## README FOR PYTHON IMPLEMENTATION OF FPMLE and FPMLE++

(nlmfe package)

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This folder contains files for algorithms 1 (FPMLE) and 2 (FPMLE<sup>++</sup>) developed in Mugnier and Wang (2022, WP).

FPMLE and FPMLE<sup>++</sup> are implemented for *N*-by-*T* data sets in the file *TwoWayFPMLE.py*.

Implementation covers the following models: unit  $i \in \{1, ..., N\}$  at time  $t \in \{1, ..., T\}$  with characteristics  $x_{it} \in R^K$  chooses outcome  $y_{it} \in \mathcal{Y}$  such that

$$\Pr(y_{it} = y \mid x_{i1}, ..., x_{it}, \alpha_i, \xi_t, \beta_i) = g(y; x'_{it}\beta_i + \alpha_i + \xi_t).$$

Model	y	Link function <i>g</i>
Binary Probit	{0,1}	$g(y; x'_{it}\beta_i + \alpha_i + \xi_t)$
		$= I(y=0) \times [1 - \Phi(x_{it}'\beta_i + \alpha_i + \xi_t)]$
		$+ I(y = 1) \times \Phi(x'_{it}\beta_i + \alpha_i + \xi_t)$
Binary Logit	{0,1}	$g(y; x'_{it}\beta_i + \alpha_i + \xi_t)$
		$= I(y = 0) \times [1 - \Lambda(x'_{it}\beta_i + \alpha_i + \xi_t)]$
		$+ I(y = 1) \times \Lambda(x'_{it}\beta_i + \alpha_i + \xi_t)$
Poisson Count	{0,1,2,}	$g(y; x'_{it}\beta_i + \alpha_i + \xi_t)$
		$= \exp(-\exp(x_{it}'\beta_i + \alpha_i + \xi_t)) \exp(y(x_{it}'\beta_i + \alpha_i + \xi_t))$
		= <u>y!</u>

where  $\Phi$  is the cumulative distribution function (cdf) of the standard normal,  $\Lambda(x) = 1/(1 + \exp(-x))$  is the cdf of the standard logistic, for a user-specified unit  $i^*$ ,  $\alpha_{i^*} = 0$ , for a user-specified set of indices  $I \subset \{1, ..., K\}$ ,  $\beta_{i,k} \equiv \beta_k$ ,  $\forall k \in I, \forall i$ . Default is  $I = \{all\ coordinates\}$ , i.e., homogeneous slope coefficient  $\beta_i \equiv \beta$ .

The file *BiasCorrections.py* contains functions for performing the analytical bias corrections developed in Fernandez-Val and Weidner (2016).

The file *PanelPreProcess.py* contains functions for pre-formating unbalanced panel data under a « missing at random » assumption.

The file *func.py* contains various useful functions.

All routines are illustrated by a simple Monte Carlo simulation and an application to trade data in the Jupyer notebook *nlmfe\_in\_practice.ipynb*.

## References:

Fernandez-Val, I. and M. Weidner (2016): «Individual and time effects in nonlinear panel models with large N, T », *Journal of Econometrics*, 192(1), 291-312,

Mugnier, M. and A. Wang (2022): « Identification and (Fast) Estimation of Large Nonlinear Panel Models with Two-Way Fixed Effects », SSRN.