

## Exercise Sheet 4

### Exercise 1 - Creating arrays

- Create a simple two dimensional array. Use the functions `len()`, `numpy.shape()` on these arrays. How do they relate to each other? And to the `ndim` attribute of the arrays?
- Experiment creating arrays with `arange`, `linspace`, `ones`, `zeros`, `eye` and `diag`. Create different kinds of arrays with random numbers. Try setting the seed before creating an array with random values. Look at the function `np.empty`. What does it do? When might this be useful?

### Exercise 2 - Indexing and slicing

- Try the different flavours of slicing, using start, end and step: starting from a `linspace`, try to obtain odd numbers counting backwards, and even numbers counting forwards.

```
>>> a[0, 3:5]
array([3, 4])

>>> a[4:, 4:]
array([[44, 55],
       [54, 55]])

>>> a[:, 2]
a([2, 12, 22, 32, 42, 52])

>>> a[2::2, ::2]
array([[20, 22, 24],
       [40, 42, 44]])
```

0	1	2	3	4	5
10	11	12	13	14	15
20	21	22	23	24	25
30	31	32	33	34	35
40	41	42	43	44	45
50	51	52	53	54	55

- Reproduce the slices in the diagram above. You may use the following expression to create the array:

```
np.arange(6) + np.arange(0, 51, 10)[: , np.newaxis]
```

### Exercise 3 - Data statistics

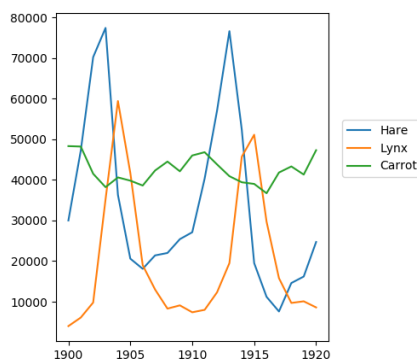
The data in `populations.txt` describes the populations of hares and lynxes (and carrots) in northern Canada during 20 years:

```
data = np.loadtxt('data/populations.txt')
year, hares, lynxes, carrots = data.T # trick: columns to variables

import matplotlib.pyplot as plt
plt.axes([0.2, 0.1, 0.5, 0.8])

plt.plot(year, hares, year, lynxes, year, carrots)

plt.legend(('Hare', 'Lynx', 'Carrot'), loc=(1.05, 0.5))
```



This exercise uses the data in `populations.txt`. You can load this into a numpy array using

```
data = np.loadtxt('populations.txt')
```

Compute (all without for-loops) and print:

- The mean and std of the populations of each species for the years in the period.
- Which year each species had the largest population.

- c) Which species has the largest population for each year. (Hint: argsort & fancy indexing of `np.array(['H', 'L', 'C'])`)
- d) Which years any of the populations is above 50000. (Hint: comparisons and `np.any`)
- e) The top 2 years for each species when they had the lowest populations. (Hint: argsort, fancy indexing)
- f) Compare (plot) the change in hare population (see `help(np.gradient)`) and the number of lynxes. Check correlation (see `help(np.corrcoef)`).

## Exercise 4 - Crude integral approximations

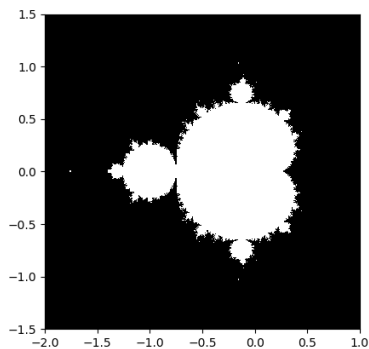
Write a function `f(a, b, c)` that returns  $a^b - c$ . Form a  $24 \times 12 \times 6$  array containing its values in parameter ranges  $[0, 1] \times [0, 1] \times [0, 1]$ .

Approximate the 3-d integral

$$\int_0^1 \int_0^1 \int_0^1 (a^b - c) da db dc$$

over this volume with the mean of the array. The exact result is:  $\ln 2 - \frac{1}{2} \approx 0.1931 \dots$  - what is your relative error? (Hints: use elementwise operations and broadcasting. You can make `np.ogrid` give a number of points in given range with `np.ogrid[0:1:20 j]`.)

## Exercise 5 - Mandelbrot fractal



Write a script that computes the Mandelbrot fractal. The Mandelbrot iteration:

```
N_max = 50
some_threshold = 50

c = x + 1j*y

z = 0
for j in range(N_max):
    z = z**2 + c
    Point (x, y) belongs to the Mandelbrot set if |z| < some_threshold.
```

Do this computation by:

- a) Construct a grid of  $c = x + 1j * y$  values in range  $[-2, 1] \times [-1.5, 1.5]$
- b) Do the iteration
- c) Form the 2-d boolean mask indicating which points are in the set
- d) Save the result to an image with:

```
import matplotlib.pyplot as plt
plt.imshow(mask.T, extent=[-2, 1, -1.5, 1.5])

plt.gray()
plt.savefig('mandelbrot.png')
```