

1. Zadatak

$$E_k = \frac{1}{2} (y_k - \sigma_k)^2$$

$$\text{izlaz: } \sigma_k = \frac{\sum_{i=1}^m \pi_i \cdot z_i}{\sum_{i=1}^m \pi_i}$$

pri čemu je

$$\pi_i = \alpha_i \cdot \beta_i$$

$$\alpha_i = \frac{1}{1 + e^{b_i(x - a_i)}}$$

$$\beta_i = \frac{1}{1 + e^{d_i(y - c_i)}}$$

$$\psi(t+1) = \psi(t) - \eta \frac{\partial E_k}{\partial \psi}$$

a_i

$$\frac{\partial E_k}{\partial a_i} = \frac{\partial E_k}{\partial \sigma_k} \cdot \frac{\partial \sigma_k}{\partial \pi_i} \cdot \frac{\partial \pi_i}{\partial \alpha_i} \cdot \frac{\partial \alpha_i}{\partial a_i}$$

$$= -(y_k - \sigma_k) \cdot \frac{z_i \sum_{j=1}^m \pi_j - \sum_{j=1}^m \pi_j z_j}{\left(\sum_{j=1}^m \pi_j\right)^2} \cdot \beta_i \cdot \alpha_i (1 - \alpha_i) \cdot b_i$$

b_i

$$\frac{\partial E_k}{\partial b_i} = \frac{\partial E_k}{\partial \sigma_k} \cdot \frac{\partial \sigma_k}{\partial \pi_i} \cdot \frac{\partial \pi_i}{\partial \alpha_i} \cdot \frac{\partial \alpha_i}{\partial b_i}$$

$$= -(y_k - \sigma_k) \cdot \frac{z_i \sum_{j=1}^m \pi_j - \sum_{j=1}^m \pi_j z_j}{\left(\sum_{j=1}^m \pi_j\right)^2} \cdot \beta_i \cdot \alpha_i (1 - \alpha_i) (a_i - x)$$

c_i

$$\frac{\partial E_k}{\partial c_i} = \frac{\partial E_k}{\partial \sigma_k} \cdot \frac{\partial \sigma_k}{\partial \pi_i} \cdot \frac{\partial \pi_i}{\partial \beta_i} \cdot \frac{\partial \beta_i}{\partial c_i}$$

$$= -(y_k - \sigma_k) \cdot \frac{z_i \sum_{j=1}^m \pi_j - \sum_{j=1}^m \pi_j z_j}{\left(\sum_{j=1}^m \pi_j\right)^2} \cdot \alpha_i \cdot \beta_i (1 - \beta_i) d_i$$

d_i

$$\frac{\partial E_k}{\partial d_i} = \frac{\partial E_k}{\partial \sigma_k} \cdot \frac{\partial \sigma_k}{\partial \pi_i} \cdot \frac{\partial \pi_i}{\partial \beta_i} \cdot \frac{\partial \beta_i}{\partial d_i}$$

$$= -(y_k - \sigma_k) \cdot \frac{z_i \sum_{j=1}^m \pi_j - \sum_{j=1}^m \pi_j z_j}{\left(\sum_{j=1}^m \pi_j\right)^2} \cdot \alpha_i \cdot \beta_i (1 - \beta_i) (c_i - y)$$



(1i)

$$\frac{\partial E_k}{\partial p_i} = \frac{\partial E_k}{\partial \sigma_k} \cdot \frac{\partial \sigma_k}{\partial z_i} \cdot \frac{\partial z_i}{\partial p_i} = -(y_k - \sigma_k) \cdot \frac{\pi_i}{\sum_{j=1}^m \pi_j} \cdot x$$

(2i)

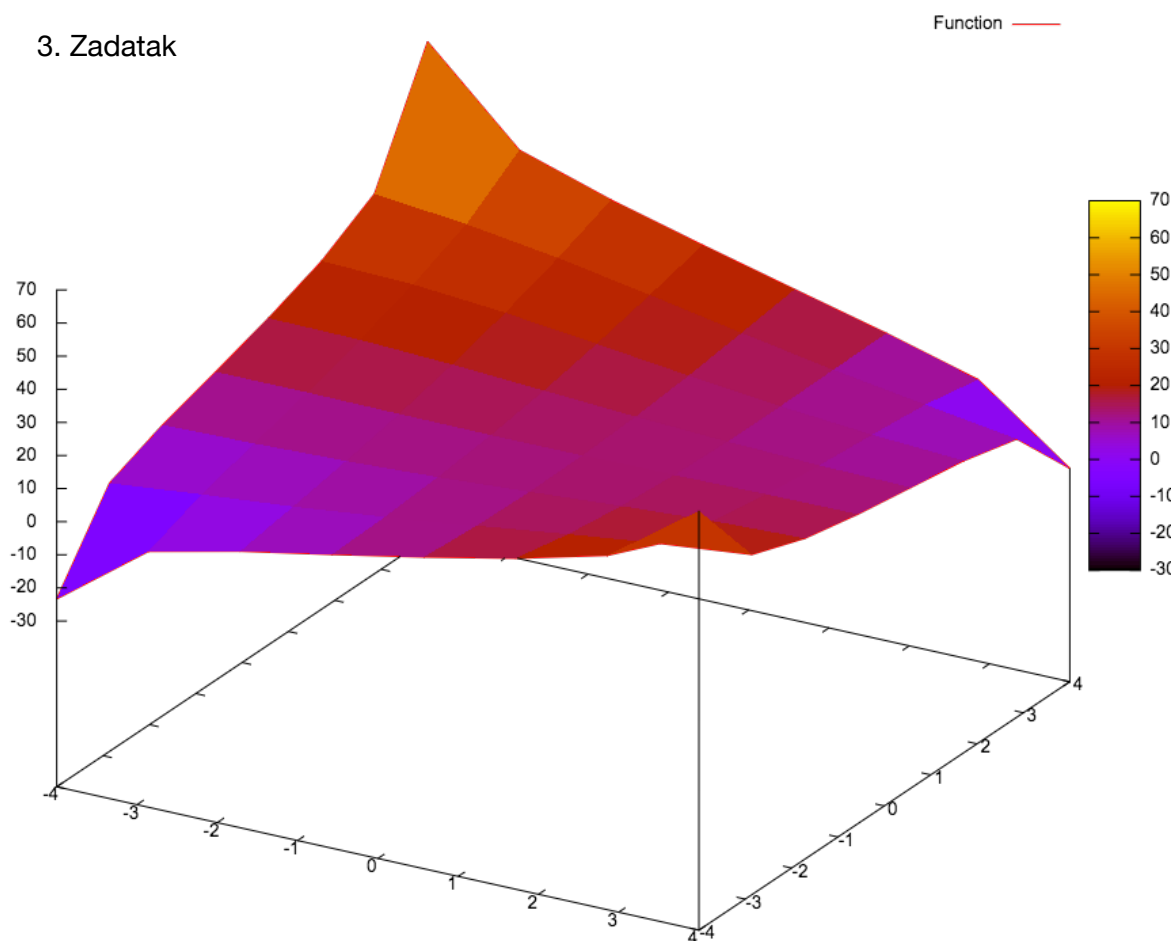
$$\frac{\partial E_k}{\partial f_i} = \frac{\partial E_k}{\partial \sigma_k} \cdot \frac{\partial \sigma_k}{\partial z_i} \cdot \frac{\partial z_i}{\partial f_i} = -(y_k - \sigma_k) \cdot \frac{\pi_i}{\sum_{j=1}^m \pi_j} \cdot y$$

(3i)

$$\frac{\partial E_k}{\partial r_i} = \frac{\partial E_k}{\partial \sigma_k} \cdot \frac{\partial \sigma_k}{\partial z_i} \cdot \frac{\partial z_i}{\partial r_i} = -(y_k - \sigma_k) \cdot \frac{\pi_i}{\sum_{j=1}^m \pi_j}$$

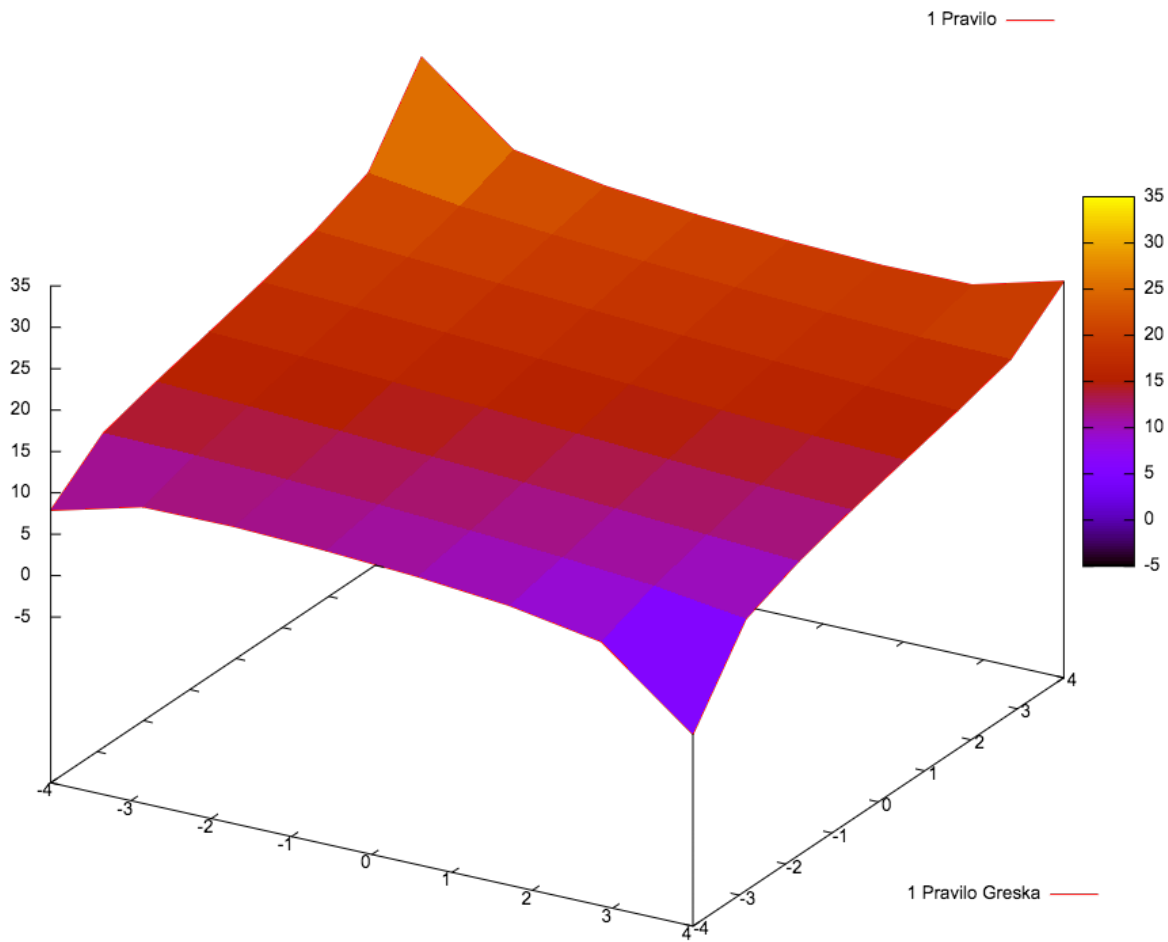
↳ stohastički, za pravi gradijentni spust se dodaje $\sum_{i=1}^n$ na svakom koraku
(gradijent se računa za sve dostupne primjere te se potom radi
o njegovoj vrijednosti)

3. Zadatak

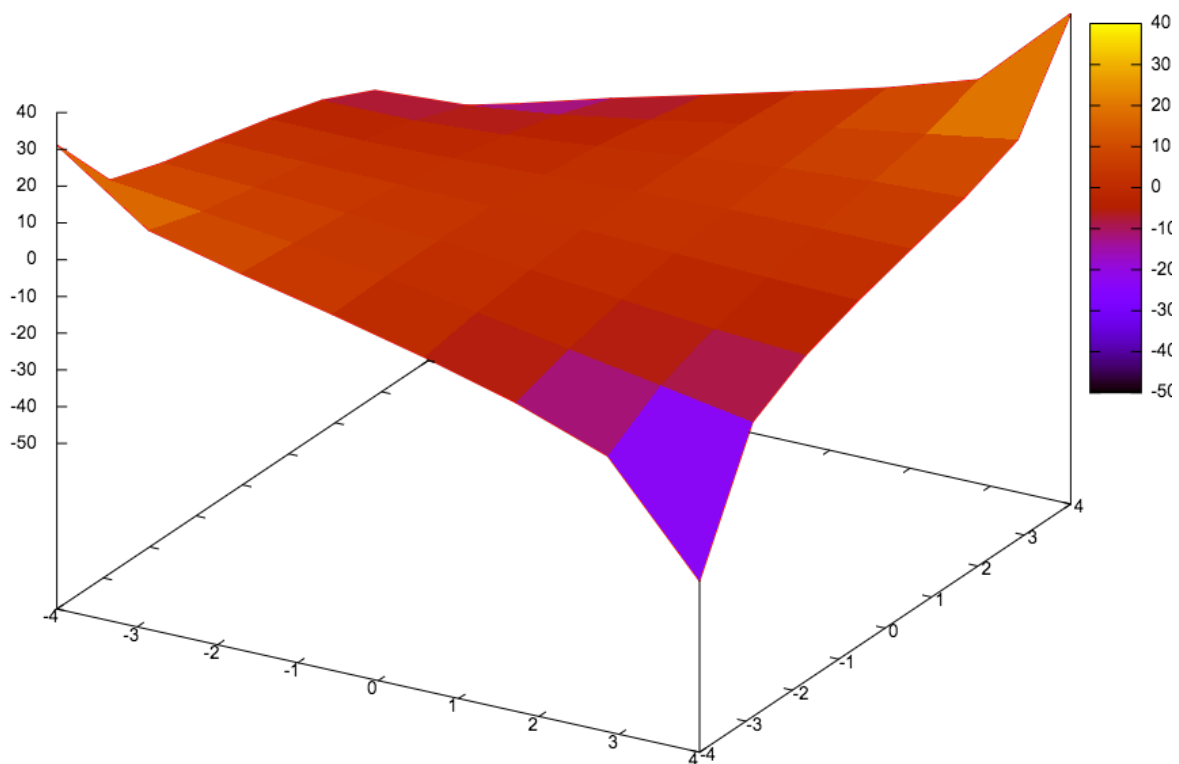


4. Zadatak

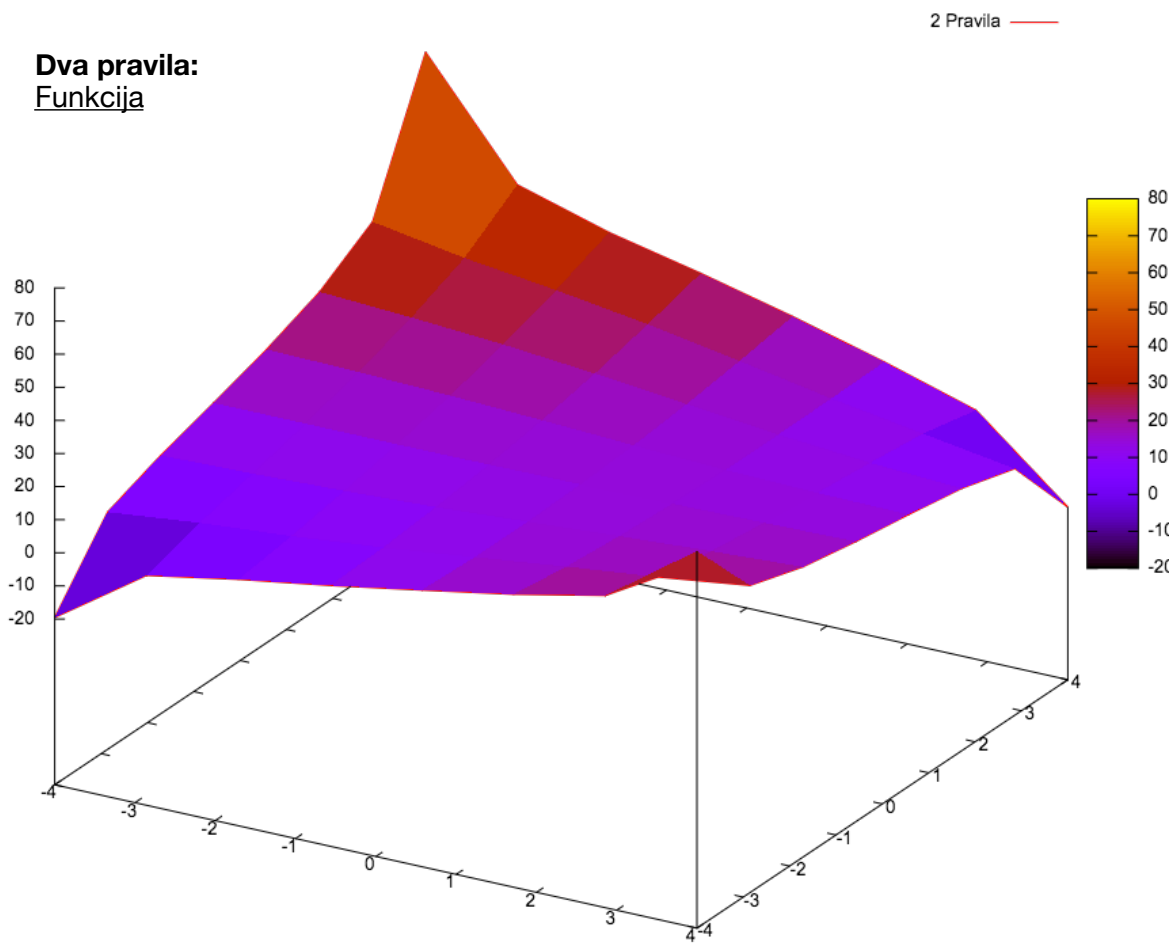
Jedno pravilo Funkcija



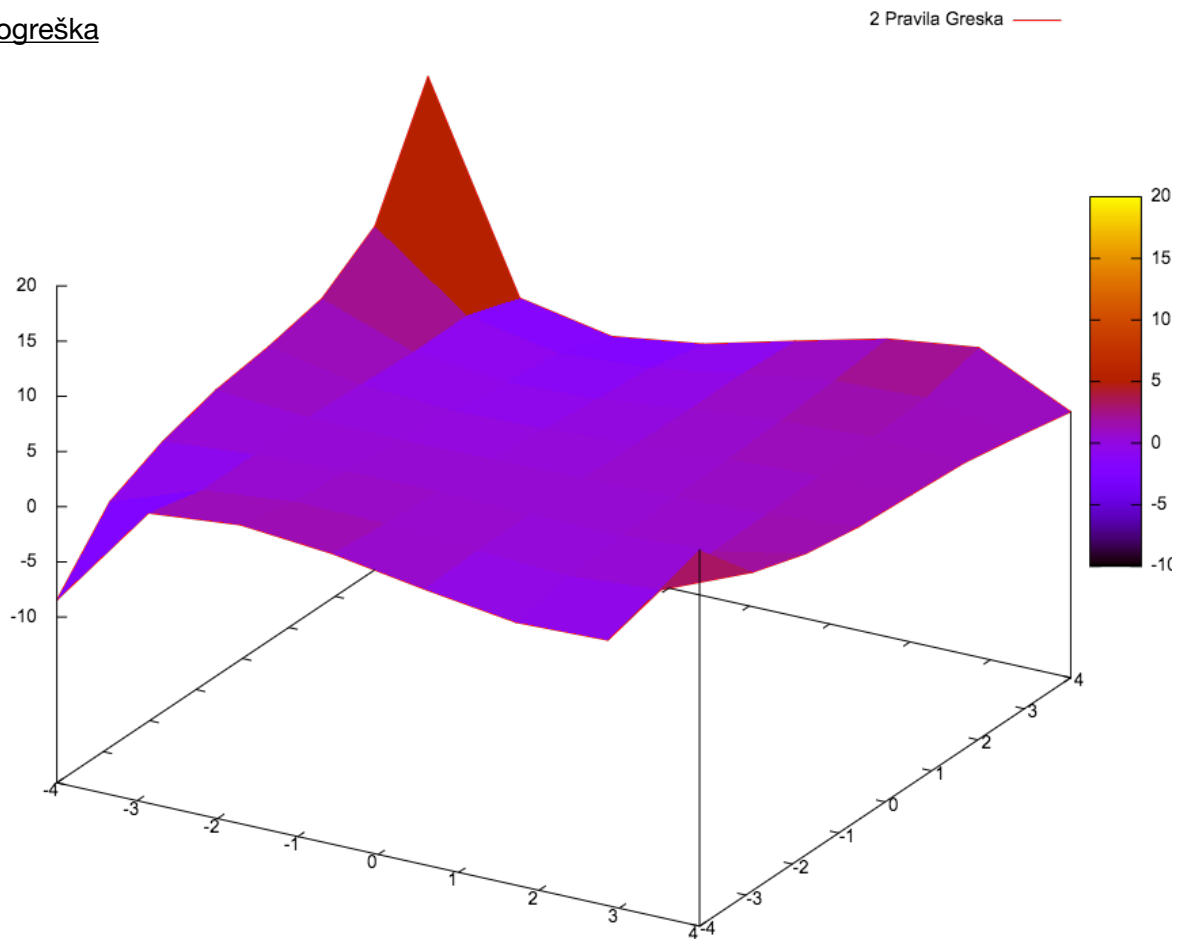
Pogreška



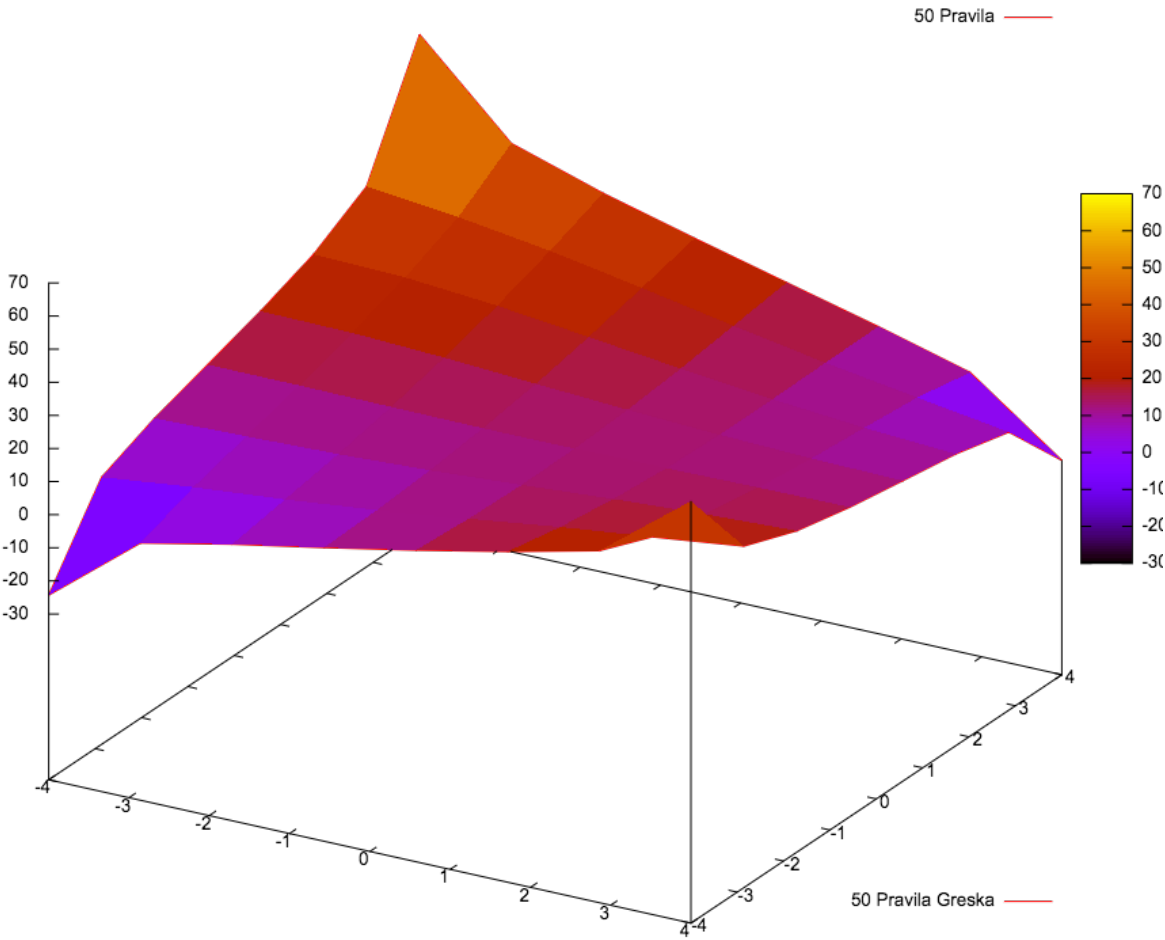
Dva pravila:
Funkcija



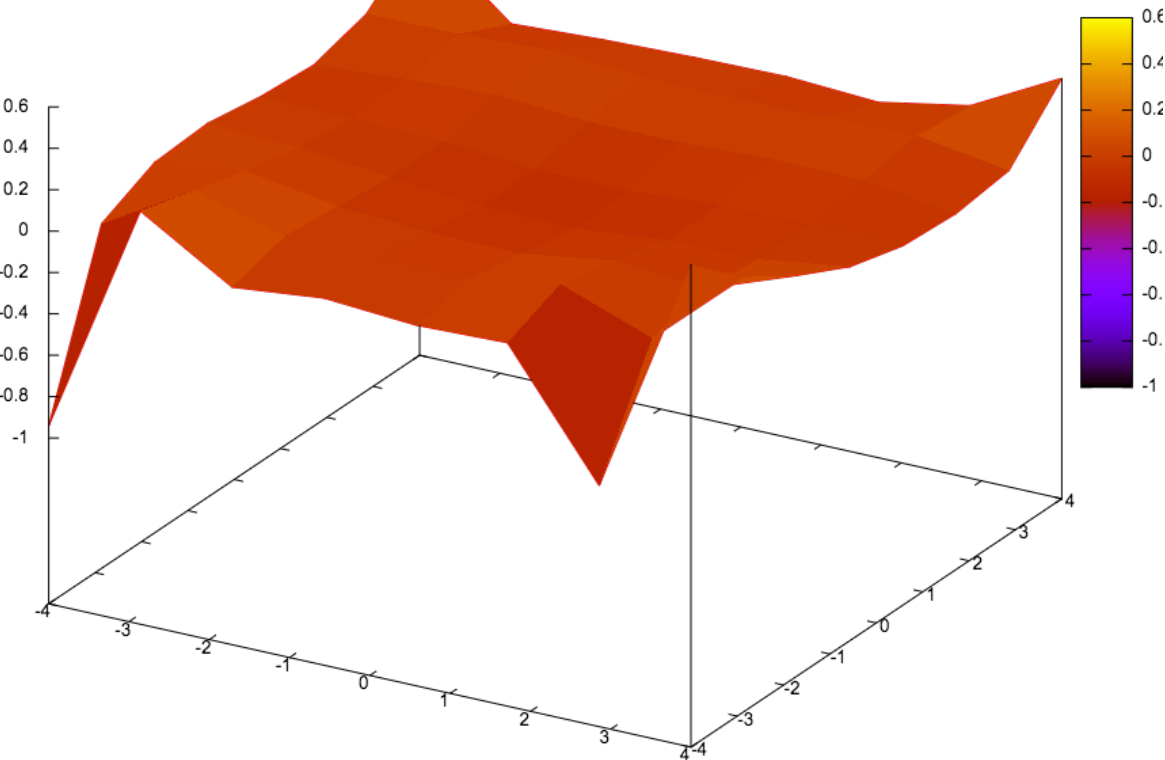
Pogreška



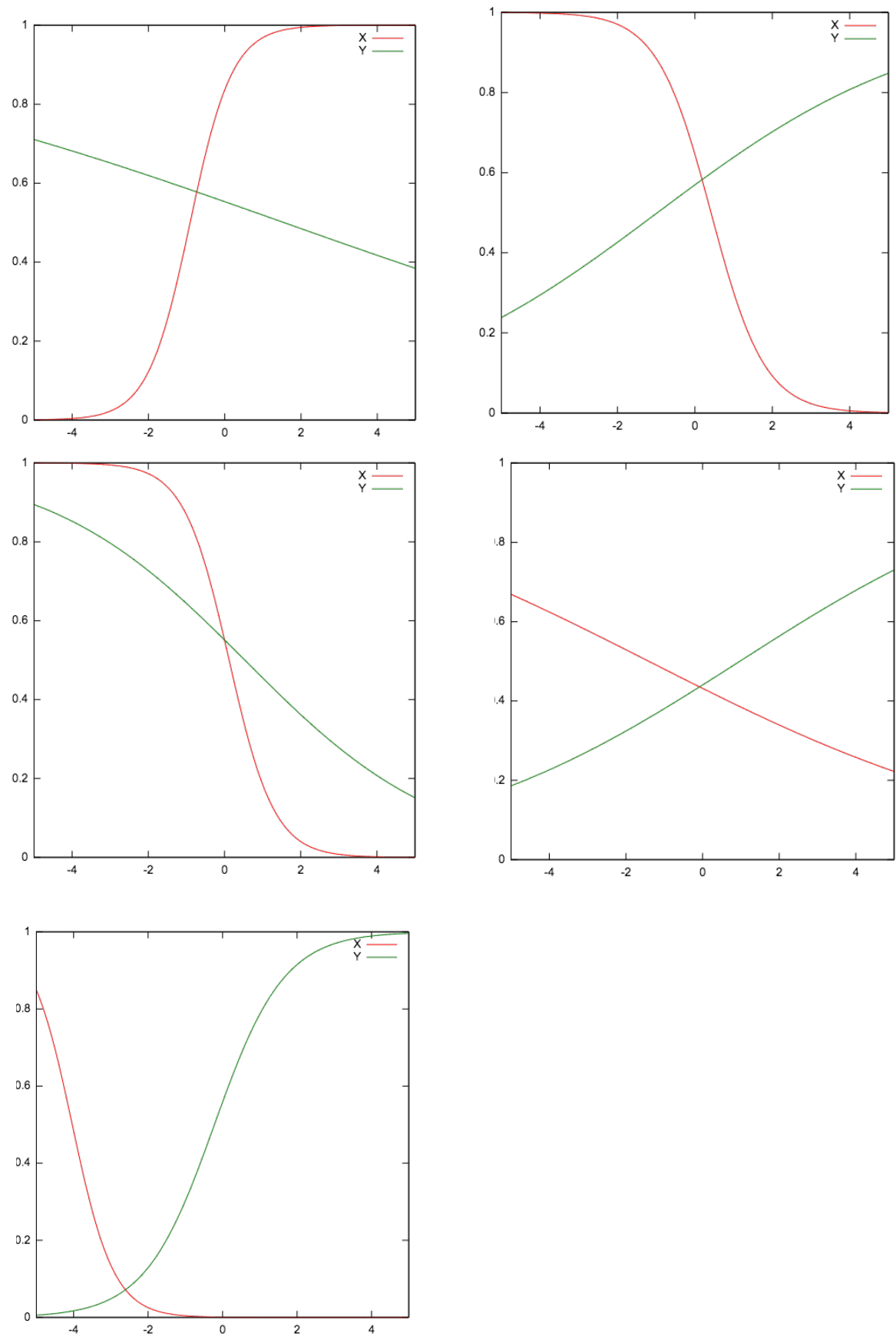
50 pravila
Funkcija



Pogreška

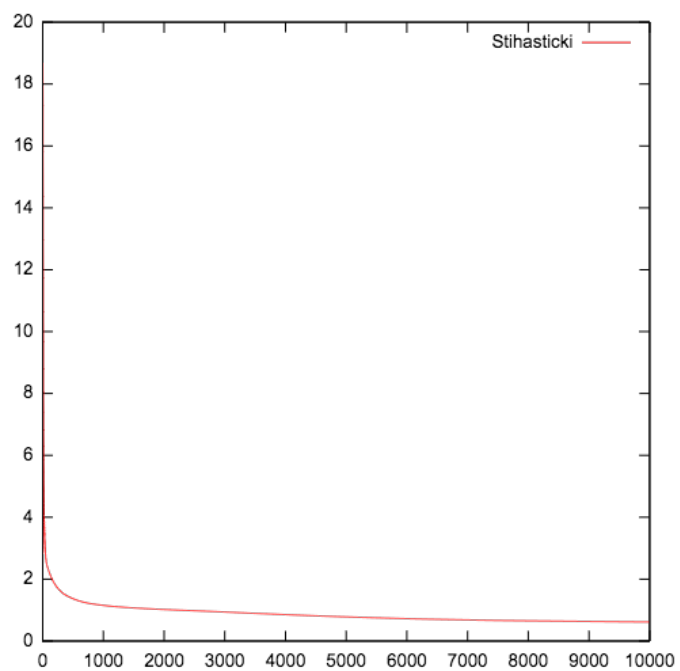


5. Zadatok

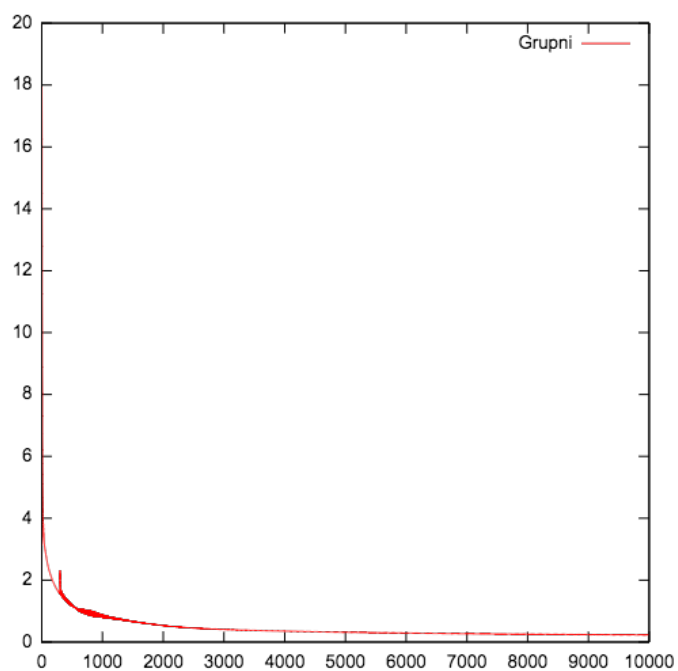


7. Zadatak

Stohastički

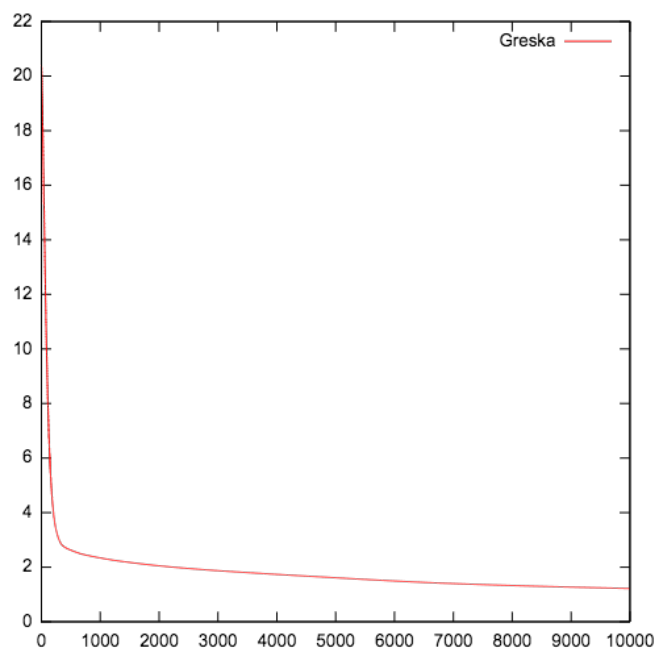


Grupni

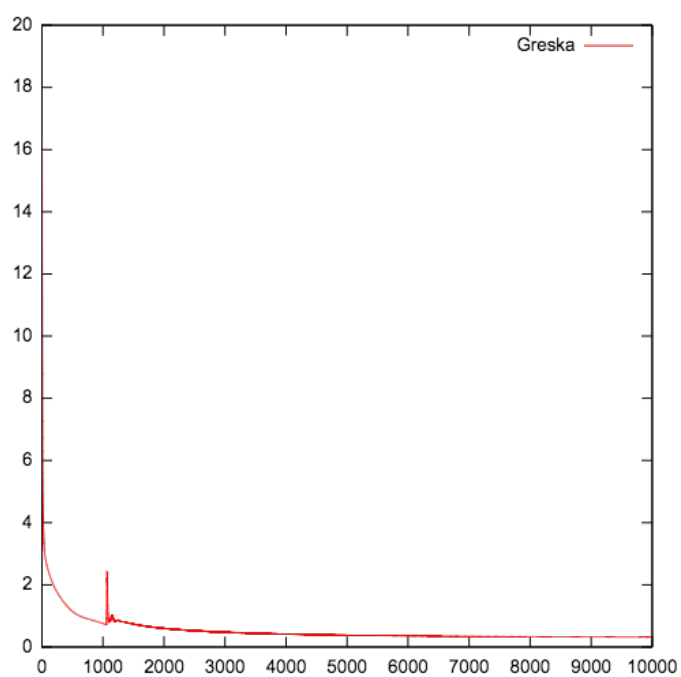


8. zadatak
Grupni

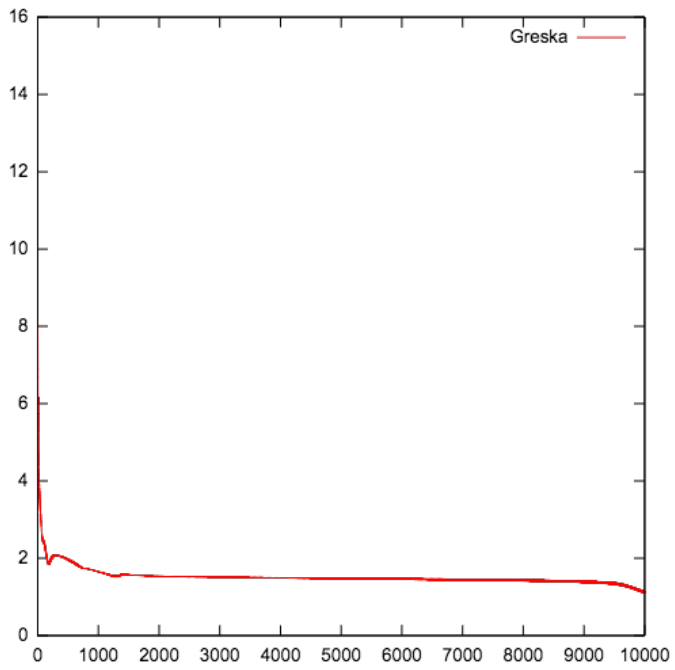
Vrlo mala



Prikladna

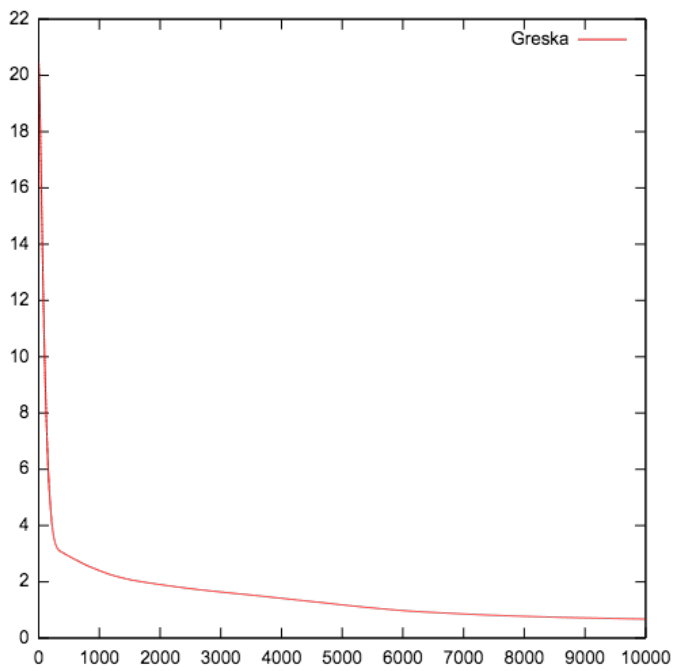


Prevelika

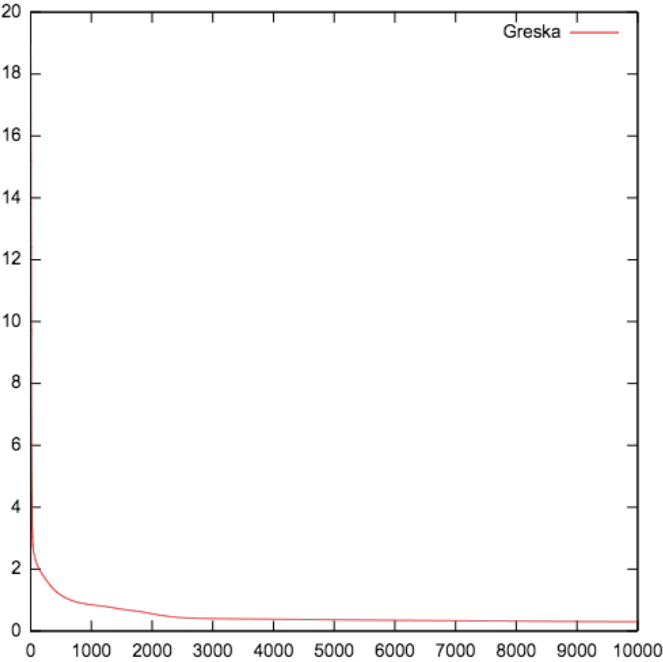


Stohastički

Vrlo mala



Prikladna



Velika

