma W_t^Q\right) \geq K$$

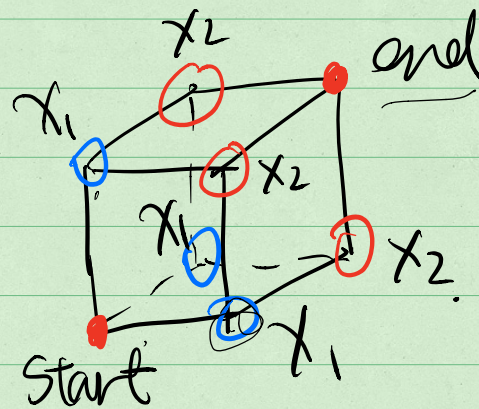
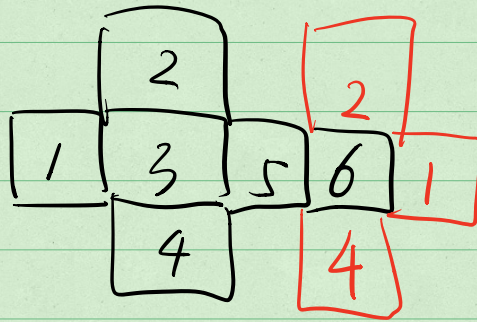
$$\Rightarrow (r - \frac{\sigma^2}{2})t + \sigma W_t^Q \geq \ln(K/S)$$

$$\Rightarrow W_t^Q \geq \frac{1}{\sigma} [\ln(K/S) - (r - \frac{\sigma^2}{2})t] \triangleq A$$

$$E_t^Q [1_{S_T \geq K} | S(t) = S]$$

$$= 1 - \Phi(A)$$

$$\Rightarrow V_t = e^{-r(T-t)} \cdot [1 - \Phi(\frac{1}{\sigma} (\ln(K/S) - (r - \frac{\sigma^2}{2})t))]$$



$$\begin{aligned}
 E[\text{Blue}] &= \frac{2}{3} E[\text{Red}] + \frac{1}{3} E[\text{Start}] + 1 \\
 E[\text{Red}] &= \frac{2}{3} E[\text{Blue}] + \frac{1}{3} E[\text{end}] + 1 \\
 E[\text{Start}] &= E[\text{Blue}] + 1 \\
 E[\text{end}] &= E[\text{Red}] + 1
 \end{aligned}$$

$$3B = 2R + (B+1) + 3$$

$$1 \quad 5K = 2B + (K+1) + 5$$

$$\begin{cases} 2B = 2R + 4 \\ 2R = 2B + 4 \end{cases}$$

$$\begin{cases} B = R + 2 \\ R = B + 2 \end{cases}$$

$$B = \frac{2}{3}R + 1$$

$$R = \frac{2}{3}B + \frac{1}{3}E + 1 \Rightarrow$$

$$E = R + 1$$

$$3B = 2R + 3$$

$$2R = 2B + 4$$

$$3B = 2B + 7$$

$$B = 7$$

$$R = 9$$

$$E = 10$$