1 Self Study 3: Exam Preparation 1

1.1 Excercise 4

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1
\pi_{\texttt{Sname}}(\texttt{Suppliers}\bowtie(\texttt{Catalog}\bowtie\sigma_{\texttt{color}=\texttt{red}}(\texttt{Parts})))
                                             \{s.\mathtt{sname}\mid s\in\mathtt{Suppliers}\wedge\exists c\in\mathtt{Catalog}(s.\mathtt{sid}=c.\mathtt{sid}\wedge\exists p\in\mathtt{Parts}(c.\mathtt{pid}=c.\mathtt{sid})\}
p.pid \land p.color = red))
                                             \{\langle b \rangle \mid \exists a, c(\langle a,b,c \rangle \in \mathtt{Suppliers} \land \exists i,j(\langle b,i,j \rangle \in \mathtt{Catalog} \ \land \ \exists y,z(\langle i,y,z \rangle \in \mathtt{Catalog} \ \land \ \exists x,z(\langle i,y,z \rangle \in \mathtt{Catalog} \ \land \ \exists x,z(\langle i,y,z \rangle \in \mathtt{Catalog} \ \land \ \exists x,z(\langle i,y,z \rangle \in \mathtt{Catalog} \ \land \ \exists x,z(\langle i,y,z \rangle \in \mathtt{Catalog} \ \land \ \exists x,z(\langle i,y,z \rangle \in \mathtt{Catalog} \ \land \ \exists x,z(\langle i,y,z \rangle \in \mathtt{Catalog} \ \land \ \exists x,z(\langle i,y,z \rangle \in \mathtt{Catalog} \ \land \ \exists x,z(\langle i,y,z \rangle \in \mathtt{Catalog} \ \land \ \exists x,z(\langle i,y,z \rangle \in \mathtt{Catalog} \ \land \ \exists x,z(\langle i,y,z \rangle \in \mathtt{Catalog} \ \land \ \exists x,z(\langle i,y,z \rangle \in \mathtt{Catalog} \ \land \ \exists x,z(\langle i,y,z \rangle \in \mathtt{Catalog} \ \land \ \exists x,z(\langle i,y,z \rangle \in \mathtt{Catalog} \ \land \ \exists x,z(\langle i,y,z \rangle \in \mathtt{Catalog} \ \land \ \exists x,z(\langle i,y,z \rangle \in \mathtt{Catalog} \ \land \ \exists x,z(\langle i,y,z \rangle \in \mathtt{Catalog} \ \land \ \exists x,z(\langle i,y,z \rangle \in \mathtt{Catalog} \ \land \ \exists x,z(\langle i,y,z \rangle \in \mathtt{Catalog} \ \land \ \exists x,z(\langle i,y,z \rangle \in \mathtt{Catalog} \ \land \ \exists x,z(\langle i,y,z \rangle \in \mathtt{Catalog} \ \land \ \exists x,z(\langle i,y,z \rangle \in \mathtt{Catalog} \ \land \ \exists x,z(\langle i,y,z \rangle \in \mathtt{Catalog} \ \land \ \exists x,z(\langle i,y,z \rangle \in \mathtt{Catalog} \ \land \ \exists x,z(\langle i,y,z \rangle \in \mathtt{Catalog} \ \land \ \exists x,z(\langle i,y,z \rangle \in \mathtt{Catalog} \ \land \ \exists x,z(\langle i,y,z \rangle \in \mathtt{Catalog} \ \land \ \exists x,z(\langle i,y,z \rangle \in \mathtt{Catalog} \ \land \ \exists x,z(\langle i,y,z \rangle \in \mathtt{Catalog} \ \land \ \exists x,z(\langle i,y,z \rangle \in \mathtt{Catalog} \ \land \ \exists x,z(\langle i,y,z \rangle \in \mathtt{Catalog} \ \land \ \exists x,z(\langle i,y,z \rangle \in \mathtt{Catalog} \ \land \ \exists x,z(\langle i,y,z \rangle \in \mathtt{Catalog} \ \land \ \exists x,z(\langle i,y,z \rangle \in \mathtt{Catalog} \ \land \ \exists x,z(\langle i,y,z \rangle \in \mathtt{Catalog} \ \land \ \exists x,z(\langle i,y,z \rangle \in \mathtt{Catalog} \ \land \ \exists x,z(\langle i,y,z \rangle \in \mathtt{Catalog} \ \land \ \exists x,z(\langle i,y,z \rangle \in \mathtt{Catalog} \ \land \ \exists x,z(\langle i,y,z \rangle \in \mathtt{Catalog} \ \land \ \exists x,z(\langle i,y,z \rangle \in \mathtt{Catalog} \ \land \ \exists x,z(\langle i,y,z \rangle \in \mathtt{Catalog} \ \land \ \exists x,z(\langle i,y,z \rangle \in \mathtt{Catalog} \ \land \ \exists x,z(\langle i,y,z \rangle \in \mathtt{Catalog} \ \land \ \exists x,z(\langle i,y,z \rangle \in \mathtt{Catalog} \ \land \ \exists x,z(\langle i,y,z \rangle \in \mathtt{Catalog} \ \land \ \exists x,z(\langle i,y,z \rangle \in \mathtt{Catalog} \ \land \ \exists x,z(\langle i,y,z \rangle \in \mathtt{Catalog} \ \land \ \exists x,z(\langle i,y,z \rangle \in \mathtt{Catalog} \ \land \ \exists x,z(\langle i,y,z \rangle \in \mathtt{Catalog} \ \land \ \exists x,z(\langle i,y,z \rangle \in \mathtt{Catalog} \ \land \ \exists x,z(\langle i,y,z \rangle \in \mathtt{Catalog} \ \land \ \exists x,z(\langle i,y,z \rangle \in \mathtt{Catalog} \ \land \ \exists x,z(\langle i,y,z \rangle \in \mathtt{Catalog} \ \land \ \exists x,z(\langle i,y,z \rangle \in \mathtt{Catalog} \ \land \ \exists x,z(\langle i,z,z \rangle \in \mathtt{Catalog} \ \land \ \exists x,z(\langle i,z,z \rangle \in \mathtt{Catalog} \ \land \ \exists x,z(
Parts \land z = red)))
\pi_{\texttt{sid}}(\texttt{Catalog} \bowtie \sigma_{\texttt{color} = \texttt{red} \ \lor \ \texttt{color} = \texttt{green}}(\texttt{Parts}))
                                             \{c.\mathtt{sid} \mid c \in \mathtt{Catalog} \land \exists p \in \mathtt{Parts}(c.\mathtt{pid} = p.\mathtt{pid} \land p.\mathtt{color} = \mathtt{red} \lor a
p.\mathtt{color} = \mathtt{green}))
                                             \{\langle b \rangle \mid \exists i,j(\langle b,i,j \rangle \in \mathtt{Catalog} \ \land \ \exists y,z(\langle i,y,z \rangle \in \mathtt{Parts} \ \land \ (z = \mathtt{red} \lor z =
green)))
3
\pi_{\texttt{sid}}(\texttt{Catalog} \bowtie \sigma_{\texttt{color}=\texttt{red}}(\texttt{Parts})) \bowtie \pi_{\texttt{sid}}(\texttt{Catalog} \bowtie \sigma_{\texttt{color}=\texttt{green}}(\texttt{Parts}))
                                             \{c_1.\mathtt{sid} \mid c_1 \in \mathtt{Catalog} \land \exists c_2 \in \mathtt{Catalog}(c_1.\mathtt{sid} = c_2.\mathtt{sid} \land \exists p_1, p_2 \in \mathtt{Catalog}(c_1)\}
\mathtt{Parts}(c_1.\mathtt{pid} = p_1.\mathtt{pid} \ \land \ c_2.\mathtt{pid} = p_2.\mathtt{pid} \ \land \ p_1.\mathtt{color} = \mathtt{red} \ \land \ p_2.\mathtt{color} =
green))}
                                           Parts \land \langle i, x, y \rangle \in \texttt{Parts} \land v = \texttt{red} \land y = \texttt{green})))
4
\{s_1.\mathtt{sid}, s_2.\mathtt{sid} \mid \exists c_1, c_2 \in \mathtt{Catalog}(c_1.\mathtt{sid} = s_1.\mathtt{sid} \land c_2.\mathtt{sid} = s_2.\mathtt{sid} + s_2.\mathtt
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 $\exists p_1, p_2 \in \mathsf{Parts}(c_1.\mathsf{pid} = p_1.\mathsf{pid} \land c_2.\mathsf{pid} = p_2.\mathsf{pid} \land p_1.\mathsf{cost} > p_2.\mathsf{cost}))\}$