

AI - Øving 2

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Python

```
1 import math
2 from PIL import Image
3
4
5 BOARDNAME = "board-1-1.txt"
6
7 IMAGENAME = "board_1-1.jpeg"
8
9 BOAR = "small"
10 #BOAR = "big"
11 ALGORITHM = "A*"
12 #ALGORITHM = "Dijkstra's"
13 #ALGORITHM = "Breadth-First Search"
14
15 if BOAR == "big":
16     ROWS = 10
17     COLUMNS = 40+1
18 elif BOAR == "small":
19     ROWS = 7
20     COLUMNS = 20 + 1
21
22 # for Image
23 SCALAR = 40
24 SCALAR2 = 30
25 SCALAR3 = 15
26
27 class Node:
28     child = []
29     def __init__(self, F, G, H, child, parent, value, status):
30         self.F = F
31         self.G = G
32         self.H = H
33         self.child.append(child)
34         self.parent = parent
35         self.value = value
36         self.status = status
37
38 def loadBoard(boardname, columns, rows):
39     board = open(boardname, "r")
40     boardMatrix = [[0 for y in range(columns)] for x in range(rows)]
41 ]
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41 column = 0
42 row = 0
43 startPosition = [0, 0]
44 endPosition = [0, 0]
45 for line in board:
46     for element in line:
47         if element == 'r':
48             boardMatrix[column][row] = Node(0, 0, 0, None, None
, 1, None)
49         elif element == '.':
50             boardMatrix[column][row] = Node(0, 0, 0, None, None
, 1, None)
51         elif element == 'g':
52             boardMatrix[column][row] = Node(0, 0, 0, None, None
, 5, None)
53         elif element == 'f':
54             boardMatrix[column][row] = Node(0, 0, 0, None, None
, 10, None)
55         elif element == 'm':
56             boardMatrix[column][row] = Node(0, 0, 0, None, None
, 50, None)
57         elif element == 'w':
58             boardMatrix[column][row] = Node(0, 0, 0, None, None
, 100, None)
59         elif element == 'A':
60             boardMatrix[column][row] = Node(0, 0, 0, None, None
, 0, "start")
61             startPosition[0] = column
62             startPosition[1] = row
63         elif element == 'B':
64             boardMatrix[column][row] = Node(0, 0, 0, None, None
, 0, "end")
65             endPosition[0] = column
66             endPosition[1] = row
67         else:
68             boardMatrix[column][row] = Node(0, 0, 0, None, None
, math.inf, None)
69             row += 1
70             row = 0
71             column += 1
72 board.close()
73 return boardMatrix, startPosition, endPosition
74
75
76 def printBoard(boardMatrix, width, height):
77     xn = 0
78     yn = 0
79     img = Image.new('RGB', (width * SCALAR, height * SCALAR), (255,
255, 255))
80
81     # make map
82     for line in boardMatrix:
83         for element in line:
84             if element.value == 1 and BOAR == "big":
85                 for x in range(SCALAR):
86                     for y in range(SCALAR):
87                         img.putpixel((x+xn,y+yn),(139,69,19))

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88         elif element.value == 5:
89             for x in range(SCALAR):
90                 for y in range(SCALAR):
91                     img.putpixel((x + xn, y + yn), (124,252,0))
92         elif element.value == 10:
93             for x in range(SCALAR):
94                 for y in range(SCALAR):
95                     img.putpixel((x + xn, y + yn), (34,139,34))
96         elif element.value == 50:
97             for x in range(SCALAR):
98                 for y in range(SCALAR):
99                     img.putpixel((x + xn, y + yn),
(128,128,128))
100         elif element.value == 100:
101             for x in range(SCALAR):
102                 for y in range(SCALAR):
103                     img.putpixel((x + xn, y + yn), (0,0,255))
104         elif element.status == "start":
105             for x in range(SCALAR):
106                 for y in range(SCALAR):
107                     img.putpixel((x + xn, y + yn), (255,0,0))
108         elif element.status == "end":
109             for x in range(SCALAR):
110                 for y in range(SCALAR):
111                     img.putpixel((x + xn, y + yn), (0,255,0))
112         elif element.value == math.inf:
113             for x in range(SCALAR):
114                 for y in range(SCALAR):
115                     img.putpixel((x + xn, y + yn), (0,0,0))
116             xn += SCALAR
117             xn = 0
118             yn += SCALAR
119
120     xn = 0
121     yn = 0
122
123     # make path, openList and closedList
124     for line in boardMatrix:
125         for element in line:
126             if element.status == "bestPath":
127                 for x in range(SCALAR - SCALAR2):
128                     for y in range(SCALAR - SCALAR2):
129                         img.putpixel((x+xn+SCALAR3,y+yn+SCALAR3)
,(0,0,0))
130             elif element.status == "openList":
131                 for x in range(SCALAR - SCALAR2):
132                     for y in range(SCALAR - SCALAR2):
133                         img.putpixel((x+xn+SCALAR3,y+yn+SCALAR3)
,(255,215,0))
134             elif element.status == "closedList":
135                 for x in range(SCALAR - SCALAR2):
136                     for y in range(SCALAR - SCALAR2):
137                         img.putpixel((x+xn+SCALAR3,y+yn+SCALAR3)
,(255,0,255))
138             xn += SCALAR
139             xn = 0
140             yn += SCALAR

```

```

141
142 # make grid
143 for x in range(width*SCALAR):
144     for y in range(SCALAR, height*SCALAR, SCALAR):
145         img.putpixel((x, y), (0, 0, 0))
146 for x in range(SCALAR, width*SCALAR, SCALAR):
147     for y in range(height*SCALAR):
148         img.putpixel((x, y), (0, 0, 0))
149
150 img.show()
151 img.save(IMAGENAME)
152
153 def costFunction(boardMatrix, endPosition, child, currentPosition):
154     H = abs(child[0]-endPosition[0]) + abs(child[1]-endPosition[1])
155     G = boardMatrix[currentPosition[0]][currentPosition[1]].G +
156         boardMatrix[child[0]][child[1]].value
157     F = G + H
158     return F, G, H
159
160 def findChild(boardMatrix, currentPosition):
161     newChildren = []
162     for x in range(-1, 2, 2):
163         if 0 <= currentPosition[1]+x < COLUMNS:
164             if boardMatrix[currentPosition[0]][currentPosition[1]+x]
165                 .value < math.inf:
166                 if boardMatrix[currentPosition[0]][currentPosition
167                     [1]+x].parent == None:
168                     newChildren.append([currentPosition[0],
169                         currentPosition[1]+x])
170     for y in range(-1, 2, 2):
171         if 0 <= currentPosition[0]+y < ROWS:
172             if boardMatrix[currentPosition[0]+y][currentPosition
173                 [1]].value < math.inf:
174                 if boardMatrix[currentPosition[0] + y][
175                     currentPosition[1]].parent == None:
176                     newChildren.append([currentPosition[0]+y,
177                         currentPosition[1]])
178     return newChildren
179
180 def addChildrenAndParent(newChildren, currentPosition, boardMatrix,
181     endPosition):
182     boardMatrix[currentPosition[0]][currentPosition[1]].child =
183     newChildren
184     for child in newChildren:
185         F, G, H = costFunction(boardMatrix, endPosition, child,
186             currentPosition)
187         boardMatrix[child[0]][child[1]].F = F
188         boardMatrix[child[0]][child[1]].G = G
189         boardMatrix[child[0]][child[1]].H = H
190         boardMatrix[child[0]][child[1]].child = None
191         boardMatrix[child[0]][child[1]].parent = currentPosition
192
193 def checkNeighborPath(boardMatrix, currentPosition):
194     gNode = boardMatrix[currentPosition[0]][currentPosition[1]].G
195     for x in range(-1, 2, 2):
196         if 0 <= currentPosition[1]+x < COLUMNS:
197             gNeighbor = boardMatrix[currentPosition[0]][

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currentPosition[1]+x].G
188     hNeighbor = boardMatrix[currentPosition[0]][
currentPosition[1]+x].H
189     valueNeighbor = boardMatrix[currentPosition[0]][
currentPosition[1]+x].value
190     if gNode + valueNeighbor < gNeighbor:
191         boardMatrix[currentPosition[0]][currentPosition[1]+x
].parent = currentPosition
192         boardMatrix[currentPosition[0]][currentPosition[1]+x
].G = gNode + valueNeighbor
193         boardMatrix[currentPosition[0]][currentPosition[1]+x
].F = gNode + valueNeighbor + hNeighbor
194         neighborPosition = [currentPosition[0],
currentPosition[1]+x]
195         checkNeighborPath(boardMatrix, neighborPosition)
196 for y in range(-1, 2, 2):
197     if 0 <= currentPosition[0]+y < ROWS:
198         gNeighbor = boardMatrix[currentPosition[0]+y][
currentPosition[1]].G
199         hNeighbor = boardMatrix[currentPosition[0]+y][
currentPosition[1]].H
200         valueNeighbor = boardMatrix[currentPosition[0]+y][
currentPosition[1]].value
201         if gNode + valueNeighbor < gNeighbor:
202             boardMatrix[currentPosition[0]+y][currentPosition
[1]].parent = currentPosition
203             boardMatrix[currentPosition[0]+y][currentPosition
[1]].G = gNode + valueNeighbor
204             boardMatrix[currentPosition[0]+y][currentPosition
[1]].F = gNode + valueNeighbor + hNeighbor
205             neighborPosition = [currentPosition[0]+y,
currentPosition[1]]
206             checkNeighborPath(boardMatrix, neighborPosition)
207
208
209 def pathfinding(boardMatrix, startPosition, endPosition):
210     openList = []
211     closedList = []
212     H = abs(startPosition[0] - endPosition[0]) + abs(startPosition
[1] - endPosition[1])
213     currentPosition = startPosition
214     boardMatrix[currentPosition[0]][currentPosition[1]].H = H
215     boardMatrix[currentPosition[0]][currentPosition[1]].F = H
216     openList.append(currentPosition)
217
218     while openList:
219
220         if ALGORITHM == "A*":
221             bestF = boardMatrix[openList[-1][0]][openList[-1][1]].F
222             bestNode = openList[-1]
223             for node in openList:
224                 if bestF > boardMatrix[node[0]][node[1]].F:
225                     bestF = boardMatrix[node[0]][node[1]].F
226                     bestNode = node
227
228             elif ALGORITHM == "Dijkstras":
229                 bestG = boardMatrix[openList[-1][0]][openList[-1][1]].G

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230         bestNode = openList[-1]
231         for node in openList:
232             if bestG > boardMatrix[node[0]][node[1]].G:
233                 bestG = boardMatrix[node[0]][node[1]].G
234                 bestNode = node
235
236         elif ALGORITHM == "Breadth-First Search":
237             bestNode = openList[0]
238
239             currentPosition = bestNode
240             if currentPosition == endPosition:
241                 break
242             openList.remove(currentPosition)
243             closedList.append(currentPosition)
244             newChildren = findChild(boardMatrix, currentPosition)
245             if startPosition in newChildren:
246                 newChildren.remove(startPosition)
247             for child in newChildren:
248                 openList.append(child)
249             addChildrenAndParent(newChildren, currentPosition,
boardMatrix, endPosition)
250             checkNeighborPath(boardMatrix, currentPosition)
251
252         nodeList = ["start", "end"]
253         for node in openList:
254             if boardMatrix[node[0]][node[1]].status not in nodeList:
255                 boardMatrix[node[0]][node[1]].status = "openList"
256         for node in closedList:
257             if boardMatrix[node[0]][node[1]].status not in nodeList:
258                 boardMatrix[node[0]][node[1]].status = "closedList"
259         path = boardMatrix[endPosition[0]][endPosition[1]].parent
260         while path is not None:
261             if boardMatrix[path[0]][path[1]].value > 0:
262                 boardMatrix[path[0]][path[1]].status = "bestPath"
263                 path = boardMatrix[path[0]][path[1]].parent
264         return boardMatrix
265
266
267
268 def main():
269
270     boardMatrix, startPosition, endPosition = loadBoard(BOARDNAME,
COLUMNS, ROWS)
271
272     boardMatrix = pathfinding(boardMatrix, startPosition,
endPosition)
273
274     printBoard(boardMatrix, COLUMNS, ROWS)
275
276 main()

```

Tabell

Fargekoder			
Farge	Bokstav	Forklaring	Verdi
	A	Start	0
	B	Slutt	0
		OpenList	
		ClosedList	
	r	Vann	1
	g	Fjell	5
	f	Skog	10
	m	Gress	50
	w	Vei	100
	#	Vegg	inf

Part 1

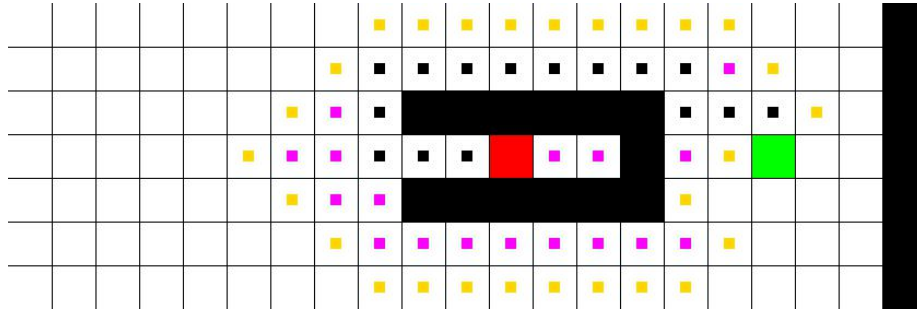


Figure 1: Board-1-1 med A*

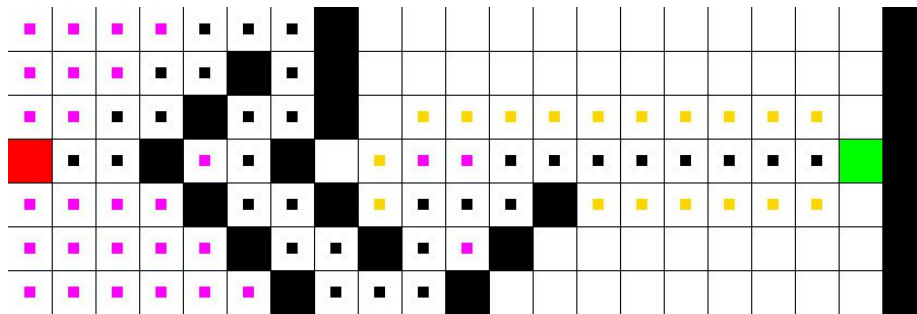


Figure 2: Board-1-2 med A*

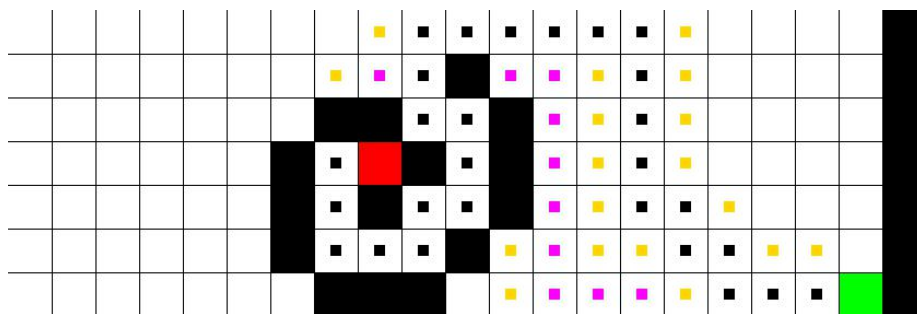


Figure 3: Board-1-3 med A*

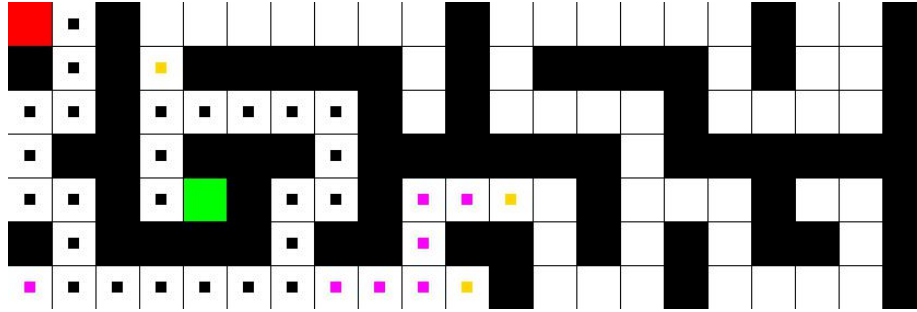


Figure 4: Board-1-4 med A*

Part 2

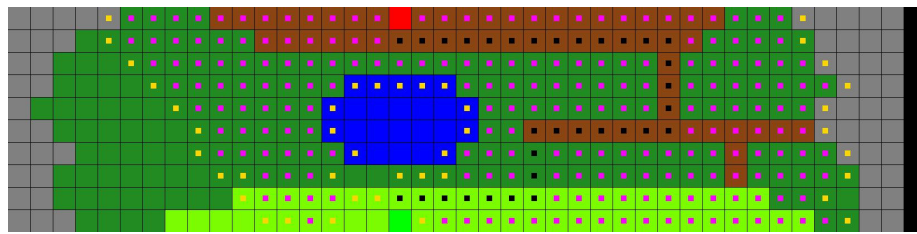


Figure 5: Board-2-1 med A*

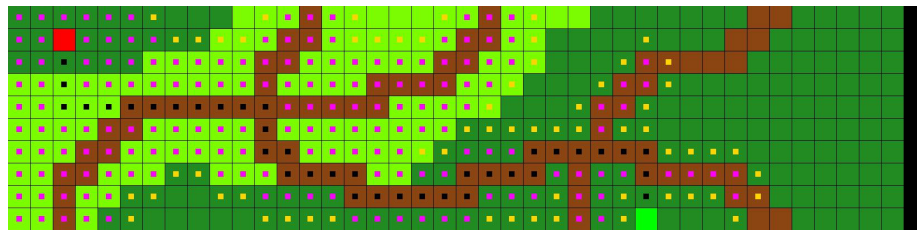


Figure 6: Board-2-2 med A*

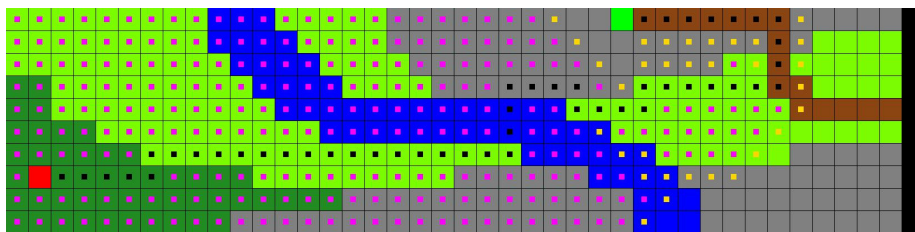


Figure 7: Board-2-3 med A*

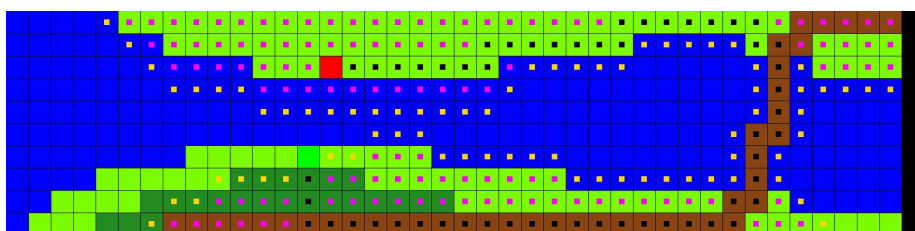


Figure 8: Board-2-4 med A*

Part 3

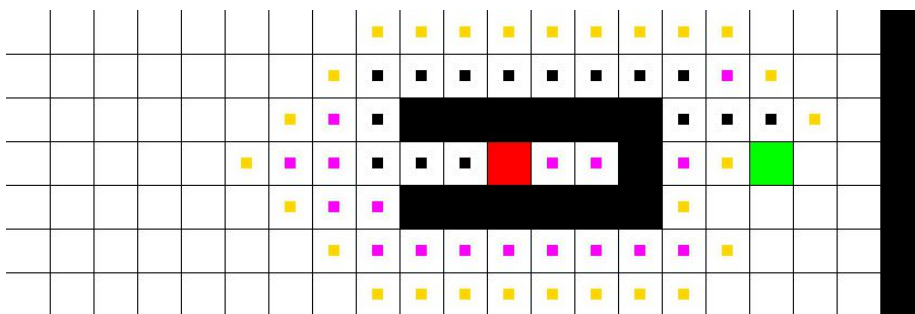


Figure 9: Board-1-1 med A*

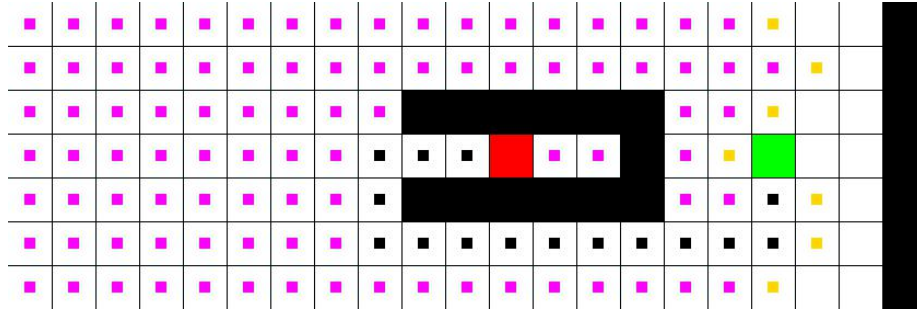


Figure 10: Board-1-1 med Dijkstra's

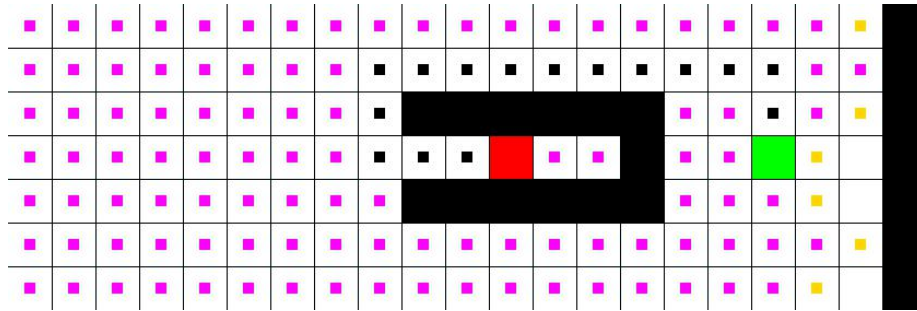


Figure 11: Board-1-1 med Breadth-First Search

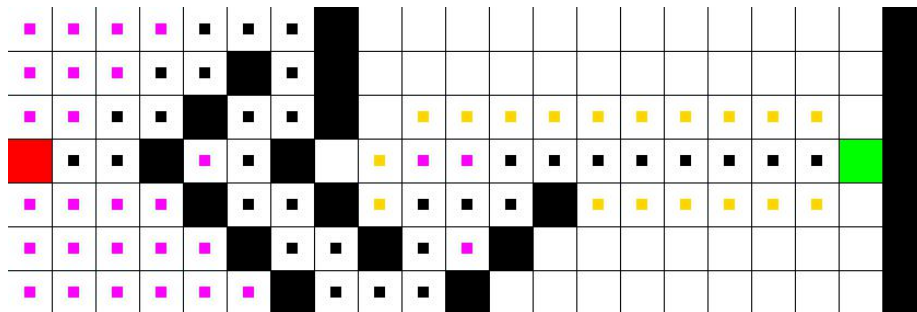


Figure 12: Board-1-2 med A*

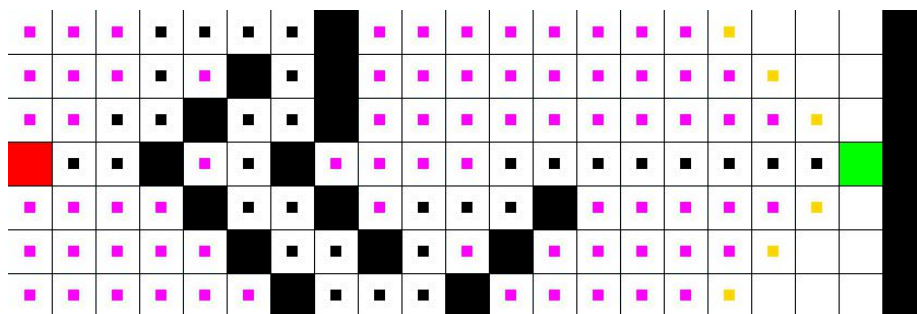


Figure 13: Board-1-2 med Dijkstra's

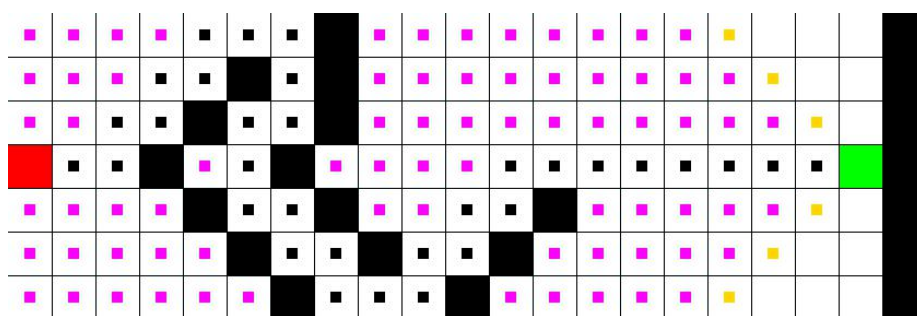


Figure 14: Board-1-2 med Breadth-First Search

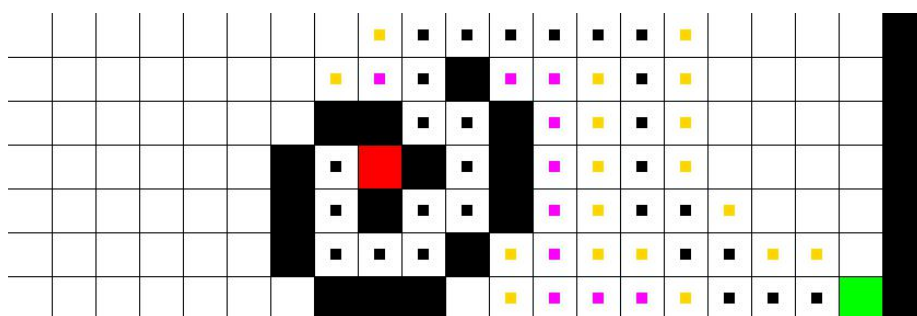


Figure 15: Board-1-3 med A*

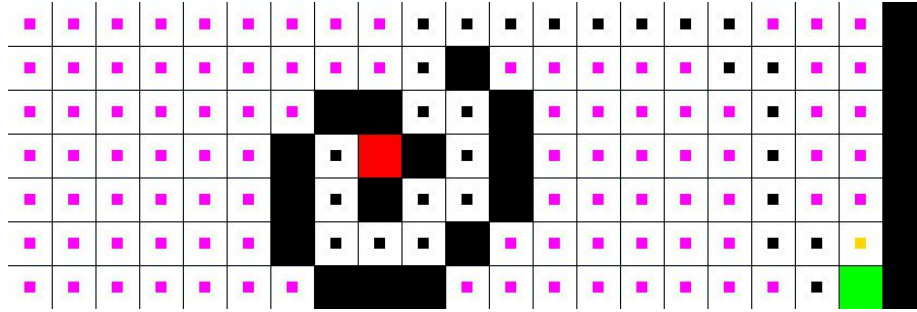


Figure 16: Board-1-3 med Dijkstra's

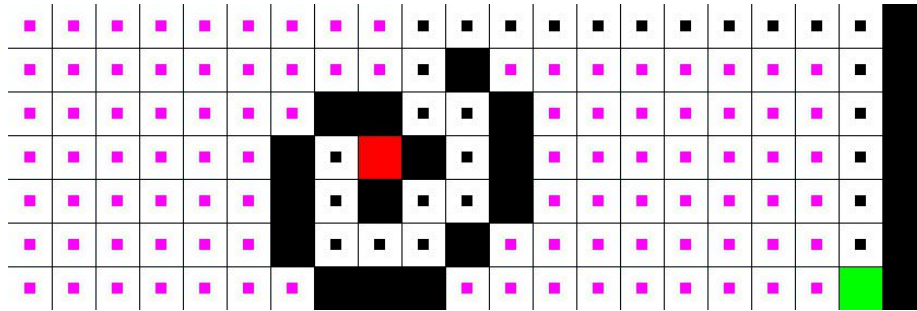


Figure 17: Board-1-3 med Breadth-First Search

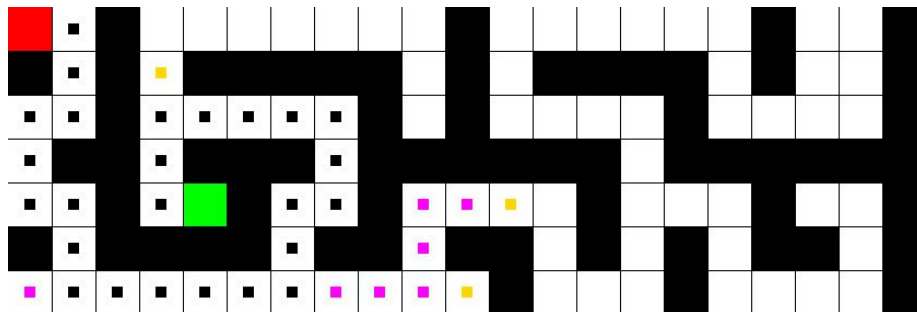


Figure 18: Board-1-4 med A*

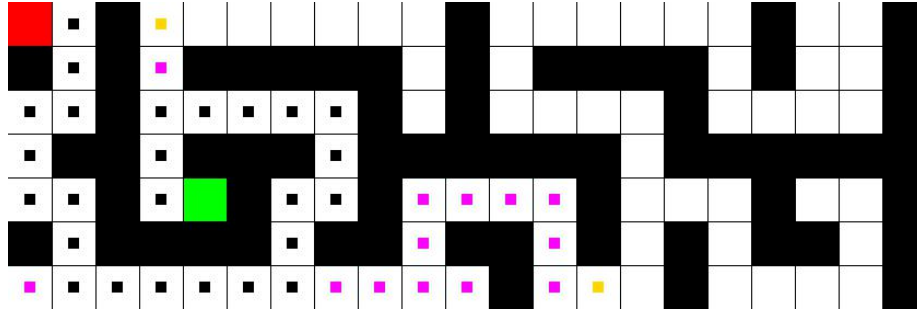


Figure 19: Board-1-4 med Dijkstra's

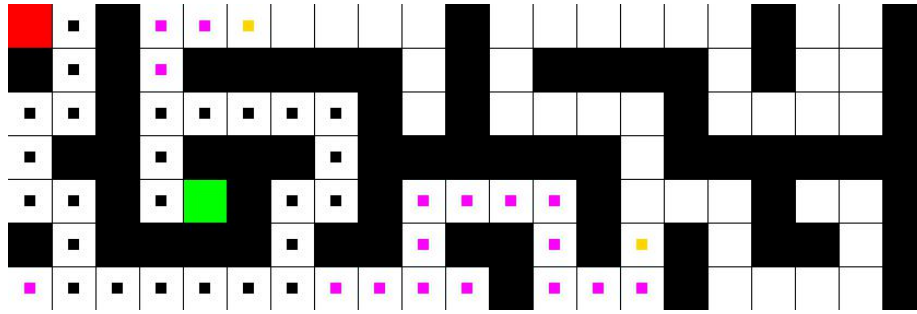


Figure 20: Board-1-4 med Breadth-First Search

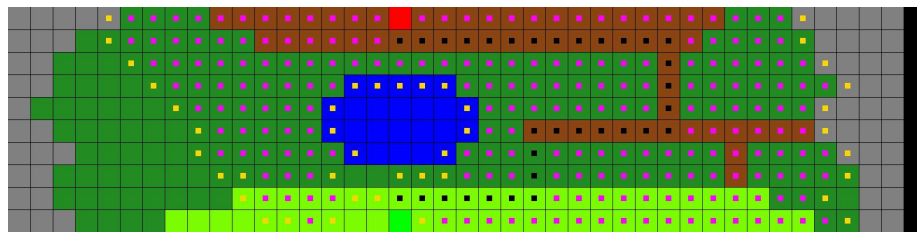


Figure 21: Board-2-1 med A*

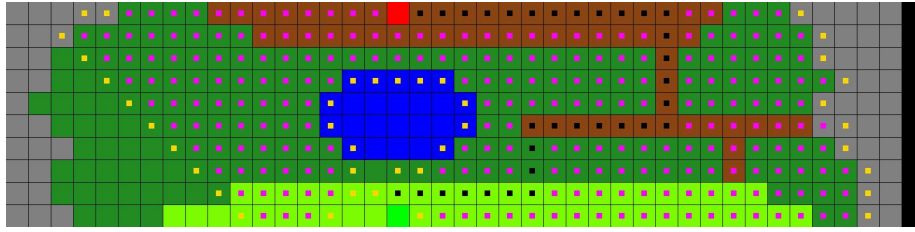


Figure 22: Board-2-1 med Dijkstra's

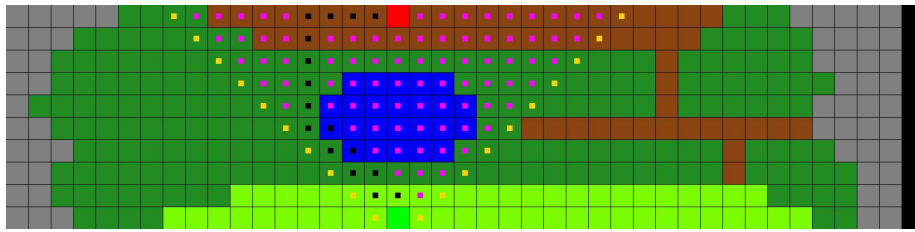


Figure 23: Board-2-1 med Breadth-First Search

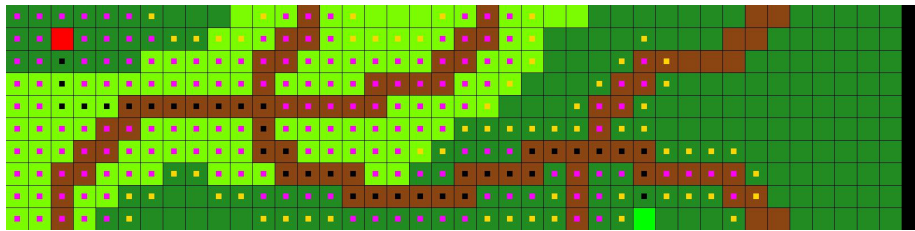


Figure 24: Board-2-2 med A*

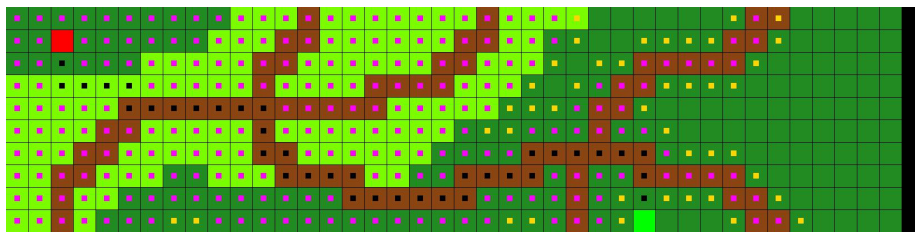


Figure 25: Board-2-2 med Dijkstra's

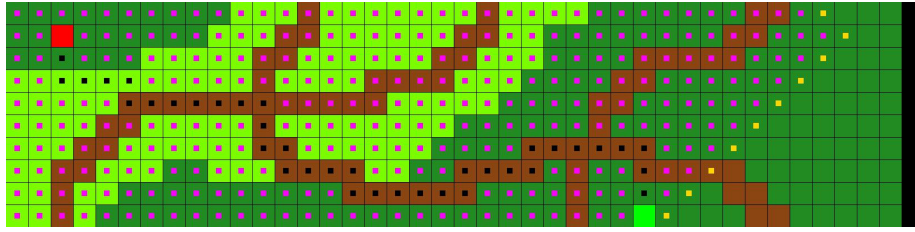


Figure 26: Board-2-2 med Breadth-First Search

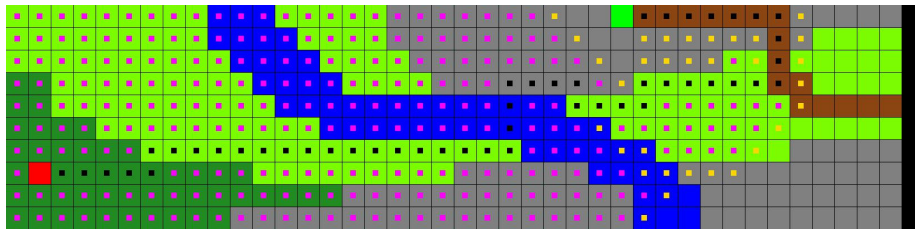


Figure 27: Board-2-3 med A*

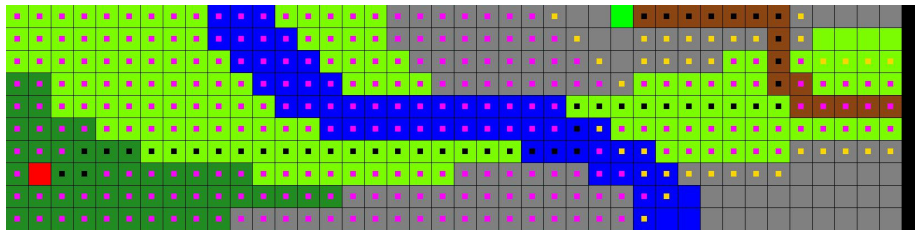


Figure 28: Board-2-3 med Dijkstra's

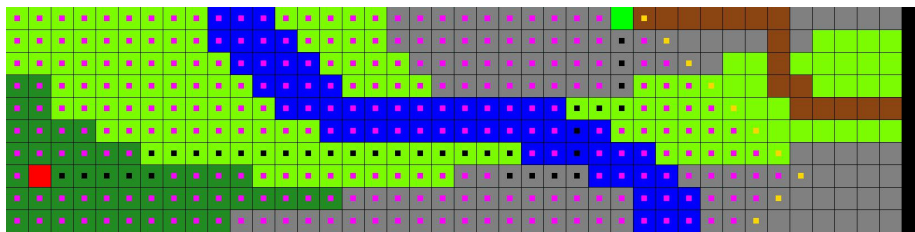


Figure 29: Board-2-3 med Breadth-First Search

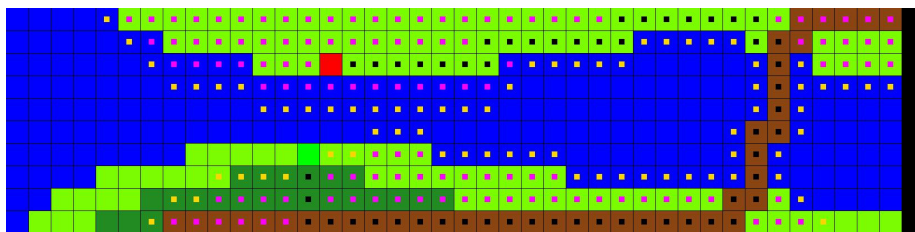


Figure 30: Board-2-4 med A*

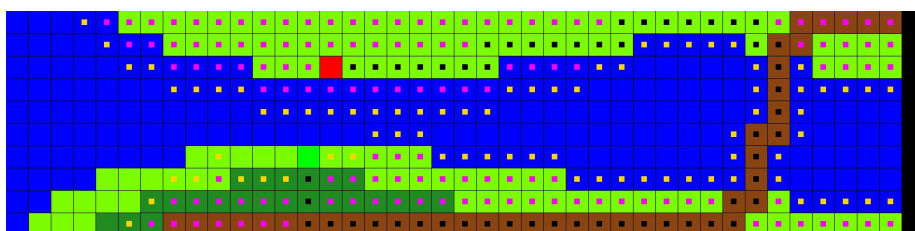


Figure 31: Board-2-4 med Dijkstra's

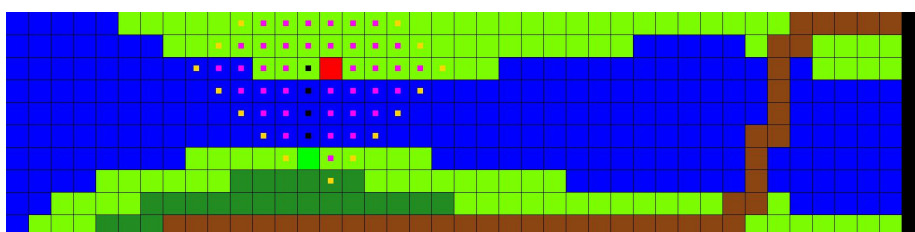


Figure 32: Board-2-4 med Breadth-First Search

3.3

For each game board processed above, a brief analysis of (a) any differences in the path found by A*, BFS and Dijkstra, and (b) any interesting differences in the number of open and closed between for the different algorithms.

- (a) Man ser at når kostnadden for alle rutene er 1 så finner alltid alle algoritmene den raskeste veien. Her er A* helt tydelig raskest da den bruker $F = G + H$ for å velge neste rute den skal undersøke, mens Dijkstra bruker bare H og BFS bruker første noden som ble lagt til i OpenList. Når rutene har forskjellige verdier vil A* og Dijkstra alltid finne den raskeste veien, mens BFS finner den raskeste veien innenfor det området den har undersøkt i det den finner den siste ruten. For eksempel finner BFS den

raskeste veien fra A til B på brett 2-2 (Figure 26), siden her er den raskeste veien innenfor det området den allerede har søkt i. Mens på brett 2-4 (Figure 32) finner den ikke den raskeste veien, siden her finner den B tidlig og setter opp den raskeste veien ut i fra de rutene den har søkt gjennom. Ser at det er små forskjeller på de beste rutene da det er flere av dem på noen av brettene. Dette varierer ut i fra hvilken node som blir først sjekket av de nodene som er like gode.

- (b) Man ser at når alle algoritmene finner den raskeste veien er det alltid A^* som har færrest noder i ClosedList. Det betyr at A^* alltid er den raskeste algoritmen for denne typen problem av de tre algoritmene, siden den søker gjennom færrest noder.