



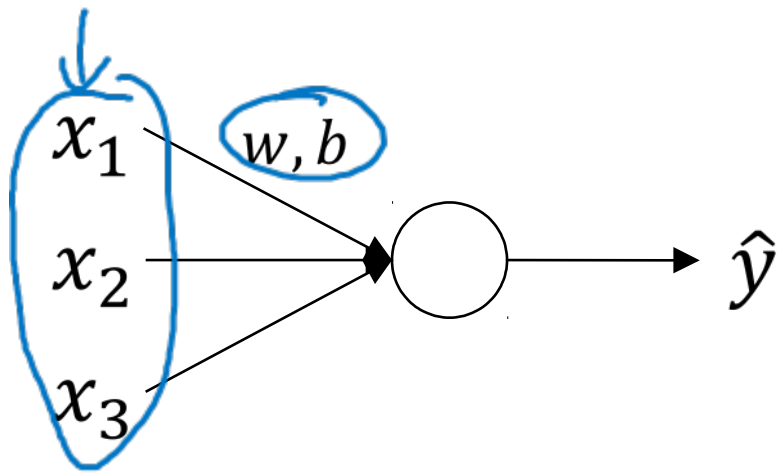
**deeplearning.ai**

# Batch Normalization

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Normalizing  
activations  
in a network

# Normalizing inputs to speed up learning

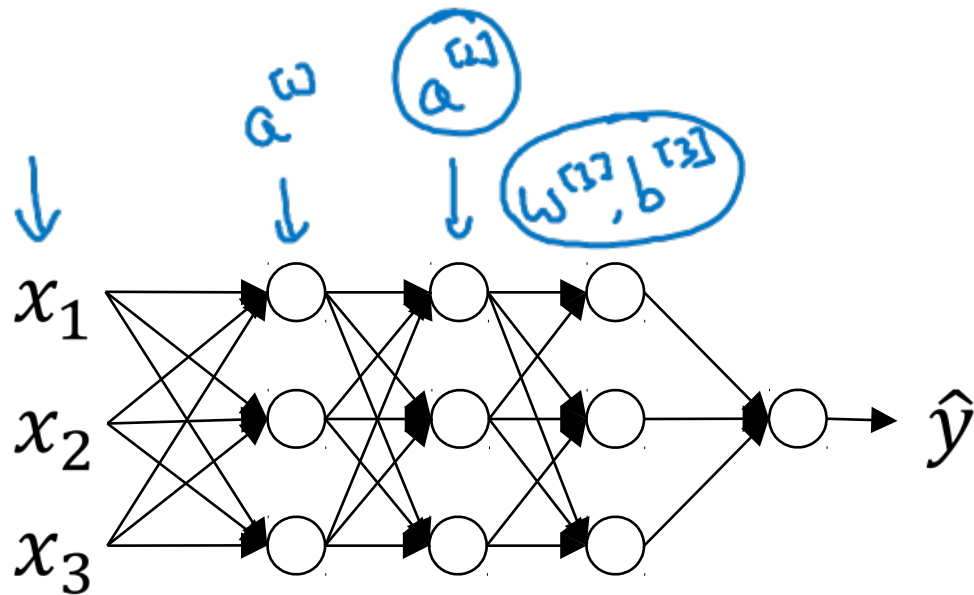


$$\mu = \frac{1}{n} \sum_i x^{(i)}$$

$$X = X - \mu$$

$$\sigma^2 = \frac{1}{n} \sum_i x^{(i)2} \quad \leftarrow \text{element-wise}$$

$$X = X / \sigma^2$$



Can we normalize  $\frac{a^{[2]}}{w^{[2]}, b^{[2]}}$  so fast?

Normalize  $\frac{z^{[2]}}{\uparrow}$

# Implementing Batch Norm

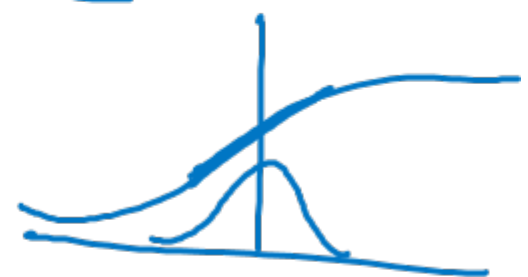
Given some intermediate values in NN

$$\underbrace{z^{(1)}, \dots, z^{(m)}}_{z^{[l]}(i)}$$

$$\left[ \begin{array}{l} \mu = \frac{1}{m} \sum_i z^{(i)} \\ \sigma^2 = \frac{1}{m} \sum_i (z^{(i)} - \mu)^2 \\ z_{\text{norm}}^{(i)} = \frac{z^{(i)} - \mu}{\sqrt{\sigma^2 + \epsilon}} \end{array} \right. \leftarrow$$

$$\left[ \begin{array}{l} \text{If } \gamma = \sqrt{\sigma^2 + \epsilon} \\ \beta = \mu \\ \text{then } \hat{z}^{(i)} = z^{(i)} \end{array} \right. \leftarrow$$

$$\begin{array}{l} x \leftarrow \\ z^{(i)} \leftarrow \end{array}$$



learnable parameters of model.

Use  $\hat{z}^{(i)}$  instead of  $z^{(i)}$ .