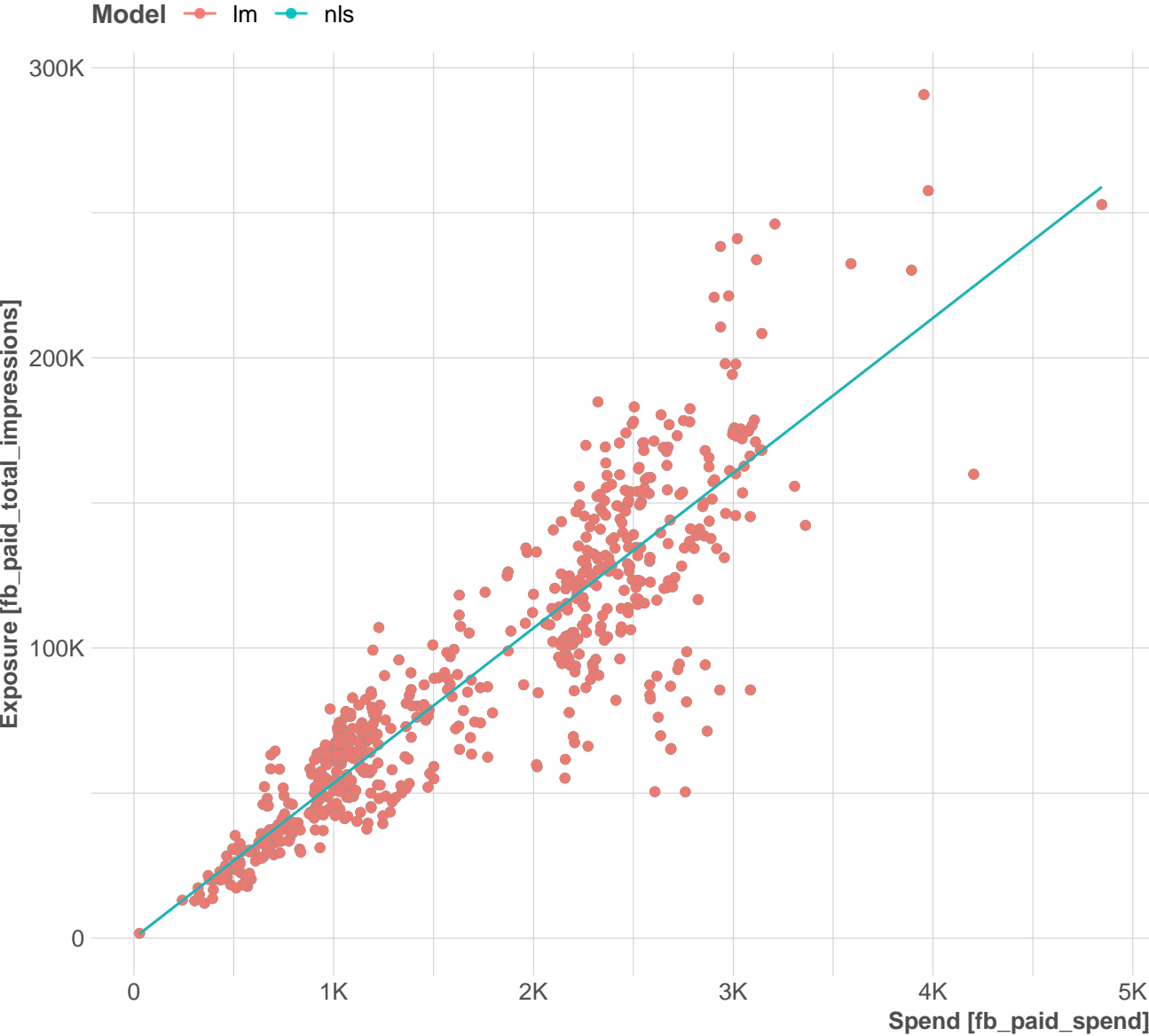
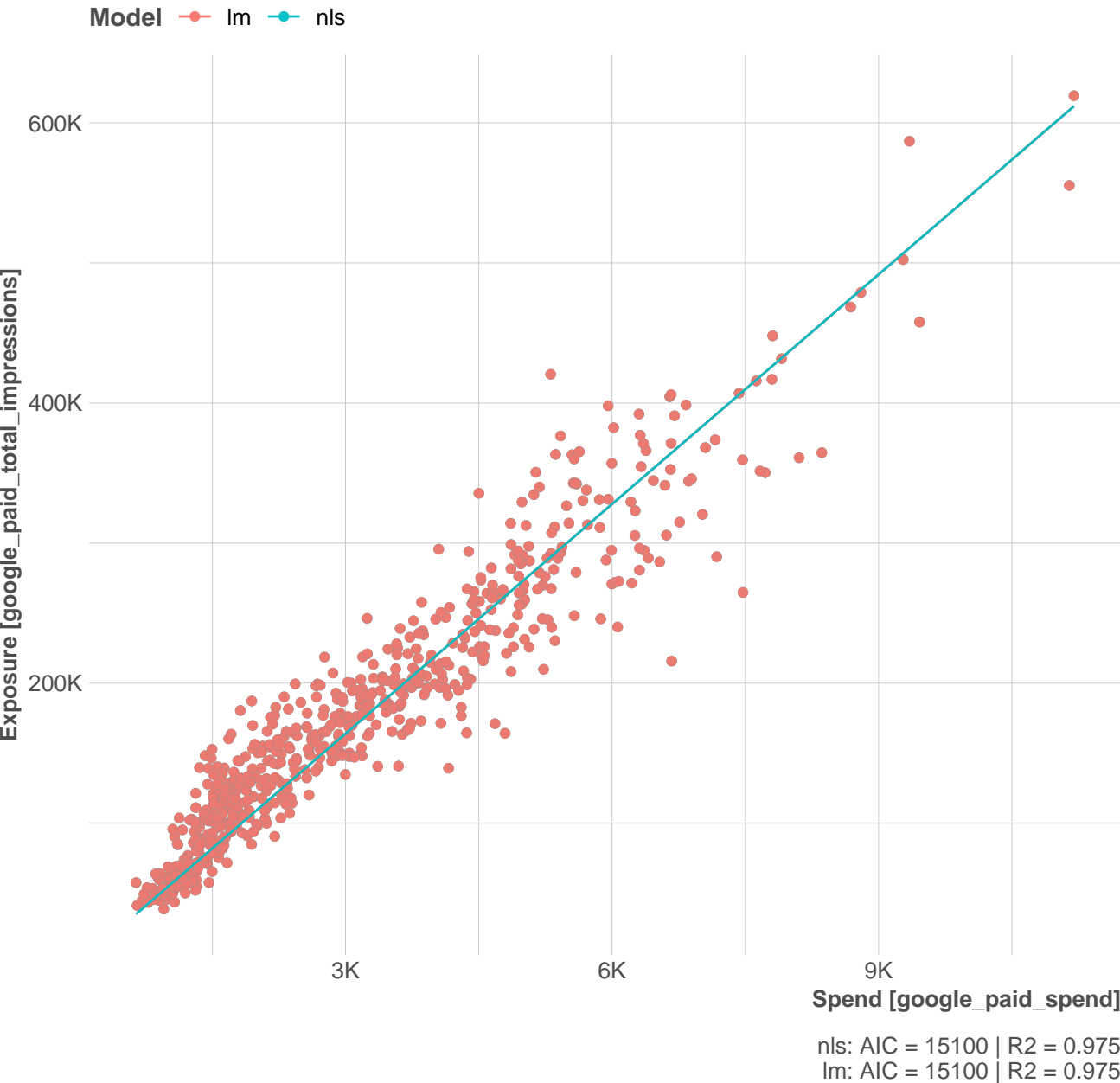


Exposure–Spend Models Fit Comparison

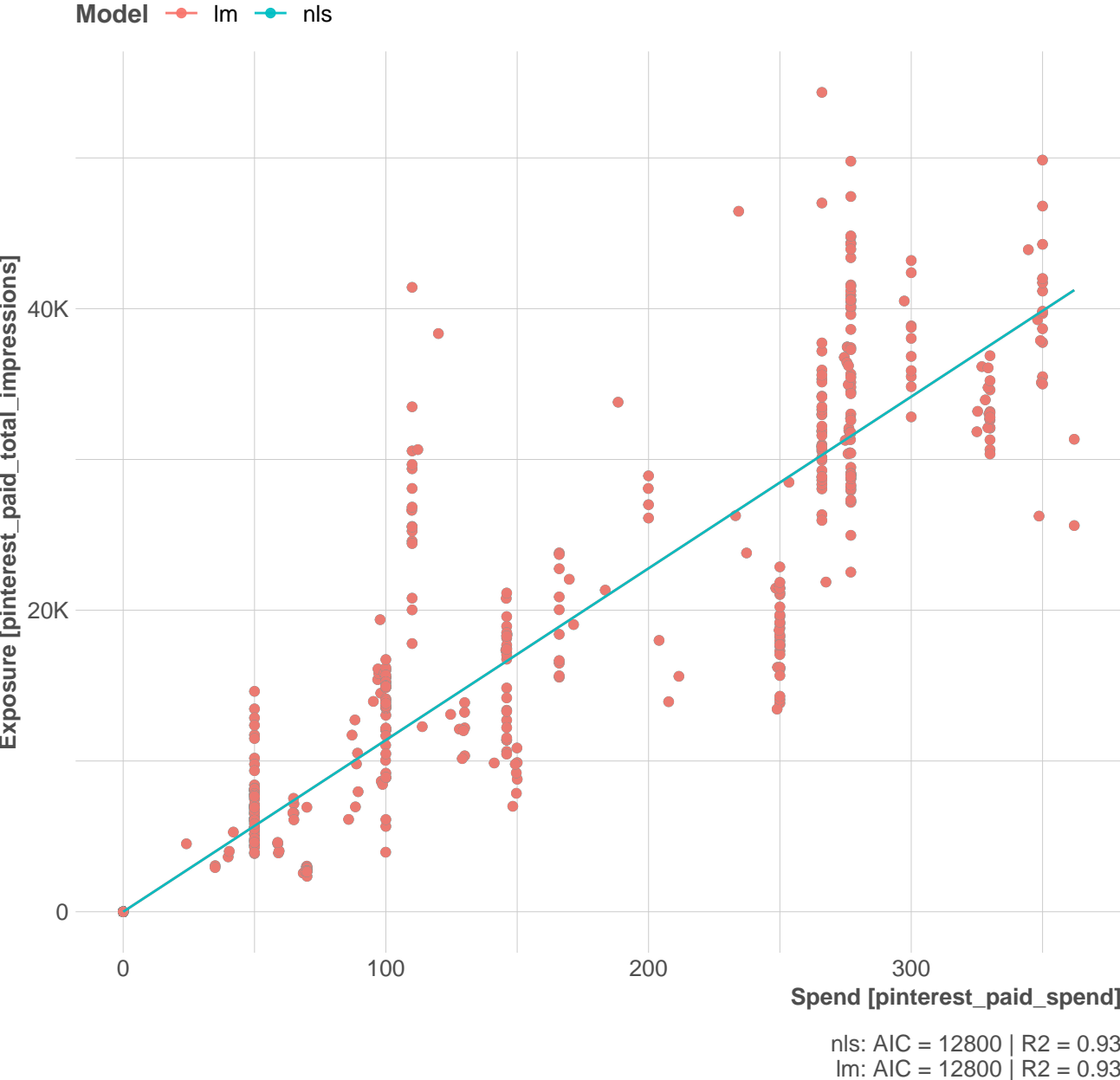


nls: AIC = 14700 | R2 = 0.956
Im: AIC = 14700 | R2 = 0.956

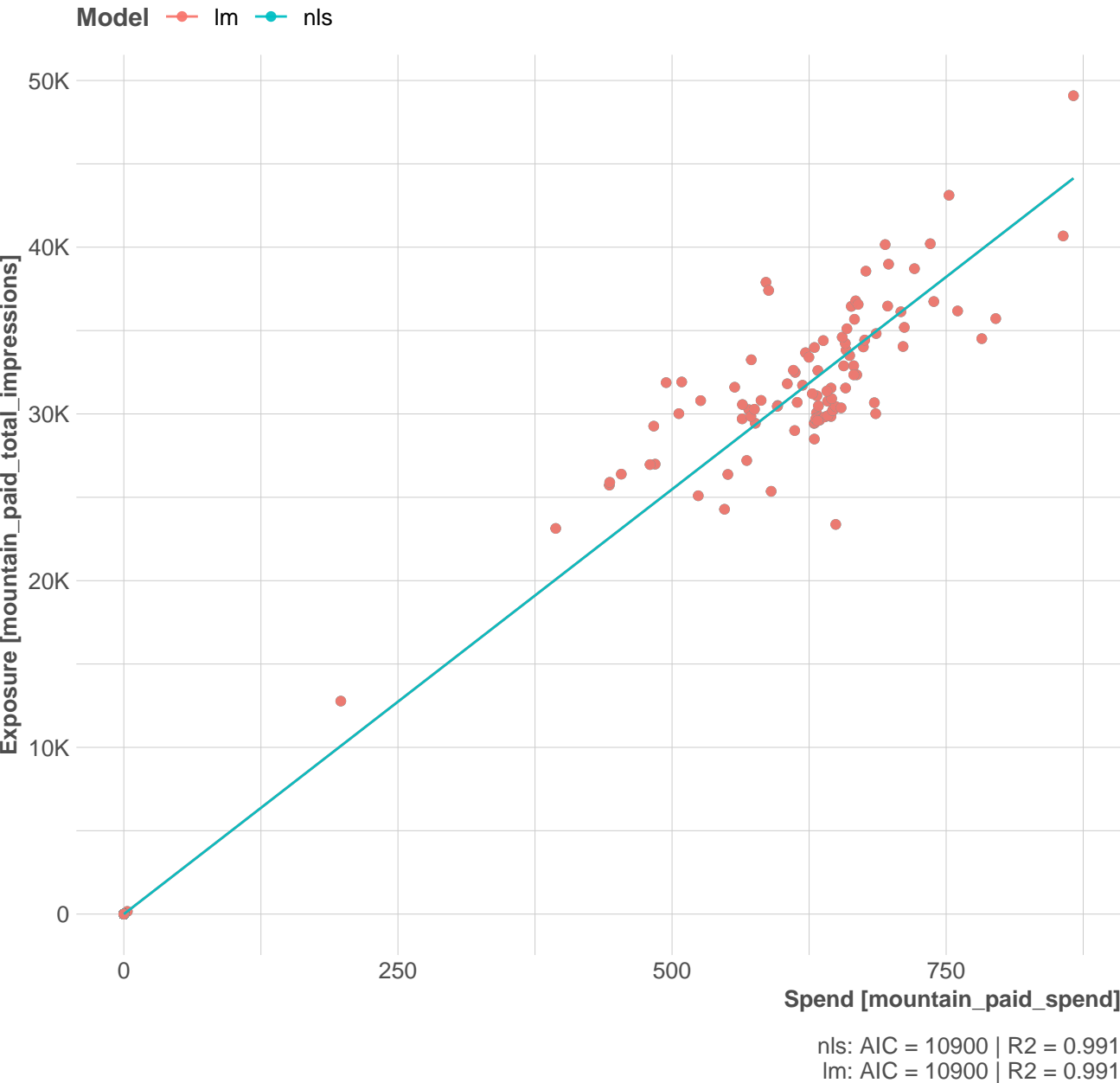
Exposure–Spend Models Fit Comparison



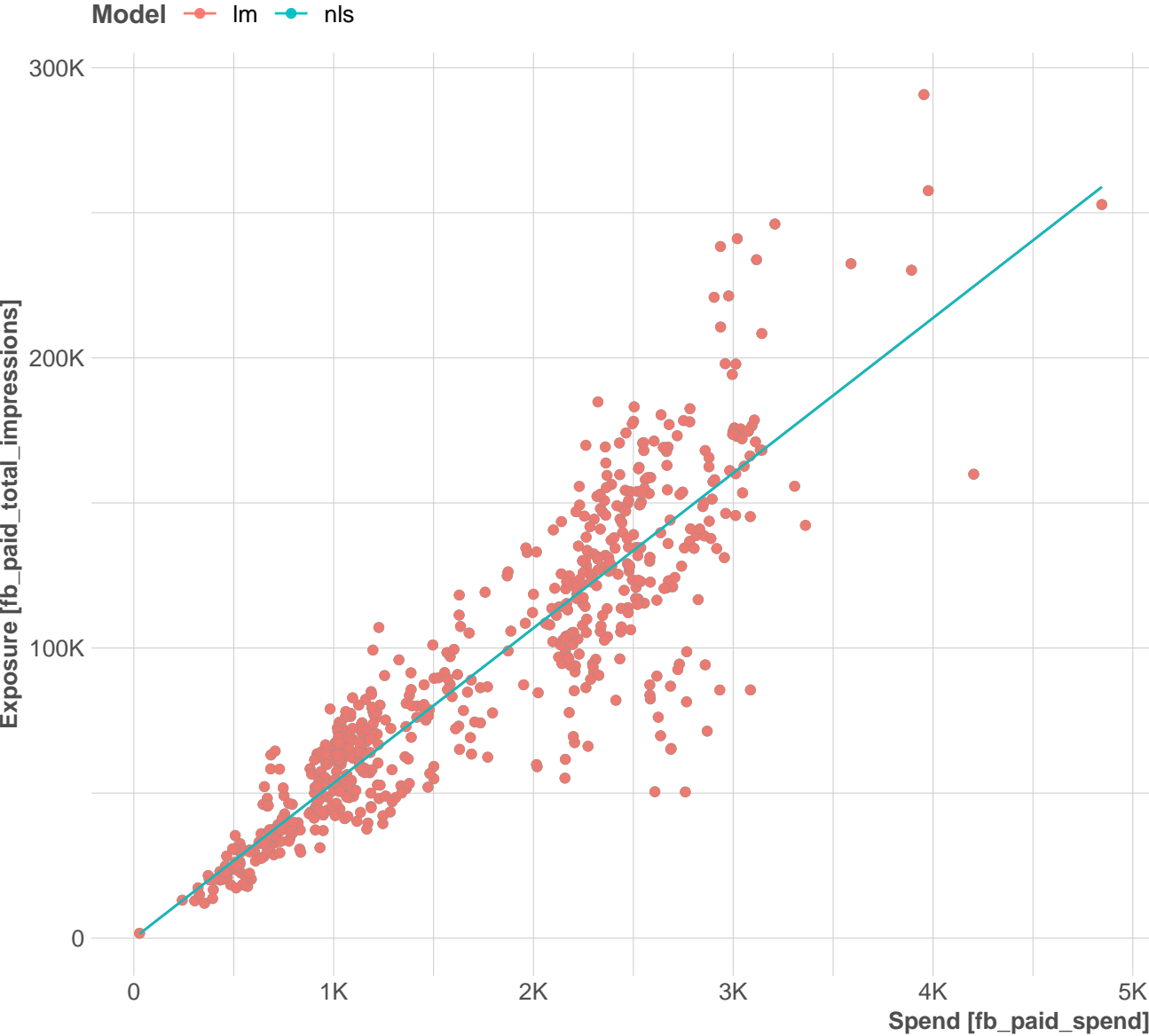
Exposure–Spend Models Fit Comparison



Exposure–Spend Models Fit Comparison

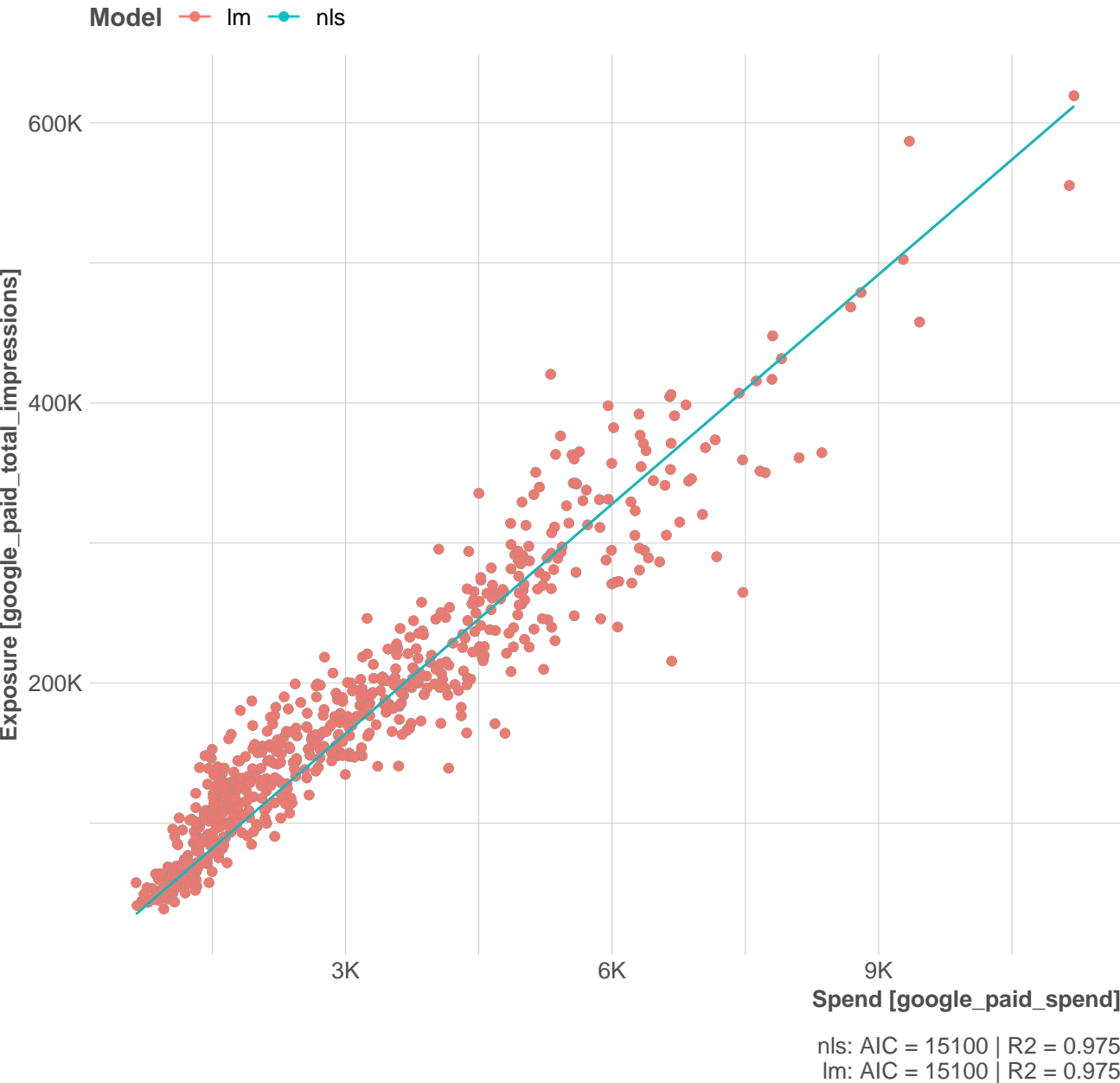


Exposure–Spend Models Fit Comparison

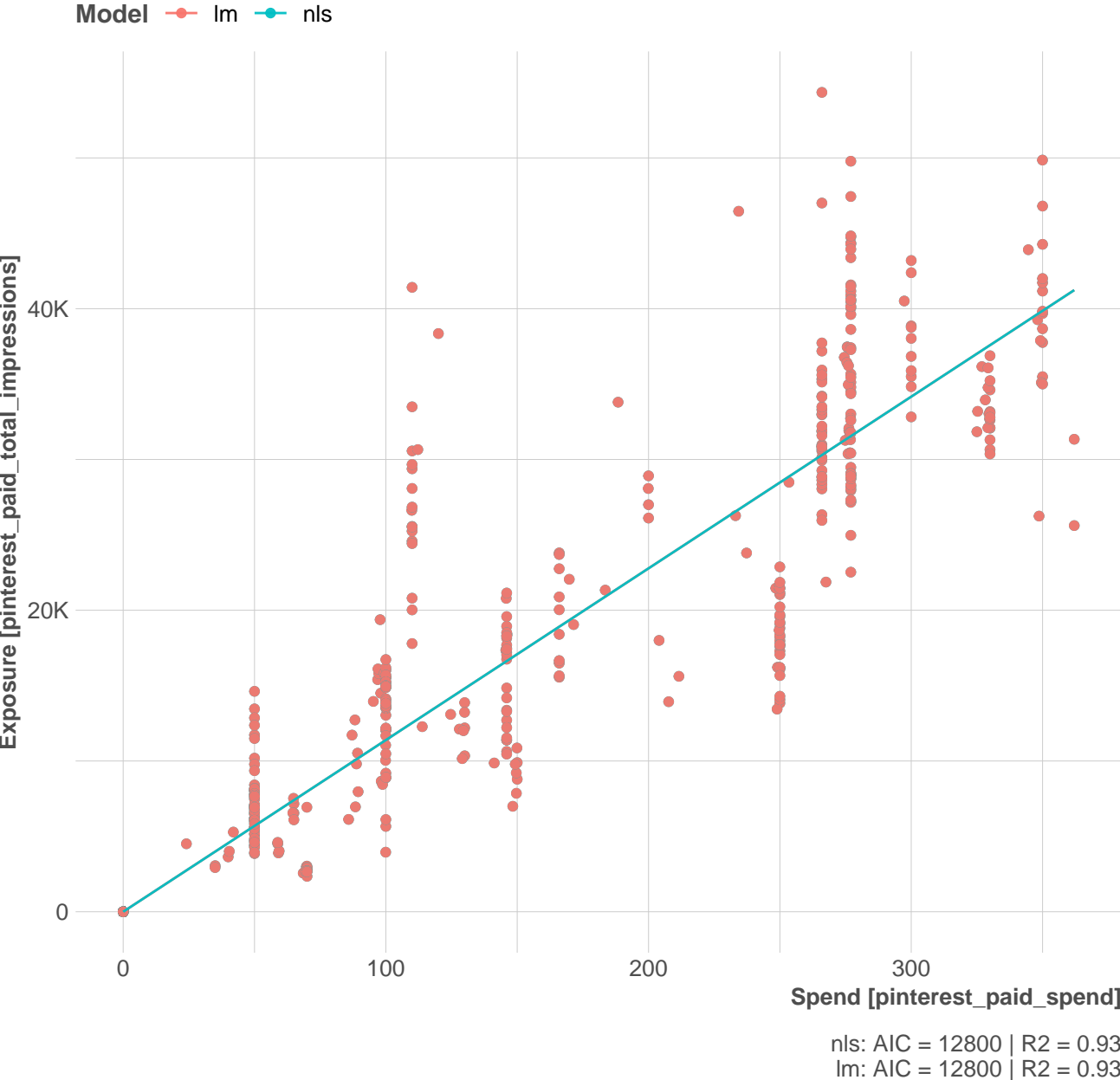


nls: AIC = 14700 | R2 = 0.956
Im: AIC = 14700 | R2 = 0.956

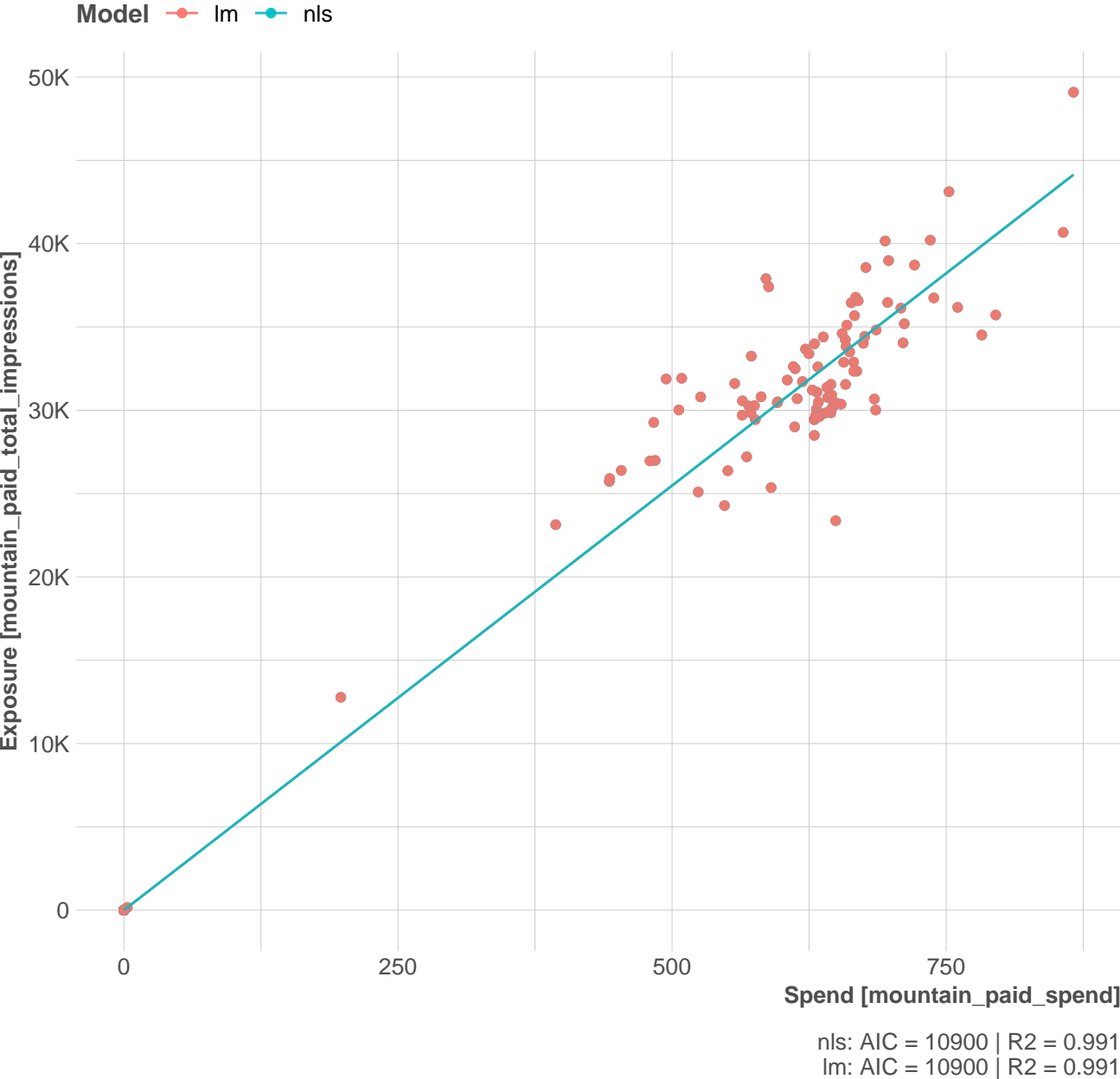
Exposure–Spend Models Fit Comparison



Exposure–Spend Models Fit Comparison

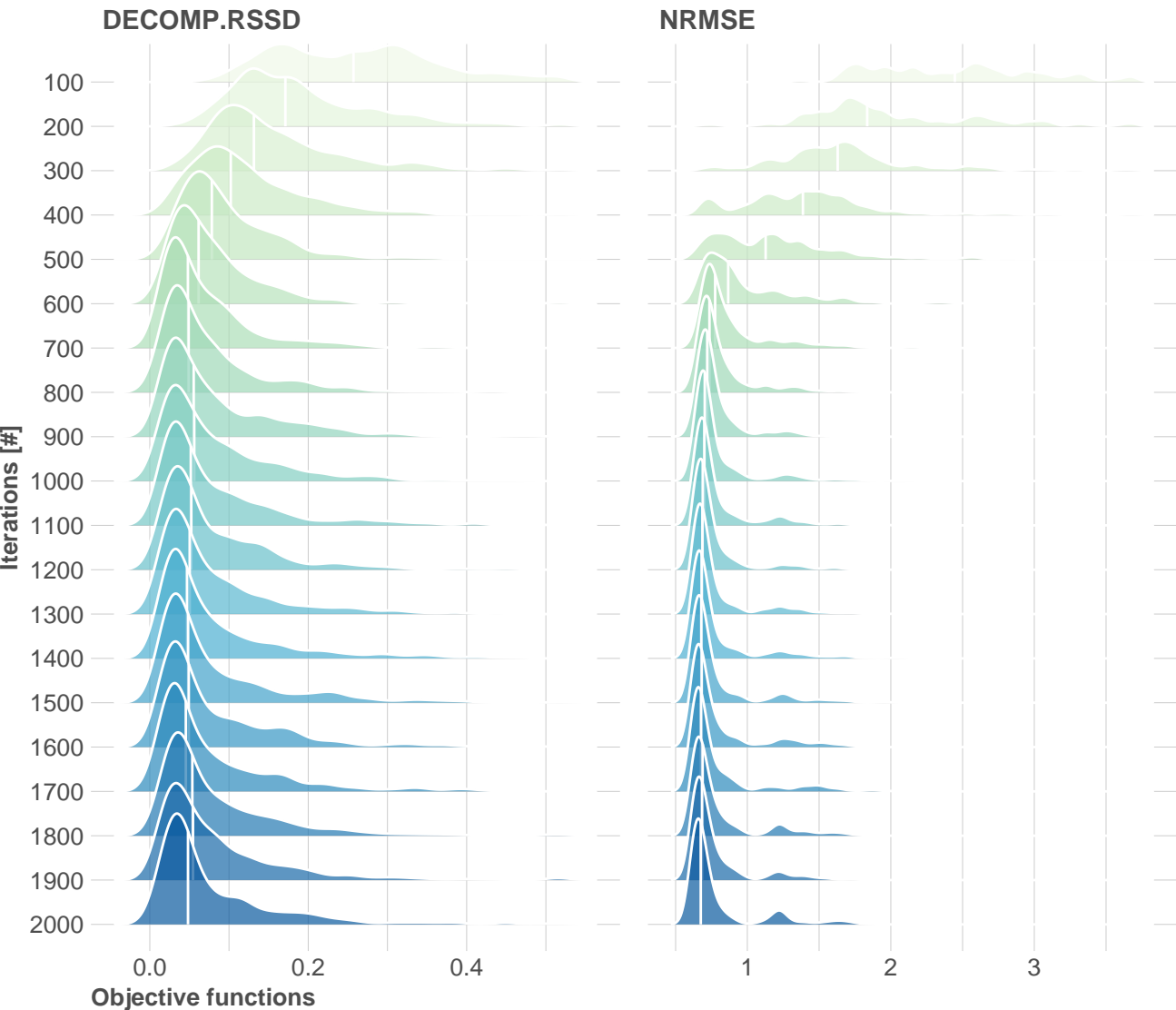


Exposure–Spend Models Fit Comparison



Objective convergence by iterations quantiles

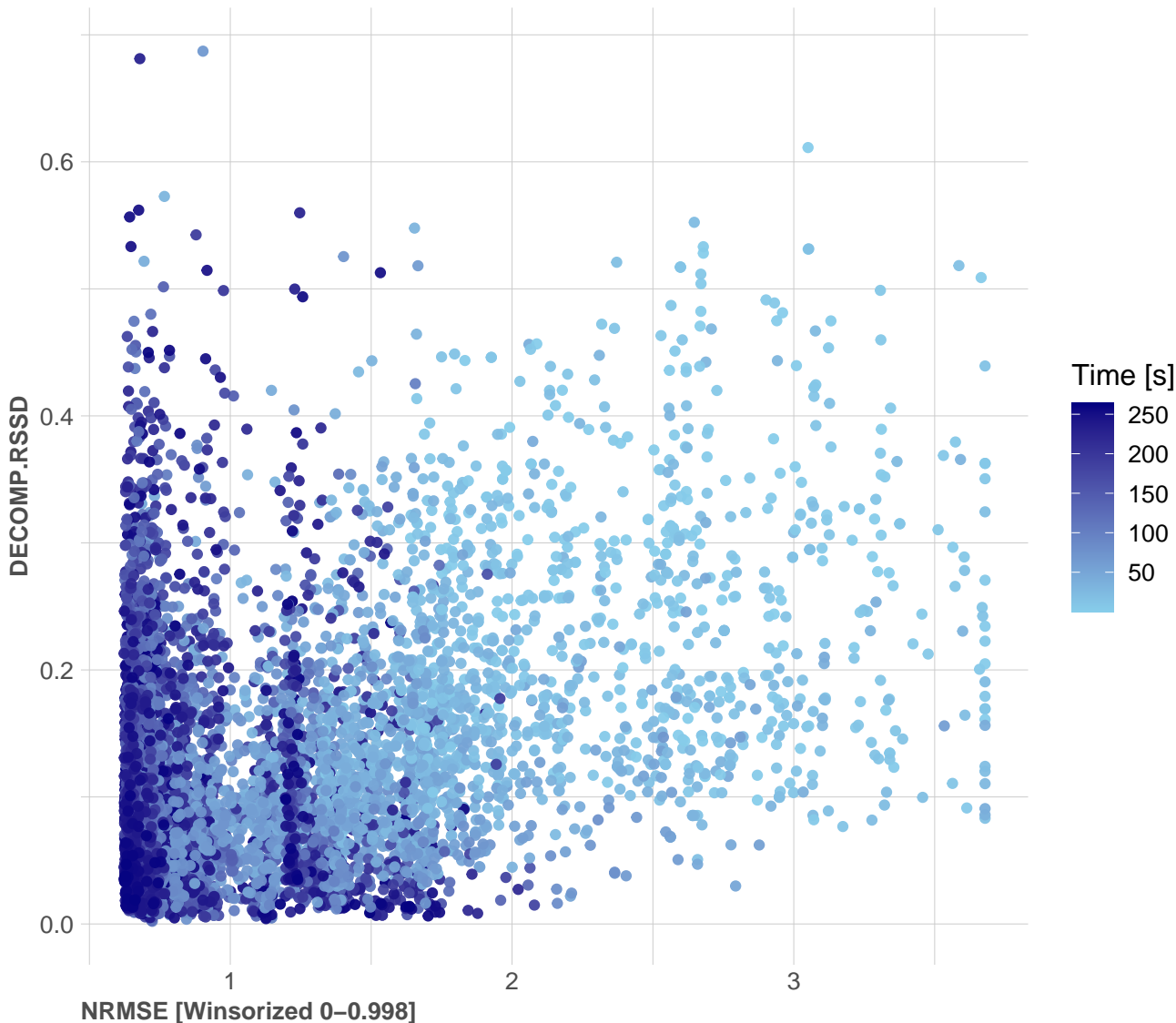
5 trials with 2000 iterations each using TwoPointsDE



DECOMP.RSSD converged: sd@qt.20 0.081 <= 0.092 & |med@qt.20| 0.048 <= 0.073
NRMSE converged: sd@qt.20 0.26 <= 0.55 & |med@qt.20| 0.68 <= 1.3

Multi-objective evolutionary performance

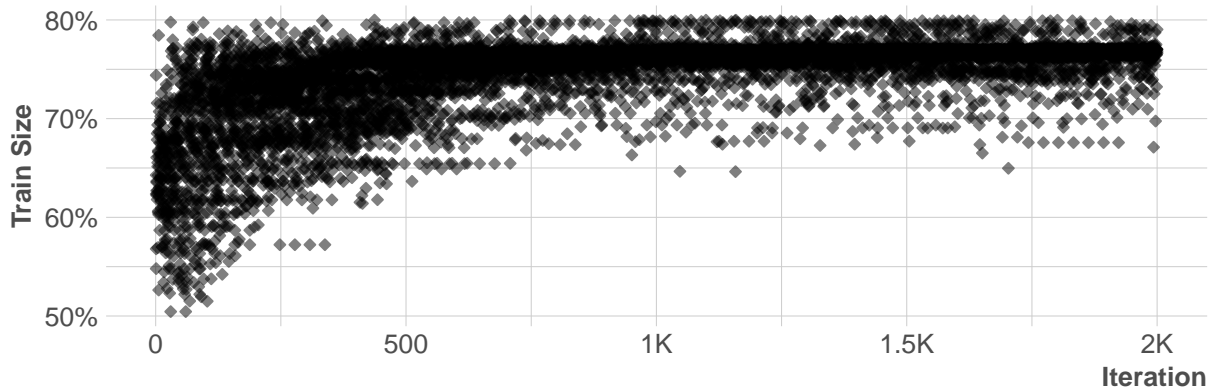
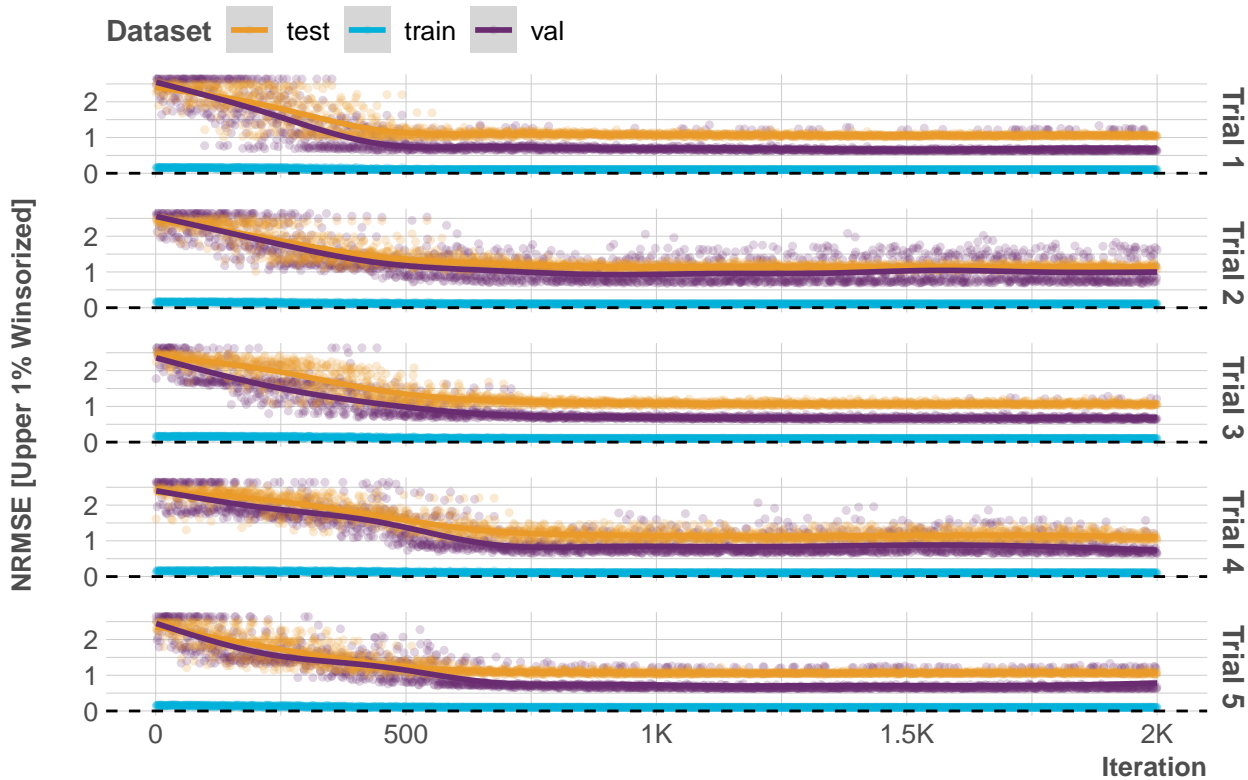
5 trials with 2000 iterations each using TwoPointsDE



DECOMP.RSSD converged: $\text{sd}@qt.20$ 0.081 \leq 0.092 & $|\text{med}@qt.20|$ 0.048 \leq 0.073

NRMSE converged: $\text{sd}@qt.20$ 0.26 \leq 0.55 & $|\text{med}@qt.20|$ 0.68 \leq 1.3

Time-series validation & Convergence

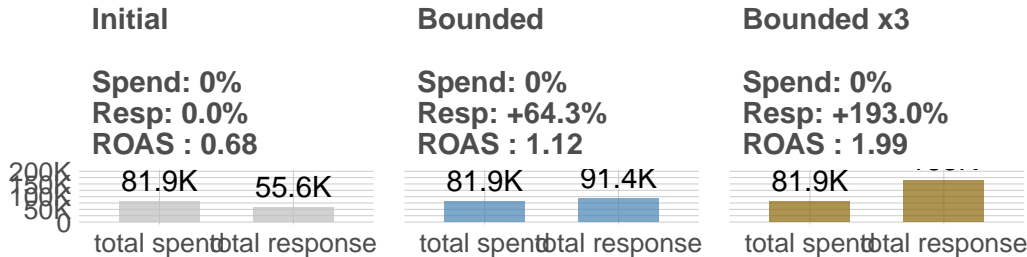


Budget Allocation Onepager for Model ID 1_1707_1

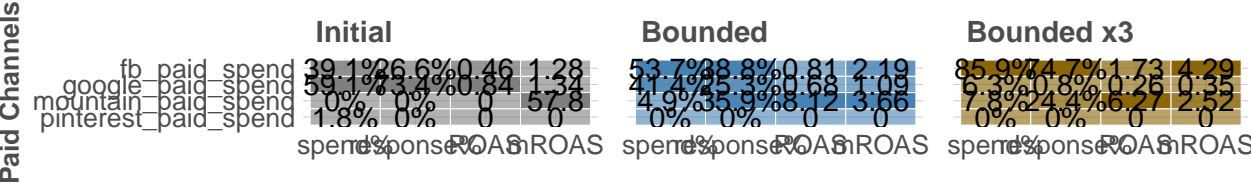
Adj.R2: train = 0.6559, val = 0.7159, test = 0.5686 | NRMSE: train = 0.1008, val = 0.6105, test = 0.6105

Simulation date range: 2023-12-31 to 2024-01-29 (30 days) | Scenario: max_response

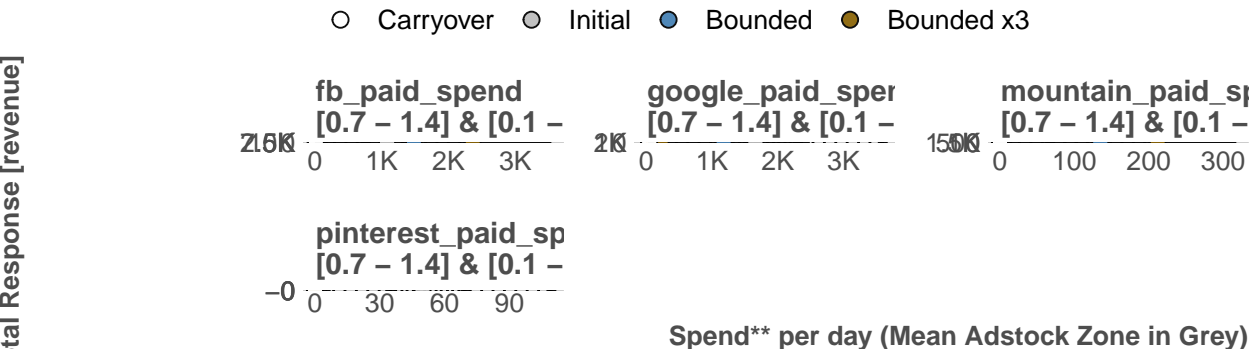
Total Budget Optimization Result



Budget Allocation per Channel*



Simulated Response Curve for Selected Allocation Period



* ROAS = total response / raw spend | mROAS = marginal response / marginal spend
* When reallocating budget, mROAS converges across media within respective bounds
** Dotted lines show budget optimization lower-upper ranges per media