## Quiz

- 1. Classify the following PDEs as either elliptic, parabolic or hyperbolic
  - Laplace eq:  $\Delta u = 0$
  - Poisson eq:  $\Delta u = f(x, y, z)$
  - ▶ Heat or diffusion eq:  $u_t = \Delta u$
  - Wave eq:  $u_{tt} = \Delta u$
- 2. Use the Taylor expansion on the following equation and show that it is a good approximation to u''(t) for small k:  $\frac{u(t+k)-2u(t)+u(t-k)}{k^2}$
- 3. Write down a method of lines discretisation of  $u_t = -u_{xx} + u^3$  with boundary conditions u(0,t) = u(1,t) = 0. From this, write a time-step equation using (a) Forwards Euler and (b) Backwards Euler. How would you solve the equation produced by (b)?
- 4. Use big O notation to write down how the storage size (in memory) of a dense N × N matrix changes with respect to N. Consider the sparse L matrix introduced in the lectures: how does its size grow with N?





## Quiz

- 5. Consider the solution of the heat equation  $u_t = u_{xx}$  over time, given an initial condition  $u(x,0) = cos(\eta x)$ . Discuss the time evolution of u(x,t) for (a) large  $\eta$ , or (b) small  $\eta$ . If you were numerically solving this equation using a forward Euler method, how would the value of  $\eta$  determine (a) the spatial resolution h and (b) the time-step k.
- 6. Write down a method of lines discretisation of  $u_t = -u_{xx} + u^3$  with Neumann boundary conditions of  $u_x(0,t) = u_x(1,t) = 0$
- 7. Use big O notation to write down how the size of *L* in *d* spatial dimensions varies with both *N* and *d*.
- 8. Write down the matrix A generated using the following MATLAB code:

$$v = [2 \ 1 \ -1 \ -2 \ -5];$$
  
 $A = diag(v)$ 



