

# Non-standard Decision-making

*Cognitive foundations*

Advanced course in Behavioural and Psychological Economics

Tampere University

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[Link to updated version](#)

## **Bibliography:**

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# Topics

Introduction

Noisy Approximations

Comparative Thinking

Reduced Cardinality

Analogies and Categorization

Complexity Aversion

# Introduction

*Standard* theory poses:

$$\max_{x_t^i \in X_t} \sum_{t=0}^{\infty} \delta^t \sum_{s_t \in S_t} p(s_t) U(x_t^i | s_t) \quad (1)$$

- $U(x | s)$ : utility
- $x^t$ : period  $t$  payoffs
- $p(s)$ : probability of state  $s$
- $\delta$ : (time-consistent) discount factor

# Introduction

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... but **individuals not always optimize**

# Information Processing is Imperfect!

## 1 Procedures and Algorithms complexity

- Simple problems
  - Behavior can be well-approximated by the standard maximizing model
- Complex problems
  - People rely on specific procedures or algorithms
  - Arrieta & Nielsen (2023): As problems become more complex, people perform better in describing their decision-making process to others
- '*Complexity*': refers to the cost of information processing in computer science
  - Oprea (2020): People are willing to pay to avoid implementing certain rules!  
Which ones? Those with higher 'dimensionality'

# Information Processing is Imperfect!

## ② Decision Maker

- Cognitive resources
  - Abundant evidence of differential choices and beliefs
    - Hard to reconcile with preferences
    - Natural from a perspective of imperfect information processing
- Experience
  - Behavioral attenuation weakens as decision makers gather more experience with a specific problem configuration
    - Suggestive of efficient coding
    - Optimal reduction of noise for problems encountered frequently

# The Cognitive Turn on Behavioral Economics

## **Focus on explaining and unifying anomalies**

- Shift away from accumulating new deviations from neoclassical predictions
- Explore interrelationships between biases
- Many behaviors reflect imperfections in basic information processing

## **Replace reduced-form notions of biases**

- Focus on cognitive mechanisms underlying choice behavior:
  - 'Which cognitive limitation generates this choice behavior?'
  - 'How does it resemble anomalies in other domains?'
- Rather than:
  - 'Which utility function rationalizes this choice?'



# The Cognitive Turn on Behavioral Economics

- **Literature:**

- Mostly recent: post-2010
- Classical antecedents:
  - Bounded rationality (Simon, 1956)
  - System 1 vs System 2 (Kahneman, 2011)

- **Why so recent?**

- More complex than previous explanations
  - Reduced-form approach avoids complexity
  - Reduced-form approach is more workable in (theory and) practice

# The Cognitive Turn on Behavioral Economics

- **(Most) economic decisions are difficult**
  - Intensive information processing requirements
- **People rely on simplification strategies**
  - Strategies play out similarly across contexts:
    - 1 Noisy Aproximations
    - 2 Comparative Thinking
    - 3 Reduced Cardinality
    - 4 Analogies or Categorization
    - 5 Complexity Aversion (avoiding options that are difficult-to-assess)
- **Decision problem features affect information-processing imperfections**
- **Still no unified model**

# Theoretical Framework

Consider a decision maker taking a decision to maximize overall utility, which is comprised of different problem dimensions  $i$ :

$$\max_a U(a, \theta) = \sum_i u_i(y_i) = \sum_i u_i(g_i(a, \theta)) \quad (11)$$

- $u_i(y_i)$ : dimension-by-dimension utility
- $y_i$ : outcomes
- $g_i(\cdot)$ : outcome production functions
- $a$ : decision
- $\theta$ : economic fundamentals

# Theoretical Framework

Decision maker would choose the decision that maximizes utility:

$$a^*(\theta) \in \arg \max_a U(a, \theta), \quad \frac{\partial a^*(\theta)}{\partial \theta_j} |_{\theta} \equiv \beta_j$$

This maps economic fundamentals in a way the maximizes utility ...

but this is a rather strong assumption!

Some examples:

- How many hours should you work per week to maximize your discounted expected lifetime utility?
- How much of your money should you invest in the stock market?
- Interest rate increases from 0% to 4%. What additional fraction of your income should you save now?
- Do you prefer a 30% chance of getting 120 EUR or a 85% chance of getting 40 EUR ?

# Do people know the optimal decision?

## Indirect evidence of choice uncertainty

- Standard measures of preferences strongly depend on the elicitation format
  - e.g., *self-reported altruism* vs. *incentivized donation to A* vs. *incentivized donation to B*
- Experimental manipulations have systematic effects on observed choices
  - Problem complexity (e.g., 1 vs.  $\int_0^\infty e^{-x} dx$ )
  - Cognitive resources (e.g., *high or low time constraints*)
- Anomalous preferences correlated with behavior in cognitive problems

## Measurements of choice uncertainty

- Direct questions to decision makers
- Deliberate randomization strategies
- Willingness to delegate decisions

# What makes problems hard?

## Cardinality

- The more dimensions a problem has, the harder
  - Outcomes of interest
  - Variables to consider
  - Signals received
- e.g., *'vanilla or chocolate?'* vs. *'small vanilla with sprinkles vs large chocolate with nuts?'*

## Aggregation

- ① Requires introspection
  - 'What is my discount/risk factor?'
- ② Even with all information available, decision makers still need to process it
  - Tradeoffs present vs future / risk vs certainty

# What do people do?

- They avoid information processing by simplifying!
- Main responses:

## **Simplify the aggregating process**

- ① (Noisily) approximate
- ② Bracket and compare

## **Subset to simplify the problem**

- ③ Reduce cardinality

## **Solve a simpler problem**

- ④ Thinking in analogies and categories
- ⑤ Avoiding objects one cannot properly evaluate

# Are these responses deliberate?

Sometimes yes, . . . but sometimes no.

Proposed solutions will depend on the source of the response:

- **Deliberate simplifications**

- In line with procedural choice and bounded rationality
  - e.g., *noisily approximation*
  - Possible policy response: simplify procedure

- **Intuitive simplifications**

- In line with distinction between 'system 1' and 'system 2' thinking
  - e.g., *salience bias*
  - Possible policy response: promote time to think



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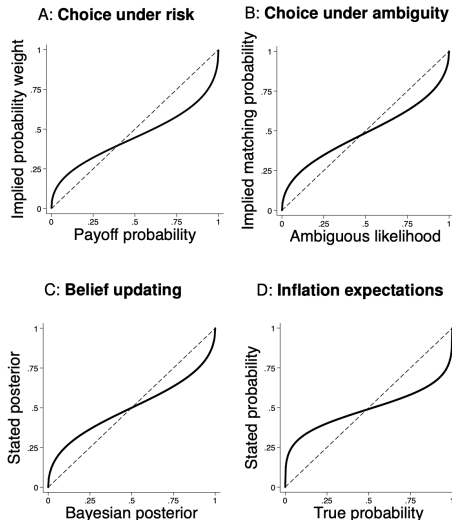
Complexity Aversion

# Noisy Approximations

**People approximate**, rather than solving a problem precisely

- Time: *"about 30 minutes"*
- Risk: *"seems like a low chance"*
- Labor: *"roughly two days to study for the exam"*
- Budget: *"costs around 200 EUR a month"*

# 'Weighting functions' in choices and beliefs



- A** Risk: people overweight small probabilities and underweight large probabilities
- B** Ambiguity: people avoid ambiguity for probable gains but seek it for unlikely gains
- C** Beliefs: people overreact after weak signals but underreact after strong signals
- D** Expectations: people expect too much when low but too little when high

# Theoretical Framework

Suppose that people's average decisions can be described as a convex combination:

$$E[a(\theta)] = (1 - \lambda)a^*(\theta) + \lambda d \quad (12)$$

- $a$ : decision
- $\theta$ : economic fundamentals
- $\lambda$ : degree of attenuation
- $d$ : default decision

# Theoretical Framework

This yields an attenuated effect:

$$\frac{\partial E[a(\theta)]}{\partial \theta} = \underbrace{(1 - \lambda)}_{\text{Attenuation}} \frac{\partial a^*(\theta)}{\partial \theta}$$

- $\frac{\partial a^*(\theta)}{\partial \theta}$ : *normative sensitivity*, that is the optimal sensitivity

# Why does attenuation ( $\lambda$ ) emerge?

## Policy uncertainty

- People know the fundamentals ( $\theta$ ) but do not know how to map them into optimal decision ( $a^*(\theta)$ )
- In response, people make noisy decisions ( $s(\theta) = a^*(\theta) + \epsilon$ ) to update on true utility-maximizing decision
  - e.g., *dine Ethiopian cuisine on Friday* vs. *dine Bolivian cuisine on Saturday*

## Noisy perceptions

- People do not know the fundamentals ( $\theta$ ), but only observe noisy signals ( $s = \theta + \epsilon$ )
- Implied decisions also show attenuation bias
  - as individuals decide based on prior fundamentals ( $\theta$ )

# What determines default decisions ( $d$ )?

## **When people have prior experience**

- Default is shaped by memory: what one usually experiences
  - e.g., *maintaining status quo*

## **When people have no prior experience**

- Less clear
- Probably, related to simple heuristics that 'usually work'
  - e.g., *choosing the middle-ground*

# When is noisy approximation stronger?

## When aggregating trade-offs is difficult

- More noise when far from dominance
  - e.g., *providing additional labour hour when payoff is 2 EUR than when it is 200 EUR*
- More noise when more dimensions to consider and dimension-by-dimension dissimilarity
  - e.g., *A arrives later, is superior, is costlier, is more econ-friendly than B*

## When the problem is less important

- More noise when people incur in less thinking about a problem (e.g., rational inattention)
  - e.g., *snack vs mobile phone purchase*
  - Determinants: relevance of decision, frequency of decision



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# Comparative Thinking

**People avoid aggregating across dimensions** and compare within-dimensions

- e.g., *'I prefer mobile A because it has better camera and battery-life, while B only is cheaper'*
- e.g., *'I will buy car C because it looks nicer and is cheaper, while D only is more efficient'*
- e.g., *'I study E because it is easier and more interesting, while F only pays more'*

# Why do people do this?

- Assessments are typically **relative** rather than absolute
    - Compare relevant quantities with (relevant or irrelevant) reference points
  - Interpretations:
    - Reference-dependent utility functions (*leading interpretation*)
    - Simplification strategy (*alternative interpretation*)
      - Helps dealing with the difficulty of information processing across dimensions
      - Difficult to translate different dimensions into a 'common currency'
      - Relative assessments are easier than absolute assessments
- e.g., 'How much is this wine worth to me?' vs.  
'Is this wine better than the one I had yesterday?'

# Pairwise Comparison

- Consider two goods with two dimensions
  - e.g., *expensive high-quality wine and a cheap low-quality wine*
- Under neoclassical theory, equivalence between:
  - ① Compare Aggregations
    - 1. Aggregate components within each option → 2. Compare aggregated values across options
  - ② Aggregate Comparisons
    - 1. Compare component-by-component → 2. Aggregate these comparisons
- But people tend to follow (ii)
  - Ariely (2011): Eye-tracking in decision making
    - Frequency of within-dimension comparisons is higher and increases when the number of dimensions increases

## Reference points

- People compare utility-relevant outcomes with normatively irrelevant reference points
  - e.g., *status quo*, *what they usually get*, *what they expect to get*

# Why decisions are particularly sensitive around reference points?

## 1 Difficulty of aggregating tradeoffs across dimensions

- People understand whether an outcome is better or worse than a comparison point, but not necessarily by how much
  - e.g., *Person's references for product A is mid-quality and very high-price. Prefers high-quality and high-price (gains in both) over low-quality and low-price (gains in one)*

# Why decisions are particularly sensitive around reference points?

## ② Efficient coding

- People have much experience around these points, and values are more precisely
  - However, this is not *per se* a reference-point comparison nor comparative thinking

# Why decisions are particularly sensitive around reference points?

## ③ Normalization

- Within-dimension differences matter more when relatively larger

### **Average-based**

→ e.g., *difference between 30 and 20 is larger than between 130 and 120*

### **Range-based**

→ e.g., *difference between 30 and 20 is larger when third item is 19 than when it is 0*

- People extrapolate relative difference to utility gains, overweighting dimensions



# Sequential contrast effects

- People hold quantities (or qualities) as larger if preceding one is smaller
  - e.g., *30 looks larger in (2,30) than in (29,30)*
  - Proven to have an impact in candidate assessment (Radbruch & Schiprowski, 2022), stock evaluations (Hartzmark & Shue, 2018)
  - Sequential contrast effects increase as tradeoffs become difficult (Enke & Graber, 2024)
- Prove-of-concept that reference point effects can be ultimately cognitive

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# Reduced Cardinality

- **People don't use all of the available information**

- In many problems, the dimension size is too large
- Simplification strategy: use a subset of information and decide with what is top of mind
  - e.g., *selective attention or memory*

# Why they do this?

## 1 Goal-driven process

- People attend/remember the **most important** elements
- Literature on rational inattention, sparsity, optimal bounded memory
- Focus on specific problem at hand

## 2 Stimuli-driven process

- People attend/remember elements **cued by the environment**
- Can be optimal *on average*
  - Maybe a response to constraints in attention/memory
  - Focus on variance/similarity broadly makes sense

# Incomplete Representations

## System Neglect

- People excessively **focus on the visible 'output' rather than on the underlying data-generating process** (DGP)
  - Example: Belief updating with bimodal response
    - Rational agents: Focus on the DGP
    - Simplifiers: Equate observed signals with the underlying process
  - Drawing people's attention to the neglected aspect of the DGP impacts behavior
    - i.e., *selective attention*
- Extends to indirect effects:
  - People do not pay sufficient attention to how others' behavior is driven by fundamentals
  - People do not pay sufficient attention to how behavioral responses impact aggregates

# Incomplete Representations

## Data Neglect

- People simplify by **entirely ignoring certain problem aspects**
  - Example: Belief updating with multi-modal response
    - Rational agents: Focus on the DGP
    - Signal-neglect agents: Only focus on the base rate
    - Base-neglect agents: Only focus on the signal
  - Non-rational agents only pay attention to one statistic
  - Drawing people's attention to the neglected aspect of the DGP impacts behavior
    - e.g., *selective attention*

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# Analogies and Categorization

**People repeat previous solutions** rather than solving the actual problem

- e.g., *'I will take route A because I took it last time and worked well'*
- e.g., *'I will buy car B because I have always bought cars from that company'*
- e.g., *'I will buy a Japanese mobile because I like Japanese films'*



# Why people do this?

## Model-free learning

- People don't form a mental model of the problem, they just learn purely by experience
  - e.g., 'I don't know why, but this works'
- People choose previously successful decisions for the same task
  - Main mechanism: reinforcement
  - **Problem 1:** most problems differ from each other
  - **Problem 2:** people do rely on model-based reasoning
- Extensions
  - Case-based reasoning, weighting past decisions by similarity to current environment
  - Dual-decision process, combining model-free with model-based learning

# Why people do this?

## Categorization

- People lump together current situations that are similar but differ
  - e.g., 'all Nordics speak North Germanic languages'
- People lump together observations into categories and then analyze categories as one
  - e.g., investors categorize as similar companies just because they report earnings same day or appear next to each other on reports, which makes stock move jointly (Charles, 2022).

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# Complexity Aversion

## **People undervalue what requires much information processing to evaluate**

- Similar to risk aversion to uncertainty resulting from imperfect information processing
  - e.g., 'picking which stock to investment in is too hard, so I avoid it'
  - e.g., 'economic news are difficult to understand, so I don't incorporate them to update my beliefs'
  - e.g., 'option A has too many caveats, so I prefer option B because is simpler'

# Source of complexity

## Cardinality

- Different states increase the complexity of assessing a decision
  - e.g., 'people shy away from products with many add-ons due to obfuscation' (Fehr & Wu, 2023)
  - e.g., 'financial assets with many distinct payouts tend to be avoided'

## Tradeoffs

- People act cautiously
  - Uncertainty about derived utility makes for conservative assessments  
concave transformation of utils due to risk aversion
  - Can explain endowment effect, certainty effect, and present bias