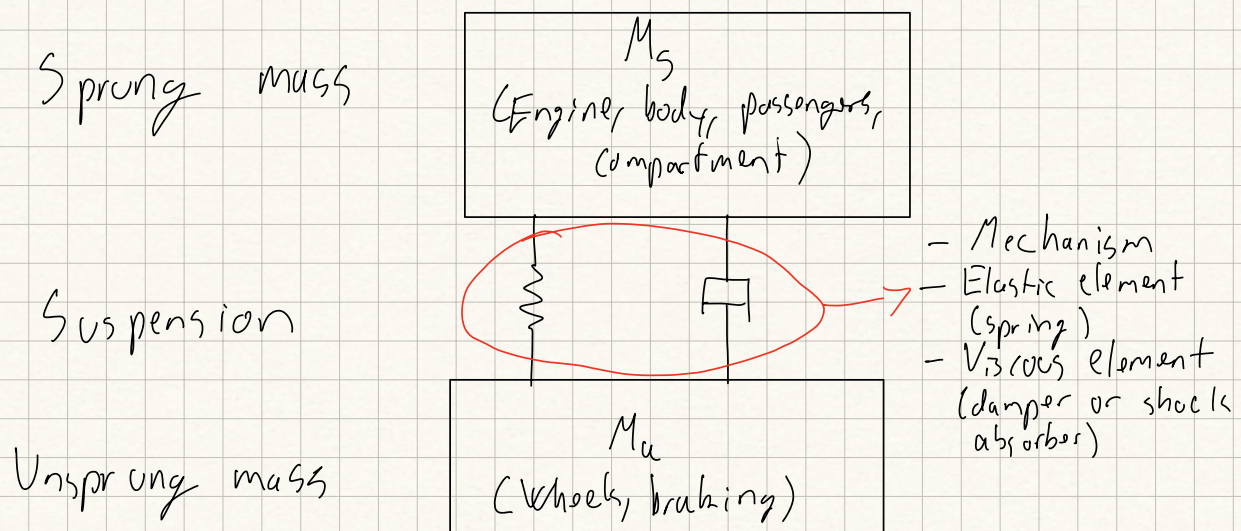


Fundamentals

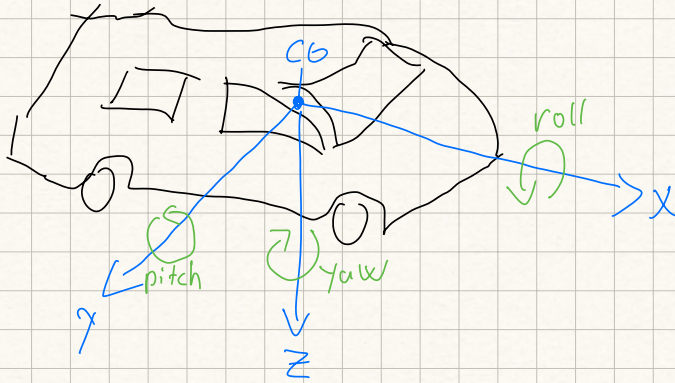
Scope

- Longitudinal dynamics
 - Acceleration
 - Braking
- Vertical dynamics
 - Ride ($f < 50 \text{ Hz}$)
 - Noise ($50 \text{ Hz} < f < 20 \text{ kHz}$)
- Lateral dynamics
 - Handling
 - Manoeuvring

Lumped parameter modeling



Vehicle reference frame



- CG centre of gravity
- x-axis: longitudinal, forward
- y-axis: lateral, pointing left
- z-axis: vertical, aligned with g

Earth-fixed axis system

- x_0 -axis: forward direction
- y_0 -axis: lateral direction
- z_0 -axis: vertical direction, aligned with $-g$

Rigid-body dynamics

$$\sum F_x = M \cdot a_x$$

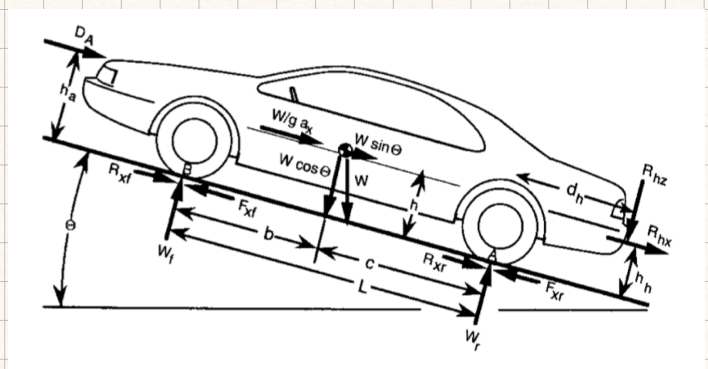
(1-directional motion)

$$\sum T_x = I_{xx} \cdot \alpha_x$$

(Planar motion)

Find v_p and v_r

To find v_{fr} use point A.



For torque: counter-clockwise rotation positive

$$-W_f \cdot L - D_A h_A - \frac{W}{g} a_x h - W \sin(\theta) h + W \cos(\theta) c = 0$$

$$W_f = \frac{1}{L} \left[W \cos(\theta) c - W \sin(\theta) h - \frac{W}{g} a_x h - D_A h_A \right]$$

To find W_r , we use point B

$$W_r L - D_A h_A - \frac{W}{g} a_x h - W \cos(\theta) b - W \sin(\theta) h = 0$$

$$W_r = \frac{1}{L} \left[W \cos(\theta) b + W \sin(\theta) h + \frac{W}{g} a_x h + D_A h_A \right]$$

When static and level:

$$v=0, \theta=0, v=0 \Rightarrow a=0$$

$$W_{fs} = \frac{1}{L} \left[W \cos(0) c - W \sin(0) h - \frac{W}{g} 0 \cdot h - 0 h_A \right]$$

$$= \frac{1}{L} W c$$

$$W_{rs} = \frac{1}{L} \left[W \cos(0) b + W \sin(0) h + \frac{W}{g} 0 \cdot h + 0 h_A \right]$$

$$= \frac{1}{L} W b$$

$$W_{fs} + W_{rs} = \frac{1}{L} W c + \frac{1}{L} W b$$

$$= \frac{1}{L} W (c + b), \quad c + b = L$$

$$= W$$

Static on upward hill:

$$a_x = 0, \quad \theta > 0$$

$$\cos(\theta) < 1, \quad \sin(\theta) > 0$$

$$W_f = \frac{1}{L} [W \cos(\theta) c - W \sin(\theta) h]$$

$$W_r = \frac{1}{L} [W \cos(\theta) b + W \sin(\theta) h]$$

$$W_f < W_{fs}$$