

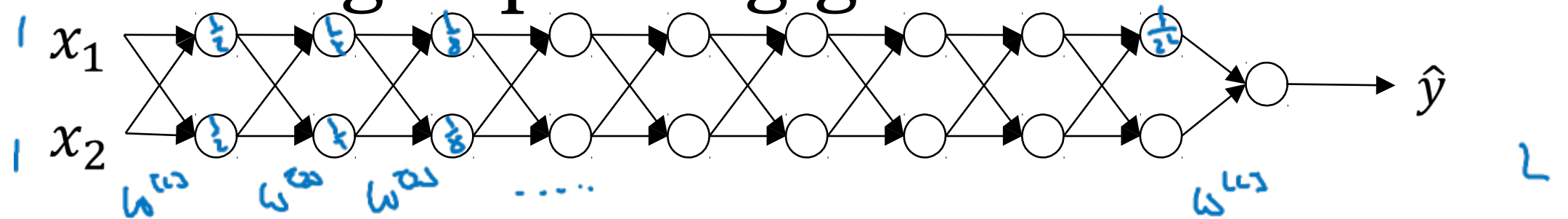


deeplearning.ai

Setting up your optimization problem

Vanishing/explo ding gradients

Vanishing/exploding gradients



$$g(z) = z \quad b^{u1} = 0$$

$$\hat{y} = w^{uL} \left(w^{u(L-1)} w^{u(L-2)} \dots w^{u1} x \right)$$

$$a^{uL} = g(z^{uL}) = g(w^{uL} x)$$

$$1.5^L$$

$$0.5^L$$

$$w^{u1} > I$$

$$w^{u2} < I \quad \begin{bmatrix} 0.9 & \\ & 0.9 \end{bmatrix}$$

$$w^{u2} = \begin{bmatrix} 0.5 & 0 \\ 0 & 0.5 \end{bmatrix}$$

$$z^{u1} = w^{u1} x$$

$$a^{u1} = g(z^{u1}) = z^{u1}$$

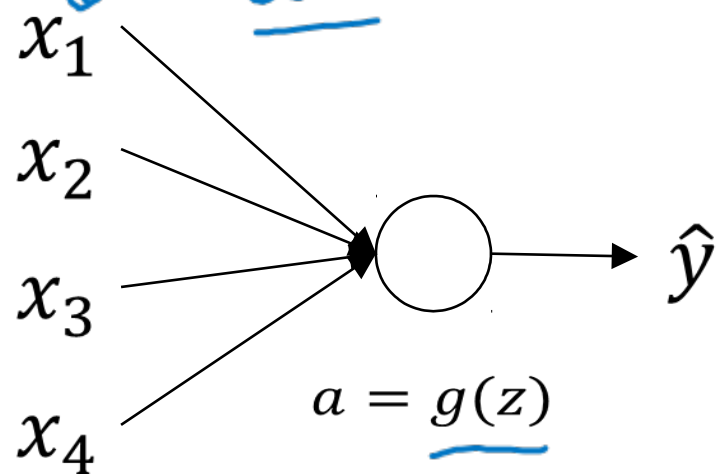
$$a^{u2} = g(z^{u2}) = g(w^{u2} a^{u1})$$

$$\hat{y} = w^{uL} \left[\begin{matrix} 0.5 & 0 \\ 0 & 0.5 \end{matrix} \right]^{L-1} x$$

$$1.5^{L-1} x$$

$$0.5^{L-1} x$$

Single neuron example



$$z = w_1 x_1 + w_2 x_2 + \dots + w_n x_n$$

large $n \rightarrow$ smaller w_i

$$\text{Var}(w_i) = \frac{1}{n} \cdot \frac{2}{n}$$

$$\underline{w}^{[1]} = \text{np.random.randn}(\text{shape}) * \text{np.sqrt}\left(\frac{2}{n^{[1-1]}}\right)$$

ReLU $g^{[2]}(z) = \text{ReLU}(z)$

Other variants:

$$\text{tanh} \quad \frac{1}{n^{[1-1]}}$$

Xavier initialization \uparrow

$$\sqrt{\frac{2}{n^{[1-1]} + n^{[1]}}}$$

\uparrow