Sinus forkurs matte oppgaver

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1.10

a)

 $-5 \in \mathbb{Z}$

b)

 $-5 \notin \mathbb{N}$

c)

 $\frac{2}{3}\notin\mathbb{Z}$

d)

 $\frac{2}{3}\in\mathbb{Q}$

e)

 $\sqrt{5} \in \mathbb{R}$

f)

 $\sqrt{5} \notin \mathbb{Q}$

1.11

 $2 \in \{1,2,3,4\}$

 $3 \not \in \{0,1,2,4\}$

 $1,5 \not\in \{1,2,3,4\}$

 $-1 \notin \{-2,1,0,1\}$

$$\{0,2,4,6,8,10,12,14,16,18,20\}$$

$$\{21, 23, 25, 27, 29, 31, 33, 35\}$$

$$\{2, 3, 5, 7, 11, 13, 17, 19, 23, 29\}$$

1.13

$$\{1, 2, 3, 4\} \setminus \{4\} = \{1, 2, 3\}$$

$$\{1, 2, 3, 4\} \setminus \{2, 4\} = \{1, 3\}$$

$$\{1, 2, 3, 4\} \setminus \{1, 5\} = \{2, 3, 4\}$$

$$\mathbb{Z}\backslash\mathbb{N}=\{...,-4,-3,-2,-1,0\}$$

$$4 * 2^2 = 4 * 4$$
$$= 16$$

$$4 * (-2)^2 = 4 * 4$$
$$= 16$$

$$5 - 3^2 = 5 - 9$$
$$= -4$$

$$(5-3)^2 = 2^2$$
$$= 4$$

$$-2^2 + 3^2 - 2*(-2) = -4 + 9 + 4$$

= 9

$$-(-2)^2 + (-3)^2 - 2^2 = -(4) + 9 - 4$$
$$= 1$$

 $\mathbf{g})$

$$(-3)^2 + 5 * (-3) + 6 = 9 - 15 + 6$$

= -5 + 6
= 0

Oppgave 1.15

a)

$$2(7-5) + 2 = 2 * 2 + 2$$

= $4 + 2 = 6$

b)

$$-3(4-12) + 2 * 3^2 = -3 * -8 + 2 * 9$$

= 24 + 18 = 42

 $\mathbf{c})$

$$-(8-4) - (3)^2 = -4 - 9$$
$$= -13$$

d)

$$-2^{4} + 3(17 - 3^{2}) + (3 * 4^{2} - 2 * 5^{2}) = -2^{4} + 3 * 8 + (3 * 4^{2} - 2 * 5^{2})$$

$$= -2^{4} + 3(17 - 3^{2}) - 2$$

$$= -16 + 24 - 2$$

$$= 8 - 2$$

$$= 6$$

Oppgave 1.16

a)

$$2(2*2-2)^{2} = 2(4-2)^{2}$$

$$= 2*4$$

$$= 8$$

$$-2^6 + (-2)^6 = -64 + 64 = 0$$

$$\mathbf{c})$$

$$4(3-2)^3 - 3(2-3)^3 = 4 * 1 - 3 * (-1)$$
$$= 4 + 3$$
$$= 7$$

d)

$$4(2^{2} - 3)^{5} - 3(2^{3} - 3^{2})^{5} = 4 * 1^{5} - 3 * (-1)^{5}$$

$$= 4 * 1 - 3 * -1$$

$$= 4 - (-3)$$

$$= 4 + 3$$

$$= 7$$

Oppgave 1.17

$$2(2 * 2 - 2)^{2} = 2(4 - 2)^{2}$$
$$= 2 * 4$$
$$= 8$$

$$-2^6 + (-2)^6 = -64 + 64 = 0$$

$$4(3-2)^3 - 3(2-3)^3 = 4 * 1 - 3 * (-1)$$
$$= 4 + 3$$
$$= 7$$

$$4(2^{2} - 3)^{5} - 3(2^{3} - 3^{2})^{5} = 4 * 1^{5} - 3 * (-1)^{5}$$

$$= 4 * 1 - 3 * -1$$

$$= 4 - (-3)$$

$$= 4 + 3$$

$$= 7$$

Oppgave 1.20

 $\mathbf{a})$

$$\frac{4}{6} = \frac{4:2}{6:2} = \frac{2}{3}$$

b)

$$\frac{9}{15} = \frac{9:3}{15:3} = \frac{3}{5}$$

c)

$$\frac{18}{21} = \frac{18:3}{21:3}$$
$$= \frac{6}{7}$$

d)

$$\frac{42}{54} = \frac{42:6}{54:6}$$
$$= \frac{7}{9}$$

Oppgave 1.21

a)

$$\frac{72}{120} = \frac{72:8}{120:8}$$

$$= \frac{9}{15}$$

$$= \frac{9:3}{15:3}$$

$$= \frac{3}{5}$$

$$\frac{126}{294} = \frac{126:7}{294:7}$$

$$= \frac{18:2}{42:2}$$

$$= \frac{9:3}{21:3}$$

$$= \frac{3}{7}$$

$\mathbf{c})$

$$\frac{132}{198} = \frac{132:2}{198:2}$$

$$= \frac{66:3}{99:3}$$

$$= \frac{22:11}{33:11}$$

$$= \frac{2}{3}$$

d)

$$\frac{153}{51} = \frac{153:3}{51:3} = \frac{51}{17}$$

exmaples

$$3 * \frac{2}{3} = \frac{3}{1} * \frac{3}{3} - \frac{2}{3}$$

$$= \frac{7}{3} = \frac{3+3+1}{3}$$

$$= \frac{3}{3} + \frac{3}{3} + \frac{1}{3}$$

$$= 1 + 1 + \frac{1}{3} = 2\frac{1}{3}$$

$$\frac{1}{12} + \frac{4}{9} = \frac{9}{9} * \frac{1}{12} + \frac{4}{9} * \frac{12}{12}$$

$$= \frac{9}{108} + \frac{48}{108}$$

$$= \frac{57:3}{108:3}$$

$$= \frac{19}{36}$$

$$\frac{1}{12} * \frac{4}{9} = \frac{4:2}{108:2}$$
$$= \frac{2:2}{54:2}$$
$$= \frac{1}{27}$$

$$\frac{1}{12} : \frac{4}{9} = \frac{1}{12} * \frac{9}{4}$$
$$= \frac{9 : 3}{48 : 3}$$
$$= \frac{3}{16}$$

$$3 + \frac{5}{12} = \frac{3 * 12}{1 * 12} + \frac{5}{12}$$
$$= \frac{36}{12} + \frac{5}{12}$$
$$= \frac{41}{12}$$

$$3 * \frac{5}{12} = \frac{3}{1} * \frac{5}{12}$$
$$= \frac{15:3}{12:3}$$
$$= \frac{5}{4}$$

$$3: \frac{5}{12} = \frac{3}{1}: \frac{5}{12}$$
$$= \frac{3}{1} * \frac{12}{5}$$
$$= \frac{36}{5}$$

$$2*\left(\frac{3}{8} + \frac{1}{4}\right) = 2*\left(\frac{4}{4} * \frac{3}{8} + \frac{1}{4} * \frac{8}{8}\right)$$

$$= 2*\left(\frac{12}{32} + \frac{8}{32}\right)$$

$$= 2*\frac{20}{32}$$

$$= \frac{2*20}{32}$$

$$= \frac{40:2}{32:2}$$

$$= \frac{20:2}{16:2}$$

$$= \frac{10:2}{8:2}$$

$$= \frac{5}{4}$$

$$\left(\frac{5}{6} - \frac{2}{9}\right) * \frac{3}{5} = \left(\frac{5*3}{6*3} - \frac{2*2}{9*2}\right) * \frac{3}{5}$$

$$= \left(\frac{15}{18} - \frac{4}{18}\right) * \frac{3}{5}$$

$$= \frac{11}{18} * \frac{3}{5}$$

$$= \frac{33:3}{90:3}$$

$$= \frac{11}{30}$$

$$\left(\frac{5}{36} + \frac{1}{12}\right) : \frac{2}{9} = \left(\frac{5}{36} + \frac{1*3}{12*3}\right) : \frac{2}{9}$$

$$= \left(\frac{5}{36} + \frac{3}{36}\right) : \frac{2}{9}$$

$$= \frac{8}{36} * \frac{9}{2}$$

$$= \frac{72}{72}$$

$$= 1$$

a)

$$\frac{\frac{2}{3}}{\frac{5}{6}} = \frac{\frac{2}{3} * \frac{6}{1}}{\frac{5}{6} * \frac{6}{1}}$$

$$= \frac{\frac{2}{3} * \frac{\cancel{6}_{1}}{1}}{\frac{\cancel{5}_{1}}{\cancel{6}_{2}} * \frac{\cancel{6}_{2}}{1}}$$

$$= \frac{\frac{4}{10}}{\frac{10}{2}}$$

$$= \frac{4}{5}$$

b)

$$\frac{\frac{21}{36}}{\frac{14}{45}} = \frac{21}{36} * \frac{45}{14}$$
$$= \frac{21}{36} * \frac{45}{14}$$
$$= \frac{21}{36} * \frac{45}{14}$$
$$= \frac{3}{4} * \frac{5}{2}$$
$$= \frac{15}{8}$$

$$\frac{\frac{3}{2} + \frac{5}{8}}{\frac{1}{4} + \frac{25}{2}} = \frac{\frac{3*8}{2*8} + \frac{5*2}{8*2}}{\frac{1*2}{4*2} + \frac{25*4}{2*4}}$$

$$= \frac{\frac{24}{16} + \frac{10}{16}}{\frac{2}{8} + \frac{100}{8}}$$

$$= \frac{\frac{34}{16}}{\frac{102}{8}}$$

$$= \frac{34}{16} * \frac{8}{102}$$

$$= \frac{34_1}{16_2} * \frac{8_1}{102_3}$$

$$= \frac{1}{2} * \frac{1}{3}$$

$$= \frac{1}{6}$$

d)

$$\frac{3 + \frac{4}{3}}{\frac{5}{12} + 5} = \frac{\frac{3*3}{1*3} + \frac{4*1}{3*1}}{\frac{5*1}{12*1} + \frac{5*12}{1*12}}$$

$$= \frac{\frac{9}{3} + \frac{4}{3}}{\frac{5}{12} + \frac{60}{12}}$$

$$= \frac{\frac{13}{3}}{\frac{65}{12}}$$

$$= \frac{13}{3} * \frac{12}{65}$$

$$= \frac{\cancel{13}_{12}}{\cancel{13}_{12}} * \cancel{\cancel{13}_{12}}$$

$$= \frac{1}{3} * \frac{\cancel{13}_{12}}{\cancel{13}_{12}}$$

$$= \frac{1}{3} * \frac{\cancel{13}_{12}}{\cancel{13}_{12}}$$

$$= \frac{\cancel{13}_{12}}{\cancel{13}_{12}} * \cancel{\cancel{13}_{12}}$$

$$= \frac{\cancel{13}_{12}}{\cancel{13}_{12}} * \cancel{\cancel{13}_{12}} * \cancel{\cancel{13}_{12}}$$

$$= \frac{\cancel{13}_{12}}{\cancel{13}_{12}} * \cancel{\cancel{13}_{12}} * \cancel{\cancel{13}_{12}}$$

$$= \frac{\cancel{13}_{12}}{\cancel{13}_{12}} * \cancel{\cancel{13}_{12}} * \cancel{\cancel{\cancel$$

$$2x - 5y + 3x + 7y + 1 = 2x + 3x - 5y + 7y + 1$$
$$= 5x + 2y + 1$$

$$a^{2} + 2a + 3 + a^{2} - 3a - 1 = a^{2} + a^{2} + 2a - 3a + 3 - 1$$

= $2a^{2} - a + 2$

c)
$$2x^{2} + x + y^{2} - 2x - 2y^{2} = 2x^{2} + y^{2} - 2y^{2} + x - 2x$$
$$= 2x^{2} - y^{2} - x$$

d)
$$2xy + xy^{2} - x^{2}y - 2xy^{2} - yx = 2xy - yx + xy^{2} - 2xy^{2} - x^{2}y$$
$$= xy + xy^{2} - x^{2}y$$

a)
$$(5x + y) + (2x - y) = 5x + y + 2x - y$$

$$= 7x + y - y$$

$$= 7x$$

b)
$$a + 2b - (-a + b) = a + 2b + a - b$$
$$= a + a + 2b - b$$
$$= 2a + b$$

c)
$$(x^2 + 2x + 1) - (x^2 - 2x + 1) = x^2 + 2x + 1 - x^2 + 2x - 1$$

$$= x^2 - x^2 + 2x + 2x + 1 - 1$$

$$= 4x + 1 - 1$$

$$= 4x$$

d)
$$2a^2 - a - 3 + (-a^2 + a + 3) = 2a^2 - a - 3 - a^2 + a + 3$$
$$= 2a^2 - a^2 - a + a - 3 + 3$$
$$= a^2$$

a)
$$2(x+4) = 2 * x + 2 * 4$$
$$= 2x + 8$$

b)
$$-2(t-3) = -2 * t - (-2 * 3)$$

$$= -2t + 2 * 3$$

$$= -2t + 6$$

c)
$$3(2x+1) - 2(3x+1) = 3 * 2x + 3 * 1 - 2 * 3x - 2 * 1$$
$$= 6x + 3 - 6x - 2$$
$$= 6x - 6x + 3 - 2$$
$$= 3 - 2$$
$$= 1$$

d)
$$5(x^2 + 3x + 2) - 5(x^2 + 1) = 5 * x^2 + 5 * 3x + 5 * 2 - 5 * x^2 - 5 * 1$$
$$= 5x^2 + 15x + 10 - 5x^2 - 5$$
$$= 5x^2 - 5x^2 + 15x + 10 - 5$$
$$= 15x + 10 - 5$$
$$= 15x + 5$$

a)
$$2(2a - b) + 3(-2a + 3b) = 2 * 2a - 2 * b + 3 * -2a + 3 * 3b$$
$$= 4a - 2b - 6a + 9b$$
$$= 4a - 6a - 2b + 9b$$
$$= -2a + 7b$$

b)
$$2a(ab - b^{2}) - 2b(a^{2} - ab) = 2a * ab - 2a * b^{2} - 2b * a^{2} + 2b * ab$$
$$= 2ba^{2} - 2ab^{2} - 2ba^{2} + 2ab^{2}$$
$$= 2ba^{2} - 2ba^{2} + 2ab^{2} - 2ab^{2}$$
$$= 0$$

c)
$$(x+1)(2x-3) = x * 2x + x * -3 + 1 * 2x - 3$$
$$= 2x^2 - x3 + 2x - 3$$
$$= 2x^2 - x - 3$$

d)
$$5(x^2 + 3x + 2) - 5(x^2 + 1) = 5 * x^2 + 5 * 3x + 5 * 2 - 5 * x^2 - 5 * 1$$
$$= 5x^2 + 15x + 10 - 5x^2 - 5$$
$$= 5x^2 - 5x^2 + 15x + 10 - 5$$
$$= 15x + 10 - 5$$
$$= 15x + 5$$

d)

a)
$$(2x-1)(x+3) + (x-1)(x-4) = 2x * x + 2x * 3 - 1 * x - 1 * 3 + x * x + x * -4 - 1 * x - 1 * -4$$

$$= 3x^2 - 3 + 4$$

$$= 3x^2 + 1$$

b)

$$2(x-1)(2x+3) = 2(x*2x + x*3 - 1*2x - 1*3)$$

$$= 2(2x^2 + 3x - 2x - 3)$$

$$= 2(2x^2 + x - 3)$$

$$= 2*2x^2 + 2*x + 2*(-3)$$

$$= 4x^2 + 2x - 6$$

c)
$$(x+3)(4x-1) - (2x+1)(2x-3) = x*4x + x*(-1) + 3*4x + 3*(-1) - 2x*2x - 2x*(-3) - 1$$

$$= 4x^2 - x + 12x - 3 - 4x^2 + 6x - 2x + 3$$

$$= 4x^2 - 4x^2 - x + 12x + 6x - 2x - 3 + 3$$

$$= 15x$$

$$\frac{3}{4}(t+3)(8t-4) = (t+3)(\frac{3}{4} * 8t - \frac{3}{4} * 4)$$

$$= (t+3)(\frac{3 * \cancel{8}_2 t}{\cancel{4}_1} - \frac{3 * \cancel{4}}{\cancel{4}})$$

$$= (t+3)(3 * 2t - 3)$$

$$= (t+3)(6t-3)$$

$$= (t*6t+t*(-3)) + (3*6t+3*(-3))$$

$$= 6t^2 - 3t + 18t - 9$$

$$= 6t^2 + 15t - 9$$

$$\frac{a}{2} + \frac{a}{3} + \frac{a}{6} = \frac{a * 3}{2 * 3} + \frac{a * 2}{3 * 2} + \frac{a}{6}$$
$$= \frac{3a}{6} + \frac{2a}{6} + \frac{a}{6}$$
$$= \frac{6a}{6}$$
$$= a$$

$$\frac{1}{2a} + \frac{1}{3a} + \frac{1}{6a} = \frac{1*3}{2*3a} + \frac{1*2}{3*2a} + \frac{1}{6a}$$
$$= \frac{3}{6a} + \frac{2}{6a} + \frac{1}{6a}$$
$$= \frac{\cancel{6}}{\cancel{6}a}$$
$$= \frac{1}{a}$$

$$\frac{2}{x} + \frac{3}{2x} - \frac{4}{3x} = \frac{2*6}{6*x} + \frac{3*3}{3*2x} - \frac{4*2}{2*3x}$$
$$= \frac{12}{6x} + \frac{9}{6a} - \frac{8}{6x}$$
$$= \frac{13}{6x}$$

$$\frac{2a}{3} * \frac{6}{a} = \frac{2\cancel{a}}{\cancel{3}_1} * \frac{\cancel{6}_2}{\cancel{a}}$$
$$= \frac{4}{1}$$
$$= 4$$

$$\frac{2x^2}{3y} * \frac{5y^2}{4x} = \frac{2x}{3} * \frac{5y}{4}$$
$$= \frac{10xy : 2}{12 : 2}$$
$$= \frac{5xy}{6}$$

c)

$$\frac{8a}{5} : \frac{4a}{15} = \frac{8_4 \cancel{d}}{\cancel{5}_1} * \frac{\cancel{15}_3}{\cancel{4}_2 \cancel{d}}$$
$$= \frac{\cancel{4}_2}{1} * \frac{3}{\cancel{2}_1}$$
$$= \frac{6}{1}$$
$$= 6$$

d)

$$\frac{6a}{5} : 2a = \frac{\cancel{0}_{3}\cancel{d}}{5} * \frac{1}{\cancel{2}_{1}\cancel{d}}$$
$$= \frac{3}{5}$$

1.42

a)

$$\frac{2}{3} * \frac{5}{a} + \frac{1}{2} * \frac{7}{3a} = \frac{10}{3a} + \frac{7}{6a}$$

$$= \frac{10 * 2}{3a * 2} + \frac{7}{6a}$$

$$= \frac{20}{6a} + \frac{7}{6a}$$

$$= \frac{27 : 3}{6a : 3}$$

$$= \frac{9}{2a}$$

b)

$$\frac{2}{x} * \left(\frac{5x}{3} - \frac{7x}{6}\right) = \frac{2}{x} * \left(\frac{5x * 2}{3 * 2} - \frac{7x}{6}\right)$$
$$= \frac{2}{x} * \left(\frac{10x}{6} - \frac{7x}{6}\right)$$
$$= \frac{\cancel{2}}{x} * \frac{3x}{\cancel{6}_3}$$
$$= \frac{3x}{3x}$$
$$= 1$$

c)

$$\left(\frac{x^2}{3} + \frac{5x}{6}\right) : \frac{x}{12} = \left(\frac{x^2 * 2}{3 * 2} + \frac{5x}{6}\right) : \frac{x}{12}$$

$$= \left(\frac{2x^2}{6} + \frac{5x}{6}\right) : \frac{x}{12}$$

$$= \left(\frac{2x^2 + 5x}{6}\right) : \frac{x}{12}$$

$$= \left(\frac{2x^2 + 5x}{6}\right) * \frac{12}{x}$$

$$= \left(\frac{2x^{\frac{1}{2}} + 5\cancel{x}}{\cancel{6}}\right) * \frac{\cancel{12}}{\cancel{x}}$$

$$= (2x + 5) * 2$$

$$= 4x + 10$$

1.43

a)

$$\frac{2x+3}{4} - \frac{x+1}{4} = \frac{(2x+3) - (x-1)}{4}$$
$$= \frac{2x - x + 3 - 1}{4}$$
$$= \frac{x+2}{4}$$

b)

$$\frac{a+2}{2} - \frac{2a-1}{6} = \frac{3(a+2)}{2*3} - \frac{(2a-1)}{6}$$
$$= \frac{3a+6}{6} - \frac{2a-1}{6}$$
$$= \frac{3a-2a+6+1}{6}$$
$$= \frac{a+7}{6}$$

c)

$$\frac{x+2}{2x} - \frac{2x-1}{3x} = \frac{3(x+2)}{2x*3} - \frac{2(2x-1)}{3x*2}$$
$$= \frac{3x+6-4x+2}{6x}$$
$$= \frac{-x+8}{6x}$$

$$\frac{2}{a} + \frac{a-2}{2a} - \frac{a+3}{3a} = \frac{2*6}{a*6} + \frac{3(a-2)}{2a*3} - \frac{2(a+3)}{3a*2}$$

$$= \frac{12}{6a} + \frac{3a-6}{6a} - \frac{2a-6}{6a}$$

$$= \frac{12-6-6+3a-2a}{6a}$$

$$= \frac{\cancel{a}}{6\cancel{a}}$$

$$= \frac{1}{6}$$

$$\frac{\frac{2x}{5} + \frac{1}{2}}{\frac{x}{2} - \frac{1}{10}} = \frac{\frac{2x*2}{5*2} + \frac{1*5}{2*5}}{\frac{x*5}{2*5} - \frac{1}{10}}$$

$$= \frac{\frac{4x}{10} + \frac{5}{10}}{\frac{5x}{10} - \frac{1}{10}}$$

$$= \frac{4x + 5}{10} * \frac{10}{5x - 1}$$

$$= \frac{4x + 5}{\cancel{10}} * \frac{\cancel{10}}{5x - 1}$$

$$= \frac{4x + 5}{5x - 1}$$

b)

$$\frac{\frac{1}{x} + \frac{1}{2}}{1 + \frac{2}{x}} = \frac{\frac{1 \times 2}{x \times 2} + \frac{1 \times x}{2 \times x}}{\frac{1 \times x}{1 \times x} + \frac{2}{x}}$$

$$= \frac{\frac{2}{2x} + \frac{x}{2x}}{\frac{x}{x} + \frac{2}{x}}$$

$$= \frac{2 + x}{2x} * \frac{x + 2}{x}$$

$$= \frac{(2 + x)}{2x} * \frac{(x + 2)}{x}$$

$$= \frac{2x + 4 + x^2 + 2x}{2x^2}$$

$$= \frac{4x + x^{\frac{1}{2}} + 4}{2x^{\frac{1}{2}}}$$

$$= \frac{5x + 4}{2x}$$

$$= 3x + 4$$

c)
$$\frac{2}{a} + \frac{a-2}{2a} - \frac{a+3}{3a} = \frac{2*6}{a*6} + \frac{3(a-2)}{2a*3} - \frac{2(a+3)}{3a*2}$$
$$= \frac{12}{6a} + \frac{3a-6}{6a} - \frac{2a-6}{6a}$$
$$= \frac{12-6-6+3a-2a}{6a}$$
$$= \frac{\cancel{e}}{6\cancel{e}}$$
$$= \frac{1}{6}$$

a)

$$3^2 = 3 * 3$$
$$= 9$$

b)

$$(-3)^2 = (-3) * (-3)$$

= 9

c)

$$3^3 = 3 * 3 * 3$$
$$= 27$$

d)

$$(-3)^2 = (-3) * (-3)$$

= 9

1.51

a)

$$3^{2} * 3^{3} = 3 * 3 * 3 * 3 * 3 * 3$$

$$= 3^{2} + ^{3}$$

$$= 3^{5}$$

$$= 243$$

b)

$$2^4 * 2^6 = 2^4 + 6^6$$
$$= 2^1 0$$

$$5^{3} * 5 = 5^{3} + 1$$
$$= 5^{4}$$

$$10^2 * 10^3 * 10^5 = 10^2 +^3 +^5$$
$$= 10^10$$

$$(2*10^4)*(5*10^3) = 2*5*10^4*10^3$$

= $10*10^4+^3$
= $10*10^7$
= 10^7+^1
= 10^8

$$\frac{2^4}{2^3} = 2^{4-3} \\ = 2^1 \\ = 2$$

$$\frac{10^5}{10^3} = 10^{5-3}$$
$$= 10^2$$
$$= 100$$

$$\frac{4^3 * 4^2}{4^4} = \frac{4^{3+2}}{4^4}$$
$$= \frac{4^5}{4^4}$$
$$= 4^{5-4}$$
$$= 4^1$$
$$= 4$$

$$\frac{3^8 * 3^6}{3^5 * 3^7} = \frac{3^{8+6}}{3^{5+7}}$$
$$= \frac{3^1 4}{3^1 2}$$
$$= 3^{14-12}$$
$$= 3^2$$
$$= 9$$

e)

$$\frac{2*10^5*6*10^2}{4*10^4} = \frac{2*6*10^{5+2}}{4*10^4}$$

$$= \frac{12*10^7}{4*10^4}$$

$$= \frac{12*10^{7-4}}{4}$$

$$= \frac{12*10^3}{4}$$

$$= \frac{12*1000}{4}$$

$$= \frac{12000}{4}$$

$$= 3000$$

$$5^0 = \frac{1}{5}$$

$$(-2)^0 = \frac{1}{-2}$$

$$5^{-1} = \frac{1}{5^1}$$

$$2^{-4} = \frac{1}{2^4}$$

$$10^{-2} = \frac{1}{10^2}$$

$$10^0 = 1$$

$$10^{-4} = \frac{1}{10^4}$$

$$2^{3} - 2^{-4} = 2^{3} - \frac{1}{2^{4}}$$

$$= \frac{1 * 2^{3}}{2^{4}}$$

$$= \frac{1 * 8}{16}$$

$$= \frac{8}{16}$$

$$= 2$$

$$3^{-4} * 3^5 = 3^{-4+5}$$

$$= 3^1$$

$$= 3$$

$$\frac{3^{-2}}{3^{-3}} = \frac{3^3}{3^2}$$

$$= 3^{3-2}$$

$$= 3^1$$

$$= 3$$

$$\frac{2^{-3} * 2^{5}}{2^{3} * 2^{-1}} = \frac{2^{-3+5}}{2^{3-1}}$$
$$= \frac{2^{2}}{2^{2}}$$
$$= \frac{4}{4}$$
$$= 1$$

$$\frac{a^4 * a^{-3}}{a^{-2} * a} = \frac{a^{4-3}}{a^{-2+1}}$$
$$= \frac{a^1}{a^{-1}}$$
$$= a * a^1$$
$$= a^2$$

$$\left(\frac{1}{2}\right)^3 = \frac{1^3}{2^3}$$
$$= \frac{1}{8}$$

$$\left(\frac{2}{3}\right)^3 = \frac{2^3}{3^3}$$
$$= \frac{8}{27}$$

$$\left(\frac{1}{10}\right)^3 = \frac{1^3}{10^3}$$
$$= \frac{1}{1000}$$

$$\left(-\frac{2}{3}\right)^4 = -\frac{2^4}{3^4}$$
$$= -\frac{16}{81}$$

$$\frac{a^4 * a^{-3}}{a^{-2} * a} = \frac{a^{4-3}}{a^{-2+1}}$$
$$= \frac{a^1}{a^{-1}}$$
$$= a * a^1$$
$$= a^2$$

a)

$$\left(\frac{2}{3}\right)^{3} * 3^{3} = \frac{2^{3} * 3^{3}}{3^{3}}$$

$$= \frac{8 * 27}{27}$$

$$= \frac{2 * 2 * 2 * 3 * 3 * 3}{3 * 3 * 3}$$

$$= \frac{2 * 2 * 2 * 3 * 3 * 3}{3 * 3 * 3}$$

$$= \frac{8}{1}$$

b)

$$\frac{2^{5}}{5^{2}} * \left(\frac{5}{2}\right)^{3} = \frac{2^{5} * 5^{3}}{5^{2} * 2^{3}}$$

$$= \frac{2 * 2 * 2 * 2 * 2 * 5 * 5 * 5}{5 * 5 * 2 * 2 * 2 * 2}$$

$$= \frac{2 * 2 * \cancel{2} * \cancel{2} * \cancel{2} * 5 * \cancel{5} * \cancel{5}}{\cancel{5} * \cancel{5} * \cancel{2} * \cancel{2} * \cancel{2}}$$

$$= \frac{4 * 5}{1}$$

$$= \frac{20}{1}$$

c)

$$\left(\frac{x}{2}\right)^2 = \frac{x^2}{2^2}$$
$$= \frac{x^2}{4}$$

d)

$$3^{5} * \left(\frac{x}{3}\right)^{4} = \frac{3^{5} * x^{4}}{3^{4}}$$

$$= \frac{3 * \cancel{\beta} * \cancel{\beta} * \cancel{\beta} * \cancel{\beta} * x * x * x * x * x}{\cancel{\beta} * \cancel{\beta} * \cancel{\beta} * \cancel{\beta} * \cancel{\beta}}$$

$$= 3x^{4}$$

$$(5*10^3)^3 = 5^3 * 10^{3*3}$$
$$= 5^3 * 10^9$$
$$= 125 * 10^9$$
$$= 1250000000000$$

$$(2*10^{2})^{-1} = 2^{-1} * 10^{2*(-1)}$$

$$= 2^{-1} * 10^{-2}$$

$$= \frac{1}{2*10^{2}}$$

$$= \frac{1}{200}$$
= 0.005

c)

$$(3*10^{-3})^{2} * (3*10^{-2})^{-1} = 3^{2} * 10^{-3*2} * 3^{-1} * 10^{-2*(-1)}$$

$$= 3^{2} * 10^{-6} * 3^{-1} * 10^{2}$$

$$= 3^{2-1} * 10^{-6+2}$$

$$= 3 * 10^{-4}$$

$$= \frac{3}{10^{4}}$$

$$= \frac{3}{10000}$$

$$= 0.0003$$

d)

$$\frac{5*10^{-2}*9*10^{4}}{3*10^{3}} = \frac{5*9*10^{-2+4}}{3*10^{3}}$$

$$= \frac{5*9*10^{2}}{3*10^{3}}$$

$$= \frac{5*9_{3}*100}{3*1000_{10}}$$

$$= \frac{5*3}{10}$$

$$= \frac{15}{10}$$

$$= 1.5$$

a)

$$x^7 * \left(x^{-2}\right)^3$$

b)

$$(2*10^{2})^{-1} = 2^{-1} * 10^{2*(-1)}$$

$$= 2^{-1} * 10^{-2}$$

$$= \frac{1}{2*10^{2}}$$

$$= \frac{1}{200}$$
= 0.005

c)

$$(3*10^{-3})^{2} * (3*10^{-2})^{-1} = 3^{2} * 10^{-3*2} * 3^{-1} * 10^{-2*(-1)}$$

$$= 3^{2} * 10^{-6} * 3^{-1} * 10^{2}$$

$$= 3^{2-1} * 10^{-6+2}$$

$$= 3 * 10^{-4}$$

$$= \frac{3}{10^{4}}$$

$$= \frac{3}{10000}$$

$$= 0.0003$$

d)

$$\frac{5*10^{-2}*9*10^{4}}{3*10^{3}} = \frac{5*9*10^{-2+4}}{3*10^{3}}$$

$$= \frac{5*9*10^{2}}{3*10^{3}}$$

$$= \frac{5*9_{3}*100}{3*1000_{10}}$$

$$= \frac{5*3}{10}$$

$$= \frac{15}{10}$$

$$= 1.5$$

$$\sqrt{\frac{16}{25}} = \frac{\sqrt{16}}{\sqrt{25}} = \frac{4}{5}$$

$$\sqrt{\frac{49}{64}} = \frac{\sqrt{49}}{\sqrt{64}}$$
$$= \frac{7}{8}$$

$$\sqrt{\frac{1}{121}} = \frac{\sqrt{1}}{\sqrt{121}}$$
$$= \frac{1}{11}$$

$$\sqrt{\frac{18}{98}} = \frac{\sqrt{9} * \sqrt{2}}{\sqrt{49} * \sqrt{2}}$$
$$= \frac{3}{7}$$

$$\sqrt{18} = 3\sqrt{2}$$

$$\sqrt{18} = \sqrt{9 * 2}$$

$$\sqrt{12} = 2\sqrt{3}$$
$$= \sqrt{4*3}$$

$$\sqrt{48} = 4\sqrt{3}$$
$$= \sqrt{16*3}$$

$$\sqrt{27} = \sqrt{9 * 3}$$
$$= 3\sqrt{3}$$

$$\sqrt{75} = \sqrt{5 * 15}$$

$$= \sqrt{5} * \sqrt{5} * \sqrt{3}$$

$$= \sqrt{25 * 3}$$

$$= 5\sqrt{3}$$

$$\sqrt{162} = \sqrt{81 * 2}$$
$$= 9\sqrt{2}$$

$$3\sqrt{27} = 3$$

$$^{3}\sqrt{1000} = 10$$

$$3\sqrt{-64} = -4$$

$$3\sqrt{-8000} = \sqrt{-80 * -10 * -10}
= \sqrt{-20 * 4 * 5 * 2 * 5 * 2}
= \sqrt{-5 * 4 * 4 * 5 * 2 * 5 * 2}
= \sqrt{-5 * 5 * 5 * 2 * 2 * 2 * 2 * 2 * 2}
= \sqrt{-20 * -20 * -20} = -20$$

$$4\sqrt{13} = 3, 6$$

$$5\sqrt{20,5} = 4,5$$

$$3\sqrt{15} = 1,96$$

$$^{3}\sqrt{-52} = -2,68$$

$$^{3}\sqrt{-27000} = -12,81$$

$$4\sqrt{-12} = 1,364$$

1.83

$$3\sqrt{10^3} = 10$$

$$^{3}\sqrt{10-6} = 10^{-9}$$

c)

$$^{3}\sqrt{-8000} = \sqrt{-80 \cdot -10 \cdot -10}
= \sqrt{-20 \cdot 4 \cdot 5 \cdot 2 \cdot 5 \cdot 2}
= \sqrt{-5 \cdot 4 \cdot 4 \cdot 5 \cdot 2 \cdot 5 \cdot 2}
= \sqrt{-5 \cdot 5 \cdot 5 \cdot 2 \cdot 2 \cdot 2 \cdot 2 \cdot 2 \cdot 2 \cdot 2}
= \sqrt{-20 \cdot -20 \cdot -20} = -20$$