

Improving efficiency

- Combining binary search with merge sort very efficient
 - If we search list k times, then efficiency is $n \cdot \log(n) + k \cdot \log(n)$
- Can we do better?
- Dictionaries use concept of hashing
 - Lookup can be done in time almost independent of size of dictionary

Hashing

- Convert key to an int
- Use int to index into a list (constant time)
- Conversion done using a **hash function**
 - Map large space of inputs to smaller space of outputs
 - Thus a many-to-one mapping
 - When two inputs go to same output – a **collision**
 - A good hash function has a uniform distribution – minimizes probability of a collision

Complexity

- If no collisions, then $O(1)$
- If everything hashed to same bucket, then $O(n)$
- But in general, can trade off space to make hash table large, and with good function get close to uniform distribution, and reduce complexity to close to $O(1)$