

# Hands-On Machine Learning: summary

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# Chapter 10: Artificial Neural Networks

Artificial neural networks (ANNs): Machine learning model inspired by networks of biological neurons. They are at the very core of Deep Learning: versatile, powerful and scalable.

## 0.1 From Biological to Artificial Neurons

Reasons to believe this wave of interest in ANNs is more profound:

- Huge quantity of data available to train & ANNs outperform other ML technologies in large & complex problems
- Tremendous increase in computing power since the 90s + GPU & cloud platforms
- Training algorithms have improved (by small tweaks with huge impact)
- Theoretical limitations have been mostly rare in practice
- ANNs seem to have entered a virtuous cycle of funding & progress

### 0.1.1 Biological neurons

Individual biological neurons seem to behave in a simple way, but are organized in a network of billions, each connected to thousands of others. Highly complex computations can emerge from their combined efforts. It appears that biological neurons are organized in consecutive layers, especially in the cerebral cortex.

### 0.1.2 Logical computations with neurons

The first artificial neurons had only binary inputs & one binary output. Each neuron's output is active if more than a certain number of inputs are. A network like this can compute complex logical expressions.

### 0.1.3 The Perceptron

The *perceptron* is a simple ANN architecture composed by a single layer of threshold logic unit neurons. Their inputs and output are now real numbers; each input connection is associated with a weight. The TLU computes a weighted sum of its inputs ( $z = \mathbf{x}^\dagger \mathbf{w}$ ) and then applies a *step function*. Its output is thus  $h_{\mathbf{w}}(\mathbf{x}) = \text{step}(z)$ .

A single TLU can be used for simple linear binary classification. The perceptron contains a layer of TLUs. each *fully connected* to all inputs and also containing a *bias* term. It can thus perform multi-output binary classification:  $h_{w,i} = \phi(\mathbf{X}\mathbf{W} + \mathbf{b})$ , where  $\phi$  is the activation function (step for TLUs),  $\mathbf{X}$  is the input matrix ( $n_{\text{instances}} \times n_{\text{features}}$ ),  $\mathbf{W}$  is the weights matrix ( $n_{\text{features}} \times n_{\text{neurons}}$ ), and  $\mathbf{b}$  is the bias vector ( $n_{\text{neurons}}$ ).

The training is done in a way to reinforce connections that help reduce the error. The perceptron receives one training instance at a time, and for each wrong output neuron, reinforces weights from inputs that would have contributed to the correct prediction:

$$w_{i,j}^{\text{next}} = w_{i,j} + \underbrace{\eta}_{\text{learning rate}} \underbrace{(y_j - \hat{y}_j)}_{0 \text{ or } 1} x_i$$

If the training instances are *linearly separable*, the algorithm is proven to converge to a (non unique) solution. Contrary to logistic regression, these perceptrons do not output a class probability.

Limitations of perceptrons (such as the XOR problem) can be eliminated by stacking multiple layers

### 0.1.4 The Multilayer Perceptron and Backpropagation

A MLP is comprised of an input layer, an output layer and several *hidden* layers. Each layer except for the output) is fully connected (layers close to the input are called *lower*).

The training algorithm is known as **backpropagation**: gradient descent with an efficient technique for computing gradients automatically (*autodiff*). In a forward and a backward pass, the algorithm is able to compute the gradient with respect to every model parameter.

#### Algorithm breakdown

1. Handles one mini-batch at a time, and goes through full training set multiple times (each pass is called an *epoch*).
2. For each instance in the mini-batch, the output is computed in a *forward-pass* (intermediate results from all layers are preserved since they are needed for the backward pass).
3. The output error is measured using the loss function
4. Then it computes each output connection's contribution to the error. This is done analytically using the chain rule.
5. It now calculates the error contributions from the weights on the layer below (also with the chain rule); this is repeated working backwards to the input layer
6. Finally, a gradient step is performed to update all weights

It is important that all weights be initialized randomly, or else the training will fail (a *symmetry breaking* is required).

In order for the algorithm to work, the step function must be smoothed to have a well-defined non-zero derivative, thus allowing GD to make some progress at every step. A first replacement is the sigmoid function  $\sigma(z) = \frac{1}{1 + \exp(-z)}$

**Other choices:**

- $\tanh(z) = 2\sigma(2z) - 1$ ; similar to the logistic, but with output in  $[-1, 1]$ . This tends to make each output mostly centered around 0 at the beginning of training, which helps speed up the convergence.
- $\text{ReLU}(z) = \max(0, z)$ ; derivative jumps at  $z = 0$ , which can make GD bounce; but works well and is very fast to compute. Its unbounded image helps reduce some issues during GD.

Nonlinearities introduced by activation functions are essential to the complexity of the model. A large enough DNN can theoretically approximate any continuous function.

**0.1.5 Regression MLPs**

One output neuron per output dimension (*e.g.*: 2 for locating the center of an object in an image; another 2 for a bounding box (height and width)). Usually no activation at the output, except for  $\text{ReLU}/\text{softplus}(z) = \log[1 + \exp(z)]$  to restrict it to positive images; or  $\sigma/\tanh$  to bound it.

Training loss is typically MSE, or MAE/Huber (a combination of both) if there are many training outliers. The number of hidden layers is usually  $\sim 1 - 5$ , and the neurons per layer are  $\sim 10 - 100$ .

**0.1.6 Classification MLPs**

For each binary classification, a single output neuron with logistic activation is used, which can be interpreted as the estimated probability of the positive class.

For single output multiclass classification, an output neuron per class is needed, and a softmax activation for the whole layer (which estimates each class' probability)

The training loss function is generally multiclass cross-entropy. The rest of the architecture is broadly the same as with regression.

**0.2 Implementing MLPs with Keras**

Keras is a high-level Deep learning API with several backends. TensorFlow comes bundled with its own implementation, `tf.keras`, which has many advantages (*e.g.* TF's Data API to load and preprocess data efficiently).

**0.2.1 Building an image classifier using the Sequential API**

We use Fashion MNIST (70k grayscale  $28 \times 28$  images, 10 classes). Since we will be using GD, we scale the input features.

**Creating the model** `model = keras.models.Sequential()` is the simplest model, for a single stack of layers connected sequentially

`model.add(keras.layers.Flatten(input_shape = [28,28]))` converts the image to a 1D array.

As is the first layer, we must pass the `input_shape` (for a single instance)

`model.add(keras.layers.Dense(#neurons, activation = 'relu'))`

Instead of adding layers by one, it is possible to pass them as a list to the `Sequential` constructor.

### 0.2.1.1 Inspection

`model.summary()` displays the layers (by name), along with their parameters. `model.layers` returns them as a list, but they can also be called by name as `model.get_layer('dense')`. Its parameters can be retrieved by `weights`, `biases = layer.get_weights()`. For a custom initialization, when creating the layer we can set `kernel_initializer` or `bias_initializer`.

### 0.2.1.2 Compiling the model

The method must be called to specify the loss function and optimizer:

`model.compile(loss = 'sparse_categorical_crossentropy', optimizer = 'sgd', metrics = ['accuracy'])`. The `metrics` arg corresponds the list of metrics to be computed during training and evaluation. The loss function here is due to exclusive classes and the class given by a single index (this is considered *sparse*). If class were given by a one-hot vector instead, we use `categorical_crossentropy`. To convert sparse to one-hot, `keras.utils.to_categorical()`

### 0.2.1.3 Training and evaluating

`history = model.fit(X_train, y_train, epochs, validation_data = (X_val, y_val))`  
With class imbalance, we can set the `class_weights` (and even `sample_weight`) arguments in the `fit` method.

The `fit` method returns a `History` object with the training parameters (`history.params`) and a dictionary `history.history` containing the loss and metrics computed during training. This can be easily put in a dataframe to plot the learning curve (the training curve should be shifted to the left by half an epoch). The `fit` method resumes training from last state if called multiple times.

To increase performance, the first hyperparameter to be tuned should be the learning rate; if that doesn't help, changing the optimizer. After that, the architecture and activation functions. Finally, we can evaluate the model with `model.evaluate(X_test, y_test)`

## 0.2.2 Building complex models using the Functional API

To build models with more complex topologies, multiple inputs or outputs, keras offers the Functional API. Each layer must be defined as a separate object, specifying its input

`input_ = keras.layers.Input(shape=[...])` an `Input` object must be defined (even more than one if necessary)

`hidden = Dense(neurons, activation = 'relu')(input_)` the input to this layer is passed by calling it as a function

`concat = keras.layers.Concatenate()([input_, hidden])` layer which concatenates inputs  
`model = keras.Model(inputs = [input_], outputs = [output])` we create the model, specifying input(s) and output(s). The model can then be compiled and trained.

With multiple inputs, the `fit` method must be supplied with a tuple (or dictionary) of input matrices. Multiple outputs may be needed in many cases:

- The task may demand it; as in object location and identification (regression for a bounding box, classification to identify).
- Multiple independent tasks on the same data; the network can learn features in the data that are useful across tasks.

- It can be used as a regularization technique, for example, by adding an auxiliary output from middle layers, to ensure the underlying part learn something useful.
- Each output needs its own loss function. These will be added to obtain the total loss used in training. The losses will be passed as a list to the `fit` method, along with a list of `loss_weights` to perform a weighted sum instead. As with inputs, a tuple of targets must be supplied.

### 0.2.3 Using the Subclassing API to build dynamic models

To create models with even greater flexibility (e.g. loops, varying shapes, dynamical behaviours), we may use the subclassing API:

```
class CustomModel(keras.Model):           #inherit from base class

    def __init__(self, ..., **kwargs):
        super().__init__(**kwargs)      #handles standard args(e.g. name)
        # all layers should be created in the constructor
        self.hidden = ...

    def call(self, inputs):
        # all computations performed here (input need not be created,
        # just passed to the call method)
        ...
        return outputs
```

The extra flexibility's cost is that the model architecture is hidden in `call`, so keras cannot easily inspect it, save it or clone it.

Keras models can be used like regular layers to combine them.

### 0.2.4 Saving and restoring a model

With the Sequential or Functional API, a model can be saved to HDF5 using `model.save(fname)`. This saves the architecture, parameters for every layer and optimizer.

It can be loaded using `keras.models.load_model`

This won't work with subclassing, but model parameters can be saved with `save_weights` (also loaded with `load_weights`).

### 0.2.5 Using Callbacks

The `fit` method accepts a list of objects in the `callbacks` argument, which will be called at the start and end of training, or each epoch or batch.

#### 0.2.5.1 Model checkpoint

`checkpoint_cb = keras.callbacks.ModelCheckpoint(fname, save_best_only=True)` the callback saves the model at regular intervals during training (by default at the end of each epoch).

`save_best_only=True` will only make the checkpoint when the performance on the validation set is the best so far.

### 0.2.5.2 Early Stopping

`early_stopping_cb = keras.callbacks.EarlyStopping(patience)` will interrupt training when it measures no progress on validation during a number of epochs (given by `patience`). The best model can be restored enabling `restore_best_weights=True`.

### 0.2.5.3 Custom Callbacks

We can create callbacks by inheriting from the base class

```
class CustomCallback(keras.callbacks.Callback):
    def on_epoch_end(self, epoch, logs):
        print(logs['val_loss'])
```

options include `on_train_end`, `on_batch_end`, etc. Also ones only with `evaluate`, `predict`.

## 0.2.6 Using TensorBoard for visualization

TensorBoard is an interactive visualization tool to view learning curves during training, compare them between runs, visualize the computation graph, training statistics & multidimensional data projected to 3D (and more).

To use it, the model must generate binary *event files*, The TB server monitors a log directory; it is useful to have a different subdir for each run. The TB callback must be used to generate the files:

```
tensorboard_cb = keras.callbacks.TensorBoard(run_logdir)
```

The server can be called with

```
%load_ext tensorboard
```

```
%tensorboard -logdir=./my_logs -port=6006
```

TF also has a low-level API to manually write logs (`tf.summary`)

## 0.3 Fine-tuning neural network hyperparameters

The main drawback of the flexibility of ANNs is the number of hyperparameters to tweak. There are some options to find the best combination.

One option is to try many combinations using grid or random search and measuring on the validation set (or using k-fold cross validation). To work with the scikit-learn API, we use a wrapper to treat models as sklearn estimators:

```
keras_reg = keras.wrappers.scikit_learn.KerasRegressor(build_model)
```

where `build_model` is function that takes a set of hyperparameters and returns a compiled model.

Random search works well for fairly simple problems, but when training is slow, it will only explore a tiny portion of hyperparameter space.

Other approaches “zoom in” when a region in the space turns out to be good; there are several libraries for this purpose

### 0.3.1 Number of hidden layers

For simple problems, a single hidden layer may be enough; but for complex problems, deep networks have a much higher *parameter efficiency* than shallow ones: they can model complex functions using exponentially fewer neurons.

Deep networks can model the hierarchical structure of data: lower layers encode low-level features, and higher layers combine them to model high-level, more abstract structures (*e.g.* from line segments to faces). This can also help the model generalize to other datasets. For example, we may reuse the lower layers from a model already trained to recognize faces to train a new model to recognize hairstyles