ParaSail Reference Manual – Draft

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Introduction

ParaSail stands for "Parallel Specification and Implementation Language," and is designed with the principle that if you want programmers to write parallel algorithms, you have to immerse them in parallelism, and force them to work harder to make things sequential. In ParaSail, parallelism is everywhere, and threads are treated as resources like virtual memory – a given computation can use 100s of threads in the same way it might use 100s of pages of virtual memory. ParaSail supports both lock-based and lock-free concurrent objects.

ParaSail also supports annotations, and in fact requires them in some cases if they are needed to prove that a given operation is safe. In particular, all checks that might normally be thought of as run-time checks (if checked by the language at all) are compile-time checks in ParaSail. This includes uninitialized variables, array index out of bounds, null pointers, race conditions, numeric overflow, etc. If an operation would overflow or go outside of an array given certain inputs, then a precondition is required to prevent such inputs from being passed to the operation. ParaSail is designed to support a *formal* approach to software design, with a relatively static model to simplify proving properties about the software, but with an explicit ability to specify run-time polymorphism where it is needed.

ParaSail has only four basic concepts – Modules, Types, Objects, and Operations. Every type is an instantiation of a module. An object is an instance of some type. An operation operates on objects.

There are no global variables. Any object to be updated by an operation must be an explicit input or output to the operation.

ParaSail has user-defined indexing (analogous to arrays or tables), user-defined literals (integers, reals, strings, characters, and enumerations), user-defined "aggregates," etc. Every type is the instantiation of some module, including those that might be considered the built-in types, and there are no "special" operators or constructs that only a built-in type can utilize.

ParaSail has no pointers, though it has references, optional and expandable objects, and user-defined indexing, which together provide a rich set of functionally equivalent capabilities without any hidden aliasing nor any hidden race conditions.

1.1 Language Design Principles

Below are some of the fundamental language design principles we tried to follow while designing ParaSail. Of course, at times we faced a conflict, so at those times tradeoffs had to be made. Although these are expressed as goals, by and large we believe they have been accomplished in the current design.

• The language should be easy to read, and look familiar to a broad swath of existing programmers, from the ranks of programmers in the Algol/Pascal/Ada/Eiffel family, to the programmers in the C/C++/Java/C# family, to the programmers in the ML/Haskell and Lisp/Scheme communities. Readability is to be emphasized over terseness, and where symbols are used, they should be familiar from existing languages, mathematics, or logic. Although extended character sets are more available

these days, most keyboards are still largely limited to the ASCII, or at best, the Latin-1, character set, so the language should not depend on the use of characters that are a chore to type.

Programs are often scanned backward, so ending indicators should be as informative as starting indicators for composite constructs. For example, "end loop" or "end class Stack" rather than simply "end" or "\rightarrow".

- Parallelism should be built into the language to the extent that it is more natural to write parallel code than to write explicitly sequential code, and that the resulting programs can easily take advantage of as many cores as are available on the host computer.
- The language should have one primary way to do something rather than two or three nearly equivalent ones. Nonessential features should be eliminated, especially those that are error prone or complicate the testing or proof process. User-defined types and language-defined types should use the same syntax and have the same capabilities.
- All code should be parameterized to some extent, since it is arguable that all code would benefit from being parameterized over the precision of the numeric types, the character code of the strings involved, or the element types of the data structures being defined. In other words, all modules should be generic templates or equivalent. But the semantics should be defined so that the parameterized modules can be fully compiled prior to being instantiated.
- The language should be inherently safe, in that the compiler should detect all potential race conditions, as well as all potential runtime errors such as the use of uninitialized data, out of bounds indices, overflowing numeric calculations, etc. Given the advances in static analysis, there is no reason that the compiler cannot eliminate all possible sources of run-time errors.

Programming is about human programmers clearly and correctly communicating with at least two audiences: 1) other human programmers, both current and future, and 2) a very literally-minded machine-based compiler or interpreter. What is needed is *human engineering*, which is the process of adapting a technology to be most useful to humans, by minimizing opportunities for errors, taking advantage of commonly understood principles, using terminology and symbols consistently and in ways that are familiar, and eliminating unnecessary complexity.

Here are some additional somewhat lower level principles followed during the ParaSail design:

- Full generality should be balanced against testability and provability. In particular, though passing functions and types as parameters is clearly useful, it is arguable whether full upward closures and types as true first-class objects (such as the *class* objects in *Smalltalk*), are useful enough to justify the significant testing and proof burdens associated with such constructs. The more disciplined packaging of type and function provided by statically-typed object-oriented programming can match essentially all of the capability provided by upward closures and types as first-class objects, while providing, through behavioral subtyping and other similar principles, a more tractable testing and proof problem.
- Avoid constructs that require fine-grained asynchronous garbage collection if possible. Garbage collectors are notoriously hard to test and prove formally, and are made even more complex when real-time and multi-processor requirements are added. Mark/release strategies, and more generally region-based storage management, as in the *Cyclone* language, suggest possible alternative approaches.
- Mutual exclusion and waiting for a condition to be true should be automatic as part of calling an
 operation for which it is relevant. This is as opposed to explicit lock/unlock, or explicit wait/signal.
 Automatic locking and/or waiting simplifies programming and eliminates numerous sources for errors
 in parallel programs with inter-thread synchronization. The result is also easier to understand and to
 prove correct.

Lexical Elements

2.1 Character Set

ParaSail programs are written using graphic characters from the ISO-10646 (Unicode) character set, as well as horizontal tab, form feed, carriage return, and line feed. A line feed terminates the line.

```
digit ::= 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9
binary_digit ::= 0 | 1
hex_digit ::= digit | A..F | a..f
extended_digit ::= digit | A..Z | a..z
```

2.2 Delimiters

The following single graphic characters are delimeters in ParaSail:

```
(){}[],;.:|<>+-*/'?
```

The following combinations of graphic characters are delimeters in ParaSail:

```
:: ;; || == != =? <= >=
==> -> ** => [[ ]] << >>
:= <== <=> <|= += -= *= /= **= <<= >>= |=
.. <.. .. < <.. <
```

The following combinations of graphic characters have special significance in ParaSail:

```
and= or= xor=
```

2.3 Identifiers

Identifiers start with a letter, and continue with letters, digits, and underscores.

```
identifier ::= letter { _ | letter | digit }
```

Upper and lower case is significant in identifiers. Letters include any graphic character in the ISO-10646 character set that is considered a letter. An identifier must not be the same as a ParaSail reserved word (see 2.6).

Examples:

```
X, A_B, a123, A123, This_Is_An_Identifier, Xyz_
```

2.4 Literals

There are five kinds of literals in ParaSail: integer, real, character, string, and enumeration.

```
literal ::=
   integer_literal
   | real_literal
   | character_literal
   | string_literal
   | enumeration_literal
```

2.4.1 Integer literals

Integer literals are by default decimal. Integers may also be written in binary, hexadecimal, or with an explicit base in the range 2 to 36.

Integer literals are of type Univ_Integer.

```
integer_literal ::=
    decimal_integer_literal
| binary_integer_literal
| hex_integer_literal
| based_integer_literal
| decimal_integer_literal ::= decimal_numeral
| binary_integer_literal ::= 0 (b|B) binary_digit { [_] binary_digit}
| hex_integer_literal ::= 0 (x|X) hex_numeral
| based_integer_literal ::= decimal_numeral # extended_numeral #
| decimal_numeral ::= digit { [_] digit }
| hex_numeral ::= hex_digit { [_] hex_digit}
| extended_numeral ::= extended_digit { [_] extended_digit }
| Examples:
| 42, 1_000_000, 0xDEAD_BEEF, 8#0177#
```

2.4.2 Real Literals

Real literals are by default decimal, with an optional decimal exponent indicating the power of 10 by which the value is to be multiplied. Reals may also be written with an explicit base in the range 2 to 36, with a decimal exponent indicating the power of the base by which the value is to be multiplied.

Real literals are of type Univ_Real.

```
real_literal ::= decimal_real_literal | based_real_literal

decimal_real_literal ::= decimal_numeral . decimal_numeral [exponent]

based_real_literal ::= decimal_numeral . extended_numeral # [exponent]

exponent ::= (e|E)[+|-] decimal_numeral

Examples:
3.14159, 0.15, 16#F.FFFF_FFFF_FFFF#e+16
```

2.4.3 Character Literals

Character literals are expressed as a pair of apostrophes bracketing a single unescaped_character, being any graphical character of the ISO-10646 character set other than apostrophe and backslash, or a single escaped_character, being a backslash followed by an escapable_character or a hexadecimal character code.

Character literals are of type Univ_Character.

```
character_literal ::= ' unescaped_character ' | ' escaped_character '
escaped_character ::= \ escapable_character | \ # hex_numeral #
escapable_character ::= \ | ' | " | n | r | t | f | 0
```

The following escapable characters have the following interpretation when preceded by \:

```
\ -- backslash
' -- apostrophe
" -- double quote
n -- line feed
r -- carriage return
t -- horizontal tab
f -- form feed
0 -- Nul
```

A character literal of the form '\#hex_numeral#' specifies the character whose ISO-10646 code is equal to the value of the given hex_numeral.

Examples:

```
'a', '0', '\'', '\r', '\#03_CO#'
```

2.4.4 String Literals

String literals are a sequence of graphical characters of the ISO-10646 character set enclosed in double quotes. The backslash and double-quote characters may appear only as part of an escaped_character. String literals are of type Univ_String.

```
string_literal ::= " { unescaped_character | escaped_character } "
```

Example:

"This is a multiline message\n and this is the second line."

2.4.5 Enumeration Literals

Enumeration literals are expressed with a # followed by an identifier or reserved word. Enumeration literals are of type Univ_Enumeration.

```
enumeration_literal ::= # ( identifier | reserved_word )
```

Examples:

#red, #true, #Monday

2.5 Comments

Comments in ParaSail start with // and continue to the end of the line. Examples:

```
// According to the Algol 68 report,
// comments are for the enlightenment of the human reader.
```

2.6 Reserved Words

The following words are reserved in ParaSail:

abs	exit	locked
abstract	extends	loop
all	exports	mod
and	for	new
block	forward	not
case	func	null
class	global	of
concurrent	if	op
const	implements	optional
continue	import	or
each	in	private
else	interface	queued
elsif	is	ref
end	lambda	rem

All reserved words in ParaSail are in lower case.

return

reverse separate some

then type until var while with xor

Types and Objects

In ParaSail, every object is an instance of some type, and every type is defined by instantiating a module and/or applying a value constraint on an existing type.

3.1 Types

A type is declared by instantiating the interface of a module (see 7.1), or by constraining an existing type, using the following syntax:

```
type_declaration ::=
   'type' identifier 'is' ['new'] type_specifier [ value_constraint ] ';'
type_specifier ::= type_name | module_name '<' module_actuals '>'
value_constraint ::= annotation
```

See Chapter 9 for the syntax of an annotation.

The presence of 'new' in a type_declaration indicates that the type is not equivalent to any other type. If no 'new' is specified, then the type is value-equivalent to any other instantiation of the same module with value-equivalent actuals. The type is constraint-equivalent to any other instantiation of the same module with constraint-equivalent actuals, and with the same value_constraint annotation, if any. A value_constraint does not create a new type per se, but instead represents a constrained subtype of a type, with the constraint(s) determining which values belong to the subtype. In other words, name equivalence is used between two types if either was declared with the reserved word 'new.' Otherwise structural equivalence applies, where the basic structure is determined by the actuals supplied to the module instantiation, and the subset of values of the type is determined by the value_constraint annotations, if any.

Two types are considered *significantly* different if they result from instantiating different modules, or if they result from distinct instantiations of the same module at least one of which included the 'new' reserved word.

Example:

Given the interface of a List module defined as follows (see 7.1):

```
interface List <Element_Type is Assignable <>> is
  func Create() -> List;
func Is_Empty(L : List) -> Boolean;
func Append(var L : List; Elem : Element_Type);
func Remove_First(var L : List) -> optional Element_Type;
func Nth_Element(ref L : List; N : Univ_Integer)
  -> ref optional Element;
```

```
end interface List;
```

A specific kind of list may be declared as follows:

```
type Bool_List is List < Boolean >;
```

This declares a Bool_List type which represents a list of Booleans.

3.2 Objects

Objects contain data, and may either be variables (declared with 'var'), allowing their data to be changed after initialization, or constants (declared with 'const'), meaning the initial value of the data of the object cannot be changed during the life of the object.

An object is declared using the following syntax:

```
object_declaration ::=
    uninitialized_object_declaration
| initialized_object_declaration

uninitialized_object_declaration ::=
    var_or_const identifier ':' object_type [ container_specifier ] ';'

initialized_object_declaration ::=
    var_or_const identifier [ ':' object_type ] [ container_specifier ] ':=' expression ';'
    | var_or_const identifier [ ':' object_type ] '<==' object_name ';'

var_or_const ::= 'var' | 'const'

object_type ::= object_qualifier type_specifier [ value_constraint ]

object_qualifier ::= [ 'optional' ] [ 'concurrent' ]</pre>
```

See section 8.4 for syntax of container_specifier.

The value of an object may be null only if it is declared to have an 'optional' type. An uninitialized object with an 'optional' type has the null value initially.

An uninitialized object that has a non-optional type must be assigned a value prior to being referenced. An uninitialized constant object may be assigned a value at most once, and if it has an optional type, must not be assigned a value after its (null) value is referenced.

When an object is initialized using the '<==' move operation (as opposed to the ':=' assign operation – see 5.2 Assignment Statements), the initial value comes from an existing object (identified by an object_name). This value is moved into the new object, and the existing object is set to the null value as a side-effect. The object_name must denote a variable with an 'optional' type.

Examples:

```
var BL : Bool_List := Create();
const T : Boolean := #true;
var Result : optional T;
var Next <== Tree.Left;</pre>
```

These declare a variable boolean list, a constant with Boolean value #true, a variable Result with implicit initial value of null, and a variable Next initialized by moving the value from Tree.Left, leaving Tree.Left null.

3.3 Object References

A reference to an existing object is declared using the following syntax:

```
object_reference_declaration ::=
  'ref' [ var_or_const ] identifier [':' type_specifier ] '=>' object_name ';'
```

A variable reference is only permitted to a variable object. A constant reference provides read-only access to an object, whether or not the object itself is a constant. A reference not specified as 'var' or 'const' allows the same access as that provided by the object to which it refers.

Examples:

```
ref const Left => L.Left_Subtree;
ref var X => M[I];
ref Max => First_Element(A);
```

These create a read-only reference to the Left_Subtree component of L, a read-write reference to the Ith element of M (which must be a variable), and a reference to the first element of A, which is a read-write reference only if A is a variable. Note that in the third example, it is assumed that the First_Element function takes a "ref" input and returns a "ref" output (see 6.1);

3.4 Declarations and Identifiers

The identifier introduced by the declaration of a type or object must not denote a currently visible declaration. However, when declaring a module formal, an operation input, or an operation output, the identifier may be omitted, in which case it is taken, in the case of a type formal, from the module name, in the case of an input to an operation, from the type name, and in the case of an operation output, from the operation name. In addition, when inside a module, the module's simple name also identifies a type which is the current instance of the module.

The identifier introduced by the declaration of an operation must not denote a currently visible interface, type, or object, but may be the same as that of an existing operation, provided it differs *significantly* in the types of one or more inputs or outputs (see 3.1 for definition of *significantly* different types).

The full name of a module must be unique within a given program.

Names and Expressions

4.1 Names

Names denote modules, types, objects, and operations.

```
name ::= module_name | type_name | object_name | operation_name
module_name ::= [ module_name '::' ] identifier

type_name ::= type_identifier [ '+' ]

type_identifier ::= [ type_identifier '::' ] identifier

object_name ::= identifier
| object_indexing_or_slicing
| operation_call
| component_selection
```

See Operation Calls (Section 6.3) for the syntax of operation_name and operation_call. See Object Indexing and Slicing (Section 8.1) for the syntax of object_indexing_or_slicing.

4.1.1 Component Selection

If an object_declaration occurs immediately within the interface (see 7.1) or class (see 7.3) for a module, and the declaration is not for an initialized 'const' object, then it declares a *component* object. Components declared within a module comprise the data of each object of a type based on the module.

Components are named by naming the enclosing object, then a '.', and then the identifier of the component:

```
component_selection ::= object_name '.' identifier
Examples:
   C.Real_Part , Point .X, List_Node .Next , T.Right_Subtree
```

4.2 Expressions

```
expression ::=
    [ type_identifier '::' ] literal
  | 'null'
  | object_name
  | postcondition_value
  | initial_value_specification
  | unary_operator expression
  | expression binary_operator expression
  | membership_test
  | null_test
  | quantified_expression
  | type_conversion
  [ type_identifier '::' ] bracketed_expression
bracketed_expression ::=
    aggregate
  | conditional_expression
  | map_reduce_expression
  | universal_conversion
  / '(' expression ')'
```

Literals evaluate to a value of a corresponding universal type, and are implicitly convertible to a type that has a corresponding "from_univ" operator, so long as the value satisfies the precondition of the operator.

The reserved word 'null' evaluates to the null value, which can be used to initialize any object declared to have an 'optional' type.

A type_identifier followed by '::' may be used to specify explicitly the result type of (the implicit conversion of) a literal, or of a bracketed_expression – one of the forms of expression that is enclosed in () or [], where the type might not be resolvable without additional context.

See Annotations (Chapter 9) for the syntax of postcondition_value and universal_conversion. See 4.2.7 for the syntax of initial_value_specification.

Examples:

```
Y:= "This_is_a_string_literal"; // Y must be of a type with a "from_univ" operator // from Univ_String

return null; // function must have a return type of the form "optional T" // indicating it might return "null" rather than a value of type T

Display(Output, Complex::(Real \Rightarrow 1.0, Imaginary \Rightarrow 1.0));
// Explicitly specify the result type of an aggregate
```

4.2.1 Unary and Binary Operators

The following are the unary operators in ParaSail:

```
"+", "-", "abs", "not"
```

The following are the binary operators in ParaSail:

```
"**" -- Exponentiation
"*", "/", "rem", "mod" -- Multiply, Divide, Remainder, and Modulo operators
```

```
"+", "-"
                         -- Addition and subtraction
"..", "<...",
                         -- Interval operators; closed, open-closed,
"..<", "<..<"
                          -- closed-open, open-open
" | "
                         -- Used to combine elements into a container
"<", "<=", "=="
                         -- The usual relational operators
"!=", ">=", ">"
"=?"
                         -- The "compare" operator; all relational
                         -- operators are defined in terms of "=?"
"<<", ">>"
                         -- left shift and right shift
"and", "or", "xor"
                         -- The basic boolean operators
"and then", "or else"
                         -- Short-circuit boolean operators
"==>"
                         -- "implication" operator
```

The highest precedence operators are the unary operators and the exponentiation ("**") operator. The next lower precedence operators are the multiplication, division, and remainder operators. The next lower precedence operators are the addition and subtraction operators. Next are the interval operators. Next the *combine* operator ("|"). Next the relational, compare, and shift operators. Lowest are the boolean operators.

Addition, subtraction, multiplication, and division are left-associative. Exponentiation is right-associative. For other operators, parentheses are required to indicate associativity among operators at the same level of precedence, except that for the boolean operators, a string of uses of the same operator do not require parentheses, and are treated as left-associative.

The binary compare operator ("=?") returns an Ordering value indicating the relation between the two inputs, being #less, #equal, #greater, or #unordered. The value #unordered is used for types with only a partial ordering. For example, the "=?" operator for sets would typically return #equal if the sets have the same members, #less if the left operand is a proper subset of the right, #greater if the left operand is a proper superset of the right, and #unordered otherwise. All of the other relational operators are defined in terms of "=?" - only "=?" is user-definable for a given type.

The evaluation of an expression using a unary or binary operator is in general equivalent to a call on the corresponding operation, meaning that the operands are evaluated in parallel and then the operation is called (see 6.3). The short-circuit boolean operators "and then" and "or else" and the implication operator "==>" are implemented in terms of the corresponding if_expression (see 4.2.6):

```
A and then B // equivalent to (if A then B else #false)
A or else B // equivalent to (if A then #true else B)
A \Rightharpoonup B // equivalent to (if A then B else #true)
```

Examples of unary and binary operators:

```
S1 = ? \ S2 \qquad // \ Compare \ S1 \ and \ S2, \\ // \ return \ \#less \ , \ \#equal \ , \ \#greater \ , \ or \ \#unordered X ** \ 3 \qquad // \ X \ cubed abs \ (X - Y) \qquad // \ absolute \ value \ of \ difference 0 \ .. < \ Length \qquad // \ The \ interval \ 0, \ 1, \ .. \ Length - 1 (A \ and \ B) \ or \ C \qquad // \ parentheses \ required A \ or \ B \ or \ C \qquad // \ parentheses \ not \ required X * \ Y + U * V \qquad // \ parentheses \ not \ required
```

4.2.2 Membership and Null Tests

A membership test is used to determine whether a value can be converted to a type, satisfies the value-constraints of a type, or is in a particular interval or set. A null test is used to determine whether a value is the null value. The result of a membership test or null test is of type Boolean.

4.2.3 Other ParaSail Operators

```
"from_univ"
            -- invoked implicitly to convert from a value of a universal type
             -- invoked using "[[ expression ]]" to convert to a universal type
"to_univ"
             -- and used implicitly to convert to a universal type for operations
             -- that take universal-type parameters
             -- invoked using "type_name ( expression )" to convert between types
"convert"
"indexing"
             -- invoked by "object [ operation_actuals ]" to index into a container
"slicing"
             -- invoked by "object [ operation_actuals ]" to select a slice of a container
"index_set"
            -- invoked by an iterator to iterate over the elements of a container
"[]"
             -- invoked by "[]" to create an empty container; invoked implicitly
                by "[ key1 => value1, key2 => value2, ... ]" followed by multiple calls
                on "\mid=" to build up a container given the key/value pairs
"[..]"
             -- invoked by "[..]" to create a universal set;
                invoked implicitly to turn a type name into the set of its values
"()"
             -- invoked by "( operation_actuals )" to create an object from components
```

Examples:

4.2.4 Aggregates

Aggregates are used for constructing values out of their constituents. There are two kinds of aggregates: the class_aggregate for creating an object of a type from its named components, and the container_aggregate, for creating an object of a container type (see 8.2) from a sequence of elements, optionally associated with one or more keys.

The class_aggregate is generally only available when inside the class defining a module, or for a type based on a module that has only components declared in its interface. In addition, if the "()" operator is explicitly declared in the interface of a module, then the class_aggregate may be used.

Aggregates have the following form:

```
aggregate ::= class_aggregate | container_aggregate

class_aggregate ::= '(' class_components ')'

class_components ::= class_component { ',' class_component }

class_component ::=
   [id '=>'] expression
   |id '<==' object_name</pre>
```

See 8.2 Container Aggregates for the syntax of a container aggregate.

In a class_aggregate, named components (class_component with an id specified) must follow any positional components (those without an id specified). If the '<==' move operation is specified, then the value of the component is moved from the named existing object, leaving it null. The named existing object must be a variable, with an 'optional' type.

Examples:

```
(X \Rightarrow 3.5 \,,\, Y \Rightarrow 6.2) \qquad /\!/ \; \textit{fully named class\_aggregate} (Element \,,\, Next \Rightarrow \textbf{null}) \;\; /\!/ \; \textit{mixed positional and named class\_aggregate} List := (Item <= Element \,,\, Next <= List \,); \\ /\!/ \; \textit{move Element to front of linked list}
```

4.2.5 Quantified Expressions

Quantified expressions are used to specify a boolean condition that depends on the properties of a set of values.

A quantified expression has the form:

```
quantified_expression ::=
   '(' 'for' all_or_some quantified_iterator '=>' condition ')'
all_or_some ::= 'all' | 'some'

quantified_iterator ::=
   set_iterator | element_iterator | initial_next_while_iterator
```

See Loop Statements (section 5.6) for the syntax of the various iterator forms.

A quantified_expression with the reserved word 'all' is true if and only if the condition evaluates to true for all of the elements of the sequence produced by the quantified_iterator. A quantified_expression with the reserved word 'some' is true if and only if the condition evaluates to true for at least one of the elements of the sequence produced by the quantified_iterator. It is not specified in what order the evaluations of the condition are performed, nor whether they are evaluated in parallel. The condition might not be evaluated for a given element of the sequence if the value for some other element already determines the final result.

Examples:

```
N_Is_Composite := (for some X in 2..N/2 \Rightarrow N rem X == 0);

Y_Is_Max := (for all I in Bounds(A) \Rightarrow A[I] <= Y);
```

4.2.6 Conditional Expressions

Conditional expressions are used to specify a value by conditionally selecting one expression to evaluate among several.

Conditional expressions are of one of the following forms:

```
conditional_expression ::= if_expression | case_expression
```

An if_expression has one of two alternative syntaxes:

```
if_expression ::=
    condition '?' expression ':' expression
    | '(' 'if' condition 'then' expression else_part_expression ')'
else_part_expression ::=
    { 'elsif' condition 'then' expression } 'else' expression
```

All expressions of an if-expression must be null or implicitly convertible to the same type.

To evaluate an if_expression, the conditions are evaluated in sequence, and the first one that evaluates to true determines the expression to be evaluated (the one following the '?' or corresponding 'then'). If all of the conditions evaluate to false, the last expression of the if_statement is evaluated to produce the value of the if_expression.

Examples:

```
Bigger := (if X > Y then X else Y);

return Y == 0? null : X/Y;  // return null if would divide by zero
Case expressions have the following form:

case_expression ::=
    '(' 'case' case_selector 'of'
        case_expression_alternative { ';'
        case_expression_alternative } [ ';'
        case_expression_default ]
    ')'

case_expression_alternative ::=
    '[' choice_list ']' '=>' expression
    | '[' identifier ':' type_name ']' '=>' expression

case_expression_default ::=
    '[..]' '=>' expression
```

See Case Statements (section 5.4) for the syntax of case_selector and choice_list.

All expressions following '=>' of a case_expression must be null or implicitly convertible to the same type.

The choice_list or type_name of each case_expression_alternative determines a set of values. If there is not a case_expression_default, then the sets associated with the case_expression_alternatives must cover all possible values of the case_selector. The sets associated with the case_expression_alternatives must be disjoint with one another.

To evaluate a case_expression, the case_selector is evaluated. If the value of the case_selector is in a set associated with a given case_expression_alternative, the corresponding expression is evaluated. If the value is not a member of any set, then the expression of the case_expression_default is evaluated.

If a case_expression_alternative includes an identifier and a type_name, then within the expression, the identifier has the given type, with its value given by a conversion of the case_selector to the given type.

Example:

```
return (case Key =? Node.Key of
  [#less] => Search(Node.Left, Key);
  [#equal] => Node.Value;
  [#greater] => Search(Node.Right, Key));
```

4.2.7 Map-Reduce Expressions

Map-reduce expressions are used to specify a value that is produced by combining a set of values, given an initial value and an operation to be performed with each value.

A map-reduce expression has the form:

See Loop Statements (section 5.6) for the syntax of the various iterator forms.

An expression_with_initial_value must have exactly one initial_value_specification within it (not including the contents of any nested map_reduce_expressions). The expression of the initial_value_specification must not refer to the loop variable of the iterator.

For the evaluation of a map_reduce_expression, first the expession of the initial_value_specification is evaluated and it becomes the *initial* result of the map_reduce_expression. Then for each element of the sequence of values produced by the map_reduce_iterator that satisfies the value_filter, if any, the expression_with_initial_value is evaluated, with the initial_value_specification taking on the value of the *current* result of the map_reduce_expression, and the result of the evaluation becoming the *next* result of the map_reduce_expression. After all of the elements of the sequence produced by the iterator have been combined, the last such evaluation determines the *final* result. If there are no elements in the sequence, then the *initial* result is used.

Examples:

```
\begin{aligned} & \text{Sum\_Of\_Squares} \ := \ (\textbf{for} \ X \ \textbf{in} \ 1..N \implies <0> + X**2); \\ & \text{Largest\_In\_Absolute\_Value} \ := \\ & (\textbf{for} \ \textbf{each} \ E \ \textbf{of} \ Arr \implies \text{Max} \ (<\textbf{null}>, \ abs \ E)); \end{aligned}
```

Note that the language-provided Max operations, when given a null operand, will return the other operand. The same applies to the Min operations.

4.2.8 Type Conversion

A type conversion can be used to convert an expression from one type to another, by using a syntax like that of an operation call but with the operation identified by the name of the target type:

```
type_conversion ::= type_name '(' expression ')'
```

The expression of a type_conversion must be *convertible* to the target type. An expression of a type A is *convertible* to a type B if the type A is *convertible* to type B and the value of the expression after conversion satisfies any value-constraints on B.

Type A is *convertible* to type B if and only if:

- Types A and B are instances of the same module with value-equivalent (see 3.1) actuals (even if one of them is a 'new' type);
- Type B is a polymorphic type (see 7.2.1), and type A is an instance of a module that extends or implements the root interface of B, with value-equivalent actuals;
- Type A is a polymorphic type, and the type-id of the expression identifies a type that is convertible to B;
- Type A has a "to_univ" operator and type B has a "from_univ" operator such that the result type of the "to_univ" operator is the input type of the "from_univ" operator;
- Type A or type B has a "convert" operator that has an input type that matches type A and a result type that matches type B.

Statements

Statements specify an action to be performed as part of a sequence of statements. A ParaSail statement can either be a simple statement, a compound statement containing other statements as constituents, or a local declaration:

```
statement ::= simple_statement | [ label ] compound_statement | local_declaration

simple_statement ::= assignment_statement
| exit_statement | continue_statement
| return_statement | operation_call

label ::= '*' statement_identifier '*'

statement_identifier ::= identifier

compound_statement ::= if_statement | case_statement | loop_statement | block_statement

local_declaration ::= object_declaration | operation_declaration | operation_definition
```

If and only if a compound_statement is preceded by a label, then the statement_identifier must appear again at the end of the compound_statement.

If a compound_statement completes normally, as opposed to ending via an exit_statement, continue_statement, or return_statement, then the with_values clause, if any, at the end of the compound_statement is executed.

```
with_values ::=
   'with' identifier '=>' expression
| 'with' '(' identifier '=>' expression { ',' identifier '=>' expression } ')'
```

5.1 Statement Separators

Statements are separated with ';', '||', or 'then'. The delimiter ';' may also be used as a statement terminator.

```
statement_list ::=
```

The scope of a local_declaration occurring immediately within a statement_sequence goes from the declaration to the end of the immediately enclosing statement_list. The scope of a local declaration occurring immediately within a statement_thread goes from the declaration to the end of the statement_thread.

For the execution of a statement_list, each statement_group is executed to completion in sequence. For the execution of a statement_sequence or a statement_thread, expressions are evaluated and assignments and calls are performed in an order consistent with the order of references to sequential objects (see chapter 10) occurring in the statements. For the execution of a statement_thread_group, each statement_thread is executed concurrently with other statement_threads of the same group.

Examples:

```
A := C(B); D := F(E) \mid | U := G(V); W := H(X);
```

The first two statements run as one thread, the latter two run as a separate thread.

```
\begin{array}{ll} \textbf{block} & \textbf{var} \ A : \ Vector < Integer > := \ [X, \ Y]; \\ \textbf{then} & \operatorname{Process}\left(A[1]\right); \\ || & \operatorname{Process}\left(A[2]\right); \\ \textbf{end} \ \ \textbf{block}: \end{array}
```

The declaration of A is completed before beginning the two separate threads invoking Process on the two elements of A.

5.2 Assignment Statements

An assignment_statement allows for replacing the value of one or more objects with new values.

```
assignment_statement ::=
   object_name ':=' expression
| object_name '<==' object_name
| object_name '<=>' object_name
| class_aggregate ':=' expression
| object_name operate_and_assign expression
```

There are builtin operations for simple assignment, for moving an object to a new location leaving a null behind, and for swapping the content of two objects:

```
":=" -- simple assignment of right-hand-side into left-hand-side
"<==" -- move contents of right-hand-side to left-hand-side, leaving
```

```
the right hand side "null"
"<=>" -- swap left and right hand content
```

Multiple objects may be assigned in a single assignment by using a class_aggregate as the left hand side of an assignment.

In addition to the built-in assignment, move, and swap operations, several of the binary operators may be combined with "=" to produce operate-and-assign operations:

```
operate_and_assign ::=
    '+=' | '-=' | '*=' | '/=' | '**=' | '<<=' | '>>='
    | 'and=' | 'or=' | 'xor=' | '|=' | '<|='
```

The last operator '<|=' combines the right hand side into the left hand side, and then sets the right hand side to null. This is analogous to the move ('<==') operation defined above, except that the left hand side is presumed to be a container into which the right hand side is combined.

Examples:

5.3 If Statements

If statements provide conditional execution based on the value of a boolean expression.

If statements are of the form:

```
if_statement ::=
    'if' condition 'then'
        statement_list
    [ else_part ]
    'end if' [ statement_identifier ] [ with_values ]

else_part ::=
    'elsif' condition 'then'
        statement_list
    [ else_part ]
    | 'else'
        statement_list

condition ::= expression -- must be of a boolean type
```

For the execution of an if_statement, the condition is evaluated and if true, then the statement_list of the if_statement is executed. Otherwise, the else_part, if any, is executed.

For the execution of an else_part, if the else_part begins with 'elsif', then the condition is evaluated and if true, the statement_list following 'then' is executed. Otherwise, the nested else_part, if any, is executed. If the else_part begins with 'else', then the statement_list following the 'else' is executed.

Example:

```
if This_Were(A_Real_Emergency) then
   You_Would(Be_Instructed, Appropriately);
elsif This_Is(Only_A_Test) then
   Not_To_Worry();
end if;
```

5.4 Case Statements

Case statements allow for the selection of one of multiple statement lists based on the value of an expression. Case statements are of the form:

```
case_statement ::=
    'case' case_selector 'of'
        case_alternative
    { case_alternative }
        [ case_default ]
    'end' 'case' [ statement_identifier ] [ with_values ]

case_selector ::= expression

case_alternative ::=
        '[' choice_list ']' '=>' statement_list
        | '[' identifier ':' type_name ']' '=>' statement_list

choice_list ::= choice { '|' choice }

choice ::= expression [ interval_operator expression ]

interval_operator ::= '..' | '..<' | '<...' | '<...<'

case_default ::=
        '[..]' '=>' statement_list
```

The choice_list or type_name of each case_alternative determines a set of values. If there is not a case_default, then the sets associated with the case_alternatives must cover all possible values of the case_selector. The sets associated with the case_alternatives must be disjoint with one another.

For the execution of a case_statement, the case_selector is evaluated. If the value of the case_selector is in a set associated with a given case_alternative, the corresponding statement_list is executed. If the value is not a member of any set, then the statement_list of the case_default is executed.

If a case_alternative includes an identifier and a type_name, then within the statement_list, the identifier has the given type, with its value given by a conversion of the case_selector to the given type.

Example:

```
Handle_Others(Input);
end case:
```

5.5 Block Statements

A block statement allows the grouping of a set of statements with local declarations and an optional set of assignments to perform if it completes normally.

A block statement has the following form:

```
block_statement ::=
  'block'
    statement_list
  'end' 'block' [ statement_identifier ] [ with_values ]
```

For the execution of a block_statement, the statement_list is executed. If the statement_list completes without being left due to an exit or return statement, the with_values clause at the end of the block, if any, is executed.

5.6 Loop Statements

A loop statement allows for the iteration of a statement_list over a sequence of objects or values. Loop statements have the following form:

```
loop_statement ::=
  while_until_loop | for_loop | indefinite_loop
while_until_loop ::= while_or_until condition loop_body
while_or_until ::= 'while' | 'until'
```

For the execution of a while_until_loop the condition is evaluated. If the condition is satisfied, meaning it evaluates to true when 'while' is specified or evaluates to false when 'until' is specified, then the statement_list of the loop_body is executed, and if the statement_list reaches its end, the process repeats. If the condition is not satisfied, then the current iteration completes without executing the statement_list. If this is the last iteration active within the loop, the while_until_loop is completed, and the with_values clause at the end of the loop_body, if any, is executed.

```
indefinite_loop ::= loop_body
```

An indefinite_loop is equivalent to a while_until_loop that begins with 'while' and has an expression of #true.

```
for_loop ::=
    'for' iterator [ value_filter ] [ direction ] loop_body
    | 'for' '(' iterator_list ')' [ value_filter ] [ direction ] loop_body
value_filter ::= annotation
direction ::= 'forward' | 'reverse' | 'concurrent'
loop_body ::=
    'loop'
        statement_list
```

```
'end' 'loop' [ statement_identifier ] [ with_values ]
iterator_list ::=
    iterator [ direction ] { ';' iterator [ direction ] }
iterator ::=
    set iterator
  | 'each' element_iterator
  | value_iterator
set_iterator ::=
  identifier [ ':' type_name ] 'in' expression
value_iterator ::=
    initial_value_iterator
  | initial_next_while_iterator
initial_value_iterator ::=
    loop_variable_initializer [ while_or_until_condition]
initial_next_while_iterator ::=
    loop_variable_initializer next_values [ while_or_until condition ]
loop_variable_initializer ::=
    identifier [ ':' type_name ] ':=' expression
  | identifier '=>' object_name
next_values ::= 'then' expression { '||' expression }
```

See 8.3 for the syntax of an element_iterator. See Chapter 9 for the syntax of an annotation.

A direction of 'forward' or 'reverse' is permitted only when at least one of the iterators of the for_statement is a set_iterator or an element_iterator. The direction determines the order of the sequence of values produced by such iterators. In the absence of a 'forward' or 'reverse' direction, such iterators may generate their sequence of values in any order.

The identifier of an iterator declares a *loop variable* which is bound to a particular object or value for each execution of the statement_list of the loop_body.

Each kind of iterator produces a sequence of values (or objects). If a value_filter is present, the sequence is reduced to those values (or objects) that satisfy the value_filter annotation (see Chapter 9 for examples of annotations).

The values in the sequence produced by a set_iterator are all of the values of the set, less those that do not satisfy the value_filter, if any. The values in the sequence produced by a value_iterator are given explicitly by the initial value (or initial object when '=>' is used), and the next values, either specified in the initial_next_while_iterator itself after then, or in continue statements within the body of the loop, as long as the while_or_until_condition is satisfied. Again, if there is a value_filter, the values that do not satisfy the value_filter are skipped. See section 8.3 for a description of the sequence of objects, or key-value pairs, produced by an element_iterator.

If the expression of a set_iterator is a type_name, it is equivalent to invoking the "[..]" operator defined for that type, to produce the set of all values of the type (see section 4.2.3).

For the execution of a for_loop with a single iterator, the statement_list of the loop_body is executed once for each element in the sequence of values produced by the iterator (along with values specified by continue_statements that apply to the for_loop and have a with_values clause – see 5.6.1). For each

execution of the statement_list, the loop variable is bound to the corresponding element of the sequence (or the value specified by the continue statement – see 5.6.1).

For the execution of a for_loop with multiple iterators, the statement_list of the loop_body is executed once for each set of elements determined by the set of iterators (and any applicable continue_statements having a with_values clause), with the iterator that produces the shortest sequence limiting the number of executions of the statement_list. That is, the for_loop terminates as soon as any one of the iterators has exhausted its sequence. If there is a value_filter, then the loop_body is skipped for any set of elements that does not satisfy the filter.

After a for_loop terminates normally, that is, without being exited by an exit or return statement, the with_values clause, if any, is executed.

Examples:

```
 \begin{array}{lll} \textbf{for} & I & \textbf{in} & 1..10 & \textbf{concurrent loop} \\ & & X[\:I\:] \: := \: I & ** & 2\:; \\ \textbf{end loop}\:; \end{array}
```

The above loop initializes a table of squares in parallel.

```
 \begin{array}{lll} \textbf{for each } S & \textbf{of } List\_Of\_Students(Classroom) & \{\mathit{Is\_Undergraduate}(S)\} & \textbf{forward loop} \\ & Print(Report \, , \, Name(S)); \\ \textbf{end loop} \, ; \end{array}
```

The above loop prints the names of the undergraduate students (i.e. those satisfying the Is_Undergraduate filter) in the order returned by the List_Of_Students function for the given Classroom.

```
for X \Rightarrow Root then X.Left \mid \mid X.Right while X not null loop Process(X.Data); end loop;
```

The above loop calls Process on the Data component of the Root, and then initiates two new iterations concurrently, one on the Left subtree of X and one on the Right subtree. An iteration is not performed for cases where X is null. The loop as a whole terminates when Process has been called on the Data component of each element of the binary tree.

5.6.1 Continue Statements

A continue statement may appear within a loop, and causes a new iteration of the loop to begin, optionally with new binding(s) for the loop variable(s).

A continue statement has the following form:

```
continue_statement ::= 'continue' 'loop' [ statement_identifier ] [ with_values ]
```

For the execution of a continue_statement, the current thread completes the current iteration of the immediately enclosing loop, and begins a new iteration of the specified loop (or in the absence of a statement_identifier, the immediately enclosing loop). If the identified loop is a for_loop without a specified sequence or next value, then there must be a with_values clause, which determines the new binding(s) for the loop variable(s).

Example:

```
\begin{array}{lll} \textbf{for} & X \Longrightarrow \operatorname{Root} \ \textbf{while} \ X \ \textbf{not} \ \textbf{null} \ \textbf{loop} \\ & \operatorname{Process}\left(X,\operatorname{Data}\right); \\ & || \ \ \textbf{continue} \ \ \textbf{loop} \ \ \textbf{with} \ X \Longrightarrow X. \ \operatorname{Left}; \\ & || \ \ \textbf{continue} \ \ \textbf{loop} \ \ \textbf{with} \ X \Longrightarrow X. \ \operatorname{Right}; \\ \textbf{end} \ \ \textbf{loop}; \end{array}
```

The above loop walks a binary tree in parallel, with the continue statements used to initiate additional iterations of the loop body to process the Left and Right subtrees of X. This is equivalent to the example given in 5.5, except that the subtrees of X are walked concurrently with calling Process on X.Data. (The

example given in 5.5 could be made exactly equivalent by making that loop into a concurrent loop, which means that while performing the statement_list of one iteration we proceed onto the next values.)

Note that the loop_statement whose iteration is terminated by a continue_statement may be nested within the loop_statement identified by the statement_identifier, and this outer loop_statement is the one that begins a new iteration.

Example:

```
var Solutions : Concurrent_Vector<Solution> := [];
*Outer_Loop*
 for (C : Column := 1; Trial : Solution := Empty()) loop
     for R in Row concurrent loop // Iterate over the rows
         if Acceptable (Trial, R, C) then
             // Found a Row/Column location that is acceptable
             if C < N then
                  // Keep going since haven't reached Nth column.
                 continue loop Outer\_Loop with (C \Rightarrow C+1,
                    Trial => Incorporate (Trial, R, C));
             else
                  // All done, remember trial result that works
                  Solutions |= Incorporate (Trial, R, C);
             end if;
         end if;
     end loop;
end loop Outer_Loop;
```

If an inner loop_statement has multiple iterations active concurrently, a continue_statement terminates only one of them. The other active iterations proceed independently. The inner loop_statement as a whole only completes when all of the active iterations within the loop are complete. If all of the iterations of the inner loop_statement end with a continue_statement to an outer loop_statement, then the thread that initiated the inner loop_statement is terminated. If at least one of the iterations of the inner loop_statement executes the with_values clause, if any, and proceeds with the statements following the inner loop_statement.

In this example, the above doubly nested loop iterates over the columns of a chessboard, and for each column iterates in parallel over the rows of the chessboard, trying to find a place to add a piece that satisfies the Acceptable function. When a place is found at a given row on the current column, the continue statement proceeds to the next column with the given Trial solution. Meanwhile, other rows are being checked, which may also result in additional continuations to subsequent columns. If a given row is not acceptable in a given column for the current Trial, it is ignored and the thread associated with that row completes rather than being used to begin another iteration of the outer loop.

5.7 Exit statements

An exit statement may be used to exit a compound statement while terminating any other threads active within the compound statement.

An exit statement has the following form:

```
exit_statement ::=
  'exit' compound_kind [ statement_identifier ] [ with_values ]
compound_kind ::= 'if' | 'case' | 'block' | 'loop'
```

An exit statement exits the specified compound_statement (or in the absence of a statement_identifier, the immediately enclosing compound_statement of the specified compound_kind), terminating any other threads

active within the identified statement. If the exit_statement has a with_values clause, then after terminating all other threads active within the compound statement, the assignments specified by the with_values clause are executed.

Example:

```
const Result : Result_Type;
block
   const Result1 := Compute_One_Way(X);
   exit block with Result => Result1;
   ||
   const Result2 := Compute_Other_Way(X);
   exit block with Result => Result2;
end block;
```

The above block performs the same computation two different ways, and then exits the block with the Result object assigned to whichever answer is computed first.

Operations

Operations are used to specify an algorithm for computing a value or performing a sequence of actions. There are two kinds of operations – functions (funcs) and operators (ops). Operators have special meaning to the language, and are invoked using special syntax. Functions are invoked using a name followed by inputs in parentheses, and may produce one or more outputs. Operations may update one or more of their variable inputs.

6.1 Operation Declarations

Operations are declared using the following forms:

```
operation_declaration ::=
  function_declaration | operator_declaration
function_declaration ::=
  [ 'abstract' | 'optional' ] [ 'queued' ] 'func' identifier inputs
     [ '->' outputs ]
operator_declaration ::=
  [ 'abstract' | 'optional' ] [ 'queued' ] 'op' operator_symbol inputs
     [ '->' outputs ]
operator_symbol ::= string_literal
inputs ::= input | '(' [ input { ';' input } ] ')'
input ::= formal_object | formal_operation | '<' formal_object '>'
formal_object ::=
  [ input_mode ] [ identifier ':' ] formal_object_type [ ':=' expression ]
identifier_list ::= identifier { ',' identifier }
input_mode ::=
    'var'
  | 'ref' [ var_or_const ]
  | 'global' [ 'var' ]
```

If an identifier is omitted for an input, the type_name may be used within the operation to identify the parameter if it is unique. Otherwise, the parameter is unnamed at the call point. In an operation_definition (see 6.2) all inputs must either have an identifier, or have a unique type name.

If an identifier is omitted for an output of a function, and there is only one output, the function identifier may be used to identify the output. If there is more than one output, each one must have an identifier.

If a formal_object_type is of the form identifier 'is' module_instantiation, the actual parameter may be of any type that matches the module_instantiation (see 7.4). The specified identifier refers to the type of the actual parameter within the operation_declaration, and within the corresponding operation_definition. If a formal_object is bracketed by '<' '>' then this input may be used as part of a parameter to such an instantiation within the same operation_declaration. See below for examples (operators "*" and "**").

If there is no input_mode, or if 'var' does not appear in the input_mode, then the formal is read-only within the body of the operation. If the input_mode is 'ref' without being followed by 'var' or 'const', then within the operation the formal is read-only; however, for any output that is also of mode simply 'ref', the output is (in the caller) a variable reference to the returned object if and only if all of the inputs with mode merely 'ref' are variables in the caller. If any of the inputs with mode 'ref' are constants, then all of the outputs with mode 'ref' are constants.

An output of mode 'ref' must be specified via a return statement as a reference to all or part of an input of mode 'ref'. An output of mode 'ref' 'var' must be specified via a return statement as a reference to all or part of an input of mode 'ref' 'var'. An output of mode 'ref' 'const' must be specified via a return statement as a reference to all or part of some 'ref' input ('var', 'const', or merely 'ref').

The designator of a formal_operation may not be the same as that of an already defined operation with the same number of inputs and outputs, unless its parameter types are significantly different from the preexisting operation.

See section 10.1.1 for the meaning of 'queued' when applied to an operation as a whole.

See section 7.2 for the meaning of 'abstract' and 'optional' when applied to an operation.

Examples:

```
func Sin (X : Float) -> Float;

op "=?" (Left, Right : Set) -> Ordering;

func Divide ( Dividend : Integer; Divisor : Integer)
   -> (Quotient : Integer; Remainder : Integer);
```

6.2 Operation Definitions

An operation may be defined with a body, with an operation import, or by equivalence to an existing operation.

An operation definition has the following form:

```
operation_definition ::=
    function_definition
  | operator_definition
  | operation_import
  | operation_equivalence
function_definition ::=
  function_declaration 'is'
    operation_body
  'end' 'func' identifier
operator_definition ::=
  operator_declaration 'is'
   operation_body
  'end' 'op' operator_symbol
operation_body ::= [ dequeue_condition ] statement_list
operation_import ::=
  operation_declaration 'is' 'import' '(' operation_actuals ')'
operation_equivalence ::=
    operation_declaration 'is' operation_name
  | operation_declaration 'is' [operation_designator] 'in' type_specifier
```

If an operation is declared with a separate, stand-alone operation_declaration, then the operation_declaration in the operation_definition must fully conform to it. If any annotations appear prior to the 'is' of the operation_definition, then they must fully conform to the annotations on the separate operation_declaration. Similarly, if any comments appear prior to the 'is' of the operation_definition, then they must fully conform to comments on the separate operation_declaration.

An operation_import indicates that the operation is defined externally to the current program, possibly in a different language. The operation_actuals indicate the external name and/or other properites of the externally defined operation.

An operation_equivalence indicates that the operation is merely a renaming of some existing operation, identified by the operation_name, or by a type and optional operation_designator. In this latter form, the existing operation must be declared in the specified type's module, with the same designator as the new operation, or with the given operation_designator if specified. The existing operation must have the same number of inputs and outputs, of the same modes and with the same types.

Examples:

```
func Sin(X : Float) -> Float is import("sinf");
  // defined externally
op "+=" (var Left : Set; Right : Element) is " |=";
  // defined by equivalence
op "in"(Left : Float; Right : Ordered_Set<Float>)
  is in Ordered_Set<Float>; // defined by equivalence
func Update(var Obj : T; New_Info : Info_Type) is
    Obj. Info := New_Info;
end func Update;
func Fib (N : Integer) -> Integer is
   // Recursive fibonacci but with linear time
   func Fib_Helper(M : Integer)
     -> (Prev_Result : Integer; Result : Integer) is
     // Recursive "helper" routine which
     // returns the pair ( Fib (M-1), Fib (M) )
       if M \le 1 then
           // Simple case
           return (Prev_Result => M-1, Result => M);
       else
           // Recursive case
           const Prior_Pair := Fib_Helper(M-1);
           // Compute next fibonacci pair in terms of prior pair
           return with
             (Prev_Result => Prior_Pair.Result,
              Result => Prior_Pair.Prev_Result + Prior_Pair.Result);
       end if;
  end func Fib_Helper;
   // Just pass the buck to the recursive helper function
   return Fib_Helper(N). Result;
end func Fib;
```

6.3 Operation Calls

Operation calls are used to invoke an operation, with inputs and/or outputs. Operation calls are of the form:

```
operation_call ::= operation_name '(' operation_actuals ')'
```

```
operation_name ::=
    [ type_identifier '::' ] operation_designator
    | object_name '.' operation_designator

operation_designator ::= operator_symbol | identifier

operation_actuals ::= [ operation_actual { ',' operation_actual } ]

operation_actual ::=
    [ identifier '=>' ] actual_object
    | [ identifier '=>' ] actual_operation

actual_object ::= expression

actual_operation ::= operation_specification | 'null'
```

Unlike other names, an operation_name need not identify an operation that is directly visible. Operations declared within modules other than the current module are automatically considered, depending on the form of the operation_name:

- If the operation_name is of the form type_identifier '::' operation_designator then only operations with the given designator declared within the module associated with the named type are considered.
- If the operation_name is of the form object_name '.' operation_designator then the call is equivalent to

```
type_of_object_name '::' operation_designator
    '(' object_name ',' operation_actuals ')'
```

• Otherwise (the operation_name is a simple operation_designator), all operations with the given designator declared in the modules associated with the types of the operation inputs and outputs, if any, are considered, along with locally declared operations with the given designator.

Any named operation_actuals, that is, those starting with identifier '=>', must follow any positional operation_actuals, that is, those without identifier '=>'.

For the execution of an operation call, the operation_actuals are evaluated (in parallel – see 10.2), as are any default expressions associated with non-global operation inputs for which no actual is provided. For 'global' inputs, a global concurrent object with the given identifier must be visible both to the caller and the called operation, and if it is a 'var' input, the caller must also have it as a 'global' 'var' input. After parallel evaluation of the operation_actuals, the body of the operation is executed, and then any outputs are available for use in the enclosing expression or statement.

If the type of one or more of the operation actuals is polymorphic (see 7.2.1), and the operation is declared in the module that is associated with the root type of the polymorphic type, then the actual body invoked depends on the run-time type-id of the actual if the corresponding formal parameter is *not* polymorphic. If multiple operation actuals have this same polymorphic type (and their corresponding formals are also *not* polymorphic), then their run-time type-ids must all be the same.

Examples:

```
Result := Fib (N \Rightarrow 3);
```

```
Graph.Display_Point(X, Y => Sin(X));
var A := Sparse_Array::Create(Bounds => 1..N);
```

6.3.1 Lambda expressions

A lambda expression is used for defining an operation as part of passing it as an actual parameter to a module_instantiation or an operation call.

A lambda expression has the following form:

```
lambda_expression ::=
    'lambda' inputs [ '->' outputs ] 'is' lambda_body
lambda_body ::= expression | '(' expression { ';' expression } ')'
Example:
    Graph_Function(Window, lambda (X : Float) -> Float is sin(X)**2);
```

6.4 Return Statements

A return statement is used to exit the nearest enclosing operation, optionally specifying one or more outputs. A return statement has the following form:

```
return_statement ::=
    'return'
| 'return' expression
| 'return' with_values
```

If there is no output value specified, any outputs of the immediately enclosing operation must have already been assigned prior to the return statement. If there is only a single expression, the immediately enclosing operation must have only a single output.

Examples:

```
return Fib(N-1) + Fib(N-2);
return with (Quotient \Rightarrow Q, Remainder \Rightarrow R);
```

Modules

Modules define a logically related group of types, operations, data, and, possibly, nested modules. Modules may be parameterized by types, operations, or values.

Every module has an interface that declares its external characteristics. If the interface of a module declares any non-abstract operations, the module must have a class that defines its internal representation and algorithms.

7.1 Interface Declaration for a Module

The interface of a module is declared using the following syntax:

```
interface_declaration ::=
  ['abstract'] ['concurrent'] 'interface' module_identifier
    '<' module_formals '>'
    [ module_ancestry ]
  'is'
     { interface_item }
  [ 'new'
     { interface_item } ]
  { 'implements' restricted_interface_item_list }
  'end' 'interface' module_identifier ';'
module_identifier ::= identifier { '::' identifier }
interface_item ::=
    type_declaration
  | operation_declaration
  | operation_import
  | operation_equivalence
  | object_declaration
  | interface_declaration
```

Module formal parameters have the following form:

```
module_formals ::= [ module_formal { ';' module_formal } ]
```

```
module_formal ::= formal_type | formal_operation | formal_object

formal_type ::= [ identifier 'is' ] interface_name '<' module_actuals '>'
```

See section 7.2 below for the syntax of module_ancestry and restricted_interface_item_list, and for an explanation of the use of 'new' to separate overriding from non-overriding operations.

Example (also used in section 3.1):

```
interface List <Element_Type is Assignable <>> is
    func Create() -> List;
func Is_Empty(L : List) -> Boolean;
func Append(var L : List; Elem : Element_Type);
func Remove_First(var L : List) -> optional Element_Type;
func Nth_Element(ref L : List; N : Univ_Integer) -> ref optional Element;
end interface List;
```

This defines the interface to a List module, which provides operations for creating a list, checking whether it is empty, appending to a list, removing the first element of the list, and getting a reference to the Nth element of the list.

7.2 Module Inheritance and Extension

A module may be defined as an *extension* of an existing module, and may be defined to *implement* the interface of one or more other modules.

```
module_ancestry ::=
   ['extends' [ identifier ':' ] module_name [ '<' module_actuals '>' ] ]
   ['implements' module_list ]

module_name ::= module_identifier

module_list ::=
   module_name '<' module_actuals '>'
        { ',' module_name '<' module_actuals '>' }
```

If a module M2 extends a module M1, but does not specify the module_actuals for M1, then M2 inherits all of the module formals of M1. Otherwise, module M2 must have its own set of formals, which may then be used to instantiate M1.

When extending M1, the instance of module M1 defined by the specified module_actuals, or by substituting the corresponding formals of M2 into M1, is called the *underlying type* for M2. A module has an *underlying type* only if it is defined to extend some other module. If a module M2 has an underlying type, then there is an *underlying* component of each object of any type produced by instantiating the module M2. This underlying component is of the underlying type, and is by default named by the identifier of the module being extended (e.g. M1), but may be given its own identifier by specifying it immediately after 'extends'.

In addition to possibly inheriting module formals, if a module M2 extends a module M1, it also inherits operations from the interface of M1. As part of inheriting an operation from M1, the types of the non-polymorphic (see 7.2.1) inputs and outputs of the operation are altered by replacing each occurrence of the original module name M1 with the new module name M2, and by substituting in the module parameter names of M2 for the corresponding module parameter names of M1. For example, an operation such as func Invert(X : M1) -> M1 becomes func Invert(X : M2) -> M2.

An operation inherited from M1 is *abstract* only if the corresponding operation in M1 is abstract, or if the operation has an output which is of a type based on M1 (as is **Invert** in the above example). If the

operation inherited from M1 is *not* abstract, then its implicit body is defined to call the operation of M1, with any input to this operation that is of the underlying type being passed the underlying component of the corresponding input to the inherited operation.

If an operation in M1 has no non-polymorphic inputs or outputs based on M1, but its first input is polymorphic, then as part of inheriting the operation, this first input has its type changed from being based on M1 to being based on M2. The types of other inputs or outputs are unaffected. So for example, an operation like func Union(Left, Right: M1+) -> M1+ becomes func Union(Left: M2+, Right: M1+) -> M1+. (Note that overriding such an inherited operation allows polymorphic operations to be specialized based on their first input.)

An *inherited* operation may be *overridden* by providing a declaration for the operation in the interface of the new module with the same name and number and types of inputs and outputs as the inherited operation. An *abstract* inherited operation must be overridden unless the new module is itself specified as 'abstract'. The declarations for any operations that *override* inherited operations must appear before the reserved word 'new', and the operations that do *not* override an inherited operation must appear after the 'new' (if it is present in the interface).

Finally, if M1 has *components*, then if M2 *extends* M1, it also inherits these components, with any visible components of M1 becoming visible components of M2.

If rather than extending M1, the module M2 *implements* M1 (directly or indirectly), and M2 is not itself declared as an abstract module, then M2 is required to declare in its interface a corresponding operation for each non-optional operation of module M1 that has at least one (non-polymorphic) input or output based on M1, but with the change in types of inputs and outputs from M1 to M2, as described above for inheritance. Operations in M1 that have no (non-polymorphic) inputs or outputs based on M1 need *not* be declared in M2.

If M1 has *visible* components, then it *cannot* be implemented by other modules, though it may still be extended.

```
restricted_interface_item_list ::=
  [ 'for' module_name { ',' module_name } ]
      { interface_item }
```

One or more restricted_interface_item_lists may be included at the end of an interface, each introduced by the reserved word 'implements', so as to meet the requirements for implementing some other module. These interface items are restricted in that they cannot be referenced directly. They are only available as definitions of operations required when the given interface is used in a context where some other module is expected. The interface items in a given restricted_interface_item_list may be used to implement any module, unless an explicit list of module_names is given after a 'for', in which case these additional items are only available when the interface is used to implement the specified modules.

Example:

```
func Create() -> Skip_List;
    // This overrides the abstract inherited operation
    ... // Here we may override other inherited operations
    // or introduce new operations

implements for Set
    func Add(var L : Skip_List; Elem : Skip_Elem_Type) is Append;
    // An operation required by the Set module, but which
    // is not to be directly callable on a Skip_List.
end interface Skip_List;
```

7.2.1 Polymorphic Types

If the name of a type is of the form identifier '+', it denotes a *polymorphic* type. A polymorphic type represents the identified type plus any type that extends or implements the identified type's interface, with matching module actuals. The identified type is called the *root* type for the corresponding polymorphic type.

For example, given the Skip_List interface from the example in 7.2, and the Bool_List type from section 3.1:

```
type Bool_Skip_List is Skip_List<Boolean>;
var BL : Bool_List+ := Bool_Skip_List :: Create();
```

The variable BL can now hold values of any type that is an instance of a module that implements the List interface, with Element_Type specified as Boolean. In this case it is initialized to hold an object of type Bool_Skip_List.

An object of a polymorphic type (a *polymorphic object*) includes a *type-id*, a run-time identification of the (non-polymorphic) type of the value it currently contains. The type-id of a polymorphic object may be tested with a membership test (see 4.2.2) or a case statement (see 5.4), and it controls which body is executed in certain operation calls (see 6.3). In the above example, the type-id of BL initially identifies the Bool_Skip_List type.

7.3 Class Definition for a Module

A class defines local types, operations, and data for a module, as well as a body for each operation declared in the module's interface.

A class has the following form:

```
class_definition ::=
  ['concurrent'] 'class' module_identifier
       [ '<' module_formals '>' ]
       [ module_ancestry ]
    'is'
       { local_class_item }
    'exports'
       { exported_class_item }
       { 'implements' restricted_class_item_list }
```

```
'end' 'class' module_identifier ';'

local_class_item ::=
    type_declaration
| operation_declaration
| operation_definition
| object_declaration
| interface_declaration
| class_definition

exported_class_item ::=
    operation_definition
| object_declaration
| class_definition
restricted_class_item_list ::=
    ['for' interface_name_list ] { exported_class_item }
```

An exported_class_item must correspond to an item declared in the module's interface. An exported_class_item within a restricted_class_item_list must correspond to an item declared within a corresponding restricted_interface_item_list in the module's interface.

Within an object_declaration in a class, a name may refer to any prior class_item using its simple identifier. Within a type_declaration in a class, a name within a value_constraint may refer to a local constant, but if the constant is not initialized at its declaration, the type has an *object-specific* constraint and may only be used within subsequent local (*object-specific*) type and object declarations (see the Index_Type of the Stack class in chapter 9 for an example of an *object-specific* constraint). Within other kinds of class_items, local interfaces, non-object-specific types, operations, and initialized constants may be referred to directly, but local variables and uninitialized constants are considered components of objects of a type associated with the enclosing class, and must be referred to using component_selection notation (see 4.1.1).

Example:

```
class List is
     interface List_Node   is
         var Elem : Element_Type;
         var Next : optional List_Node;
     end interface List_Node;
     var Head : optional List_Node <>;
  exports
     func Create() -> List is
        return (Head => null);
     end func Create;
     func Is_Empty(L : List) -> Boolean is
        return L. Head is null; // Must say "L. Head," not simply "Head"
     end func Is_Empty;
     func Append(var L : List; Elem : Element_Type) is
        for X => L. Head loop
           if X is null then
              // Found the end, add new component here
              X := (Elem \Rightarrow Elem, Next \Rightarrow null);
           else
              // Iterate with next node
```

```
continue loop with X \Rightarrow X.Next;
            end if:
        end loop:
     end func Append;
     func Remove_First(var L : List) -> optional Element_Type is
         if L. Head is null then
            // List is empty, nothing to return
            return null;
         else
            // Save first element and then delete node from list
            Remove_First := L. Head. Elem;
            L.Head := L.Head.Next;
            return; // Output already assigned
        end if;
     end func Remove_First;
     func Nth_Element(ref L : List; N : Univ_Integer)
       -> ref optional Element is
        for (X \Rightarrow L. Head; I := 1) loop
            if X is null then
               // reached end of list
               return null;
            elsif I = N then
               // reached Nth element
               return X. Elem;
               // continue with next node of list
               continue loop with (X \Rightarrow X. Next, I \Rightarrow I+1);
            end if;
        end loop;
     end func Nth_Element;
end class List;
```

The above class defines the module List whose interface is given in 7.1. The items preceding exports are local to the module, and are used to implement the linked list structure. The items after exports correspond to the items declared in the List interface.

TBD: Private interfaces, module extensions, module specializations

7.4 Module Instantiation

Modules are instantiated by providing actuals to correspond to the module formals. If an actual is not provided for a given formal, then the formal must have a default specified in its declaration, and that default is used.

The actual parameters used when instantiating a module to produce a type have the following form:

```
module_actuals ::= [ module_actual { ',' module_actual } ]
module_actual ::=
    [ identifier '=>' ] actual_type
    | [ identifier '=>' ] actual_operation
    | [ identifier '=>' ] actual_object
actual_type ::= object_type
```

Any module actuals with a specified identifier must follow any actuals without a specified identifier. The identifier given preceding '=>' in a module_actual must correspond to the identifier of a formal parameter of the corresponding kind.

Containers

A container is a type that defines an "indexing" operator, an "index_set" operator, a container aggregate operator "[]", a combining assignment operator "|=", and, optionally, a "slicing" operator. It will also typically define a Length or Count function, other operations for creating containers with particular capacities, for iterating over the containers, etc.

The *index type* of a container type is determined by the type of the second parameter of the "indexing" operator, and the *value type* of a container type is determined by the type of the result of the "indexing" operator.

The *index-set type* of a container type is the result type of the "index_set" operator, and must be either a set or interval over the index type.

Examples:

```
interface Map<Key_Type is Hashable<>; Element_Type is Assignable<>> is
    op "[]"() -> Map;
    op "|="(var M : Map; Key : Key_Type; Elem : Element_Type);
    op "indexing"(ref M : Map; Key : Key_Type)
        -> ref optional Element_Type;
    op "index_set"(M : Map) -> Set<Key_Type>;
end interface Map;
```

The Map interface defines a container with Key_Type as the index type and Element_Type as the value type. The interface includes a parameterless container aggregate operator "[]" which produces an empty map, a combining operator "|=" which adds a new Key => Elem pair to the map, "indexing" which returns a reference to the element of M identified by the Key (or null if none), and "index_set" which returns the set of Keys with non-null associated elements in the map.

The Set interface defines a container with the Element_Type as the value type and Univ_Integer as the index type. The interface includes a parameterless container aggregate operator "[]" which produces an empty set, a combining operator "|=" which adds a new element to the set, an "in" operator which tests whether

a given element is in the set, an "indexing" operator which returns the n-th element of the set, and an "index_set" operator which returns the interval of indices defined for the set (i.e. 1..Count(S)). The compare operator ("=?" - see 4.2.1) is provided for comparing sets for equality and subset/superset relationships.

```
interface Array<Component.Type is Assignable <>; Indexed_By is Countable <>> is
    type Bounds_Type is Interval<Indexed_By>;
    func Bounds(A : Array) -> Bounds_Type;
      (Index_Set : Bounds_Type; Values : Map<Bounds_Type, Component_Type>)
      \rightarrow Result : Array { Bounds (Result) == Index_Set} ;
    op "indexing" (ref A : Array;
      Index : Indexed_By {Index in Bounds(A)} )
      -> ref Component_Type;
    op "index_set" (A : Array)
      \rightarrow Result : Bounds_Type { Result == Bounds(A) ;
    op "slicing" (ref A : Array;
      Slice: Bounds_Type { Slice \le Bounds(A) }
      \rightarrow ref Result : Array { Bounds(Result) == Slice} ;
    op "|=" (var A : Array;
      Index : Indexed_By \{Index \ in \ Bounds(A)\};
      Value : Component_Type);
    op "|=" (var A : Array;
      Slice : Bounds_Type \{Slice \le Bounds(A)\}\ ;
      Value : Component_Type);
end interface Array;
```

The Array interface defines a container with Component_Type as the value type and Indexed_By as the index type. The index-set type is Bounds_Type. The interface includes a container aggregate operator "[]" which creates an array object with the given overall Index_Set and the given mapping of indices to values. It also defines an "indexing" operator which returns a reference to the component of A with the given Index, a "slicing" operator which returns a reference to a slice of A with the given subset of the Bounds, plus combining operators "|=" which can be used to specify a new value for a single component or all components of a slice of the array A.

8.1 Object Indexing and Slicing

Object indexing is used to invoke the "indexing" operator to obtain a reference to an element of a container object. Object slicing is used to invoke the "slicing" operator to obtain a reference to a subset of the elements of a container object.

Object indexing and slicing use the following syntax. The form with '[..]' is only for slicing.

```
object_indexing_or_slicing ::=
   object_name '[' operation_actuals ']'
   object_name '[..]'
```

If the form with '[..]' is used, or one or more of the operation_actuals are sets or intervals, then the construct is interpreted as an invocation of the "slicing" operator. Otherwise, it is interpreted as an invocation of the "indexing" operator. The object_name denotes the container object being indexed or sliced.

When interpreted as an invocation of the "slicing" operator, the construct is equivalent to:

```
"slicing" '(' object_name, operation_actuals ')'
```

```
or, for the form using '[..]':

"slicing" '(' object_name ')'
```

When interpreted as an invocation of the "indexing" operator, the construct is equivalent to:

```
"indexing" '(' object_name, operation_actuals ')'
```

The implementation of an "indexing" operator must ensure that, given two invocations of the same "indexing" operator, if the actuals differ between the two invocations, then the results refer to different elements of the container object. Similarly, the implementation of a "slicing" operator must ensure that, given two invocations of the same "slicing" operator, if at least one of the actuals share no values between the two invocations, then the results share no elements.

If an implementation of the "indexing" operator and an implementation of the "slicing" operator for the same container type have types for corresponding inputs that are the same or differ only in that the one for the "slicing" operator is an interval or set of the one for the "indexing" operator, then the two operators are said to *correspond*. Given invocations of corresponding "indexing" and "slicing" operators, the implementation of the operators must ensure that if at least one pair of corresponding inputs share no values, then the results share no elements of the container object. A slice defined using '[..]' is presumed to refer to *all* elements of the container.

Examples:

8.2 Container Aggregates

A container aggregate is used to create an object of a container type, with a specified set of elements, optionally associated with explicit indices.

```
container_aggregate ::=
    empty_container_aggregate
    | universal_container_aggregate
    | positional_container_aggregate
    | named_container_aggregate
    | iterator_container_aggregate
    | iterator_container_aggregate ::= '[]'

universal_container_aggregate ::= '[..]'

positional_container_aggregate ::= '[' positional_container_element { ', ' positional_container_element } ']'

positional_container_element ::= expression | default_container_element

default_container_element ::= '...' '=>' expression

named_container_aggregate ::= '[' named_container_element { ', ' named_container_element } ']'
```

```
named_container_element ::=
    choice_list '=>' expression
    | default_container_element

iterator_container_aggregate ::=
    '[' 'for' iterator [ value_filter ] [ ',' index_expr ] '=>' expression ']'
index_expr ::= expression
```

An empty_container_aggregate is only permitted if the container type has a parameterless container aggregate operator "[]".

A universal_container_aggregate is only permitted if the container type has a universal set operator "[..]".

The choice_list in a named_container_element must be a set of values of the index type of the container. The expression in a container_element must be of the value type of the container.

If present in a container_aggregate, a default_container_element must come last. A default_container_element is only permitted when the container_aggregate is being assigned to an existing container object, or the index-set type of the container has a universal set operator "[..]".

In an iterator_container_aggregate, the iterator must not be an initial_value_iterator, and if it is an initial_next_while_iterator, it must have a while_or_until condition.

The evaluation of a container_aggregate is defined in terms of a call on a container aggregate operator "[]" or "[..]", optionally followed by a series of calls on the combining move operation "<|=" (for positional_container_aggregates) or the "var_indexing" operator (for named_container_aggregates).

For the evaluation of an empty_container_aggregate, the parameterless container aggregate operator "[]" is called. For the evaluation of a universal_container_aggregate, the parameterless universal container aggregate operator "[..]" is called.

For the evaluation of a positional_container_aggregate or a named_container_aggregate:

- if there is a container aggregate operator "[]" which takes an index set and a mapping of index subsets to values, this is called with the index set a union of the indices defined for the aggregate, and the mapping based on the container elements specified in the container_aggregate. The default_container_element is treated as equivalent to the set of indices it represents.
- if there is only a parameterless container aggregate operator "[]" then it is called to create an empty container; the combining operator "<|=" is then called for each positional_container_element in the aggregate, while the "var_indexing" operator is called for each named_container_element, with a choice_list of more than one choice resulting in multiple calls.

If there is a default_container_element, it is equivalent to a container_element with a choice_list that covers all indices of the overall container not covered by earlier container_elements.

For the evaluation of an iterator_container_aggregate, the expression is evaluated once for each element of the sequence of values produced by the iterator, with the loop variable of the iterator bound to that element. If an explicit index_expr is present, it is provided as the index to the "var_indexing" operator. Otherwise, the loop variable is implicitly provided as the index, unless only the "<|=" operator is available, in which case no index is used. If there is a value_filter, the expression is evaluated only for elements of the sequence that satisfy the value_filter.

Examples:

Container Element Iterator 8.3

An element iterator may be used to iterate over the elements of a container.

An element iterator has the following form:

```
element_iterator ::=
    identifier [ ':' type_name ] 'of' expression
   '[' identifier '=>' identifier ']' 'of' expression
```

An element_iterator is equivalent to an iterator over the index set of the container identified by the expression. In the first form of the element_iterator, in each iteration the identifier denotes the element of the container with the given index. In the second form of the element_iterator, the first identifier has the value of the index itself, and the second identifier denotes the element at the given index in the container. The identifier denoting each element of the container is a variable if and only if the container identified by the expression is a variable.

Example:

```
for each [ Key => Value ] of Table loop
    // Iterate over key/value pairs of table
    Display (Output, Key, Value);
end loop;
```

Container Specifiers 8.4

Left <== Result;

There are various operations in ParaSail for moving rather than copying objects and components of objects, such as the "<==" and the "<|=" operations (see section 5.2). These can be used to reduce the amount of copying that is performed, which can be important when dealing with containers whose elements are themselves large objects. In some cases, we may build up a large object, with the intent of moving it into a container. In this case, there is some advantage to indicating, when the object is declared, that it is specifically intended to be moved into a particular container or other object when complete. This will cause its storage to be allocated in the same region as that of the specified container or other existing object.

The container or object whose region is to be used may be indicated when declaring an object, using a container_specifier, whose syntax is as follows:

```
container_specifier ::= 'for' object_name
Examples:
    // Compute the intersection of Left and Right
    // and put result back in Left.
    var Result : Set for Left := []; // Result in same region as Left
    for Elem in Right loop
        if Elem in Left then
            Result |= Elem;
                                       // Add Elem to intersection
        end if;
    end loop;
                                       // Move result to be new value for Left.
```

Annotations

Annotations may appear at various points within a program. Depending on their location, they can represent a precondition of an operation, a postcondition of an operation, a value constraint on a type, a value filter on an iterator, an invariant of a class, or a simple assertion at a point in a sequence of statements.

Annotations have the following form:

```
annotation ::= '{' [ label ] condition { ';' condition } '}'
```

The optional label of an annotation is for documentation purposes only. When an annotation appears as the value_filter for an iterator, any values that do not satisfy the condition(s) of the annotation are skipped. In any other context, the condition(s) of an annotation must each evaluate to true under every possible execution of the program. The ParaSail compiler will complain if some condition of an annotation might not always be true, or if it cannot be proved to be always true by the compiler.

```
postcondition_value ::= object_name '''
universal_conversion ::= '[[' expression ']]'
```

Within an annotation that is used as a postcondition, a postcondition_value (e.g. S') refers to the value of the specified object (e.g. S) after the operation is complete. The specified object must be a variable input to the operation.

An expression of the form '[[' expression ']]' may be used to convert an expression to a universal type, generally for use in an annotation. The type of the expression must have a "to_univ" operator; the type of the universal_conversion is the result type of this operator.

Examples:

```
func Sqrt(X : Float { X >= 0.0 }) \rightarrow Float { Sqrt >= 0.0 };
```

The first annotation is a precondition; the second is a postcondition.

```
type Age is new Integer < 0..200 >;
type Minor is Age { Minor < 18 };
type Senior is Age { Senior >= 50 };
```

These annotations define value constraints on two different subtypes of the Age type.

```
interface Modular< Modulus : Univ_Integer {Modulus >= 2} > is
  op "from_univ"(Univ : Univ_Integer {Univ in 0 .. < Modulus})
  -> Modular;

op "to_univ"(Val : Modular) -> Result : Univ_Integer
  { Result in 0 .. < Modulus };</pre>
```

```
op "+"(Left, Right : Modular) -> Result : Modular
    { [[Result]] == ( [[Left]] + [[Right]] ) mod Modulus };
...
end interface Modular;
```

The precondition on "from_univ" indicates the range of integer literals that may be used with a modular type with the given modulus. The postcondition on "to_univ" indicates the range of values returned on conversion back to Univ_Integer. The postcondition on "+" expresses the semantics of the Modular "+" operator in terms of the language-defined operations on Univ_Integer.

Here is a longer example:

```
interface Stack
  <Component is Assignable <>;
   Size_Type is Integer >> is
    func Max_Stack_Size(S : Stack) -> Size_Type;
    func Count(S : Stack) -> Size_Type;
    func Create (Max : Size_Type \{Max > 0\}) -> Stack
      \{Max\_Stack\_Size(Create) == Max; Count(Create) == 0\};
    func Push
      (\mathbf{var} \ S : Stack \ \{Count(S) < Max\_Stack\_Size(S)\};
       X : Component) \{ Count(S') = Count(S) + 1 \};
    func Top(ref S : Stack \{Count(S) > 0\}) \rightarrow ref Component;
    func Pop(var S : Stack \{Count(S) > 0\})
      \{Count(S') = Count(S) - 1\};
end interface Stack;
class Stack is
    const Max_Len : Size_Type;
    var Cur_Len : Size_Type { Cur_Len in 0.. Max_Len};
    type Index_Type is Size_Type {Index_Type in 1.. Max_Len};
    var Data : Array<optional Component, Indexed_By => Index_Type>;
  exports
    \{for \ all \ I \ in \ 1.. \ Cur\_Len \Rightarrow Data[I] \ not \ null\} \ // \ invariant \ for \ Top()
    func Max_Stack_Size(S : Stack) -> Size_Type is
        return S. Max_Len;
    end func Max_Stack_Size;
    func Count(S : Stack) -> Size_Type is
      return S.Cur_Len;
    end func Count;
    func Create (Max : Size_Type \{Max > 0\}) -> Stack
      \{Max\_Stack\_Size(Create) == Max; Count(Create) == 0\} is
      return (Max_Len => Max, Cur_Len => 0, Data => [.. => null]);
    end func Create;
    func Push
      (var S : Stack \{Count(S) < Max\_Stack\_Size(S)\};
       X : Component) \{ Count(S') = Count(S) + 1 \}  is
      S.Cur_Len += 1;
      S.Data[S.Cur\_Len] := X;
```

```
end func Push;
func Top(ref S : Stack { Count(S) > 0}) -> ref Component is
    return S.Data[S.Cur_Len];
end func Top;

func Pop(var S : Stack { Count(S) > 0})
    {Count(S') == Count(S) - 1} is
    S.Cur_Len -= 1;
end func Pop;
end class Stack;
```

This example illustrates annotations used as preconditions ({Count(S) > 0}), postconditions ({Count(S') == Count(S) - 1}), value constraints ({Cur_Len in 0..Max_Len}), and a class invariant ({for all I in 1..Cur_Len => Data[I] not null}).

Concurrent Objects

Expression evaluation in ParaSail proceeds in parallel (see 6.3), as do statements separated by '||' (see 5.1), and the iterations of a concurrent loop (see 5.6 and 5.6.1). The ParaSail implementation ensures that this parallelism does not introduce *race conditions*, situations where a single object is manipulated concurrently by two distinct threads without sufficient synchronization. A program that the implementation determines might result in a race condition is illegal.

Objects in ParaSail are either *concurrent* or *sequential*, according to whether their type is defined by instantiating a concurrent or non-concurrent module. Concurrent objects allow concurrent operations by multiple threads by using appropriate hardware or software synchronization. Sequential objects allow concurrent operations only on non-overlapping components.

10.1 Concurrent Modules

A module is *concurrent* if its interface is declared with the reserved word 'concurrent'. The class defining a concurrent module must also have the reserved word 'concurrent'. Types produced by instantiating a concurrent module are *concurrent* types.

Example:

```
concurrent interface Atomic < Item_Type is Machine_Integer >>> is
   func Create(Initial_Value : Item_Type) -> Atomic;
   func Test_And_Set(var X : Atomic) -> Item_Type;
     // If X == 0 then set to 1; return old value of X
   func Compare_And_Swap(var X : Atomic;
      Old_Val, New_Val : Item_Type) -> Item_Type;
         // If X == Old_{-}Val then set to New_Val; return old value of X
end interface Atomic;
\operatorname{var} X : \operatorname{Atomic} < \operatorname{Int}_{32} > := \operatorname{Create}(0);
var TAS_Result : Int_32 := -1;
var CAS_Result : Int_32 := -1;
block
    TAS_Result := Test_And_Set(X);
    CAS_Result := Compare_And_Swap(X, 0, 2);
end block;
// Now either TAS_Result == 0, CAS_Result == 1, and X is 1,
// or TAS_Result == 2, CAS_Result == 0 and X is 2.
```

This is an example of a concurrent module which defines an atomic object which can hold a single Machine_Integer, and can support concurrent invocations by multiple threads of Test_And_Set and Com-

pare_And_Swap operations. The implementation of this module would presumably use hardware synchronization.

10.1.1 Locked and Queued Operations

The operations of a concurrent module M may include the reserved word 'locked' or 'queued' for inputs of a type based on M. If a concurrent module has any operations that have such inputs, then it is a *locking* module; otherwise it is *lock-free*. Any object of a type based on a locking module includes an implicit *lock* component.

If an operation has an input that is marked 'locked', then upon call, a lock is acquired on that input. If it is specified as a 'var' input, then an exclusive read-write lock is acquired; if it is not specified as a 'var' input then a sharable read-only lock is acquired. Once the lock is acquired, the operation is performed, and then the caller is allowed to proceed.

If an operation has an input that is marked 'queued', then the body of the operation must specify a dequeue condition. A dequeue_condition has the following form:

```
dequeue_condition ::= 'queued' while_or_until condition 'then'
```

A dequeue condition is *satisfied* if the condition evaluates to true and the reserved word 'until' appears, or if the condition evaluates to false and the reserved word 'while' appears.

Upon call of an operation with a 'queued' input, a read-write lock is acquired, the dequeue condition of the operation is checked, and if satisfied, the operation is performed, and then the caller is allowed to proceed. If the dequeue condition is not satisfied, then the caller is added to a queue of callers waiting to perform a queued operation on the given input.

Within an operation of a concurrent module, given an input that is marked 'locked' or 'queued', the components of that input may be manipulated knowing that an appropriate lock is held on that input object. If there is a concurrent input that is *not* marked 'locked' or 'queued', then there is no lock on that input, and only concurrent components of such an input may be manipulated directly.

If upon completing a locked or queued operation on a given object, there are other callers waiting to perform queued operations, then before releasing the lock, these callers are checked to see whether the dequeue condition for one of them is now satisfied. If so, the lock is transferred to that caller and it performs its operation. If there are no callers whose dequeue conditions are satisfied, then the lock is released, allowing other callers not yet queued to contend for the lock.

If an operation of a module performs a call on a queued operation internally, but does not have a queued parameter, then the operation as a whole must be marked with the reserved word 'queued' prior to the reserved word 'func' or 'op' (see 6.1). This indicates that an indefinite delay within the operation might occur, while waiting for the dequeue condition associated with some call to be satisfied. Such operations must not be called from within a locked operation, as they could cause a lock to be held indefinitely. On the other hand, operations with a parameter explicitly marked as 'queued' may be called while already holding a lock on that parameter, but the dequeue condition must already be satisfied at the point of call.

Example:

```
concurrent interface Queue<Element_Type is Assignable >>> is
   func Create() -> Queue;
   func Append(locked var Q : Queue; Elem : Element_Type);
   func First(locked Q : Queue) -> optional Element_Type;
        // Returns null if queue is empty.
   func Remove_First(queued var Q : Queue) -> Element_Type;
        // Queued until the queue has at least one element
end interface Queue;
...
var Q : Queue<Int32> := Create();
var A : Int32 := 0;
var B : Int32 := 0;
```

```
block
    Append(Q, 1); Append(Q, 2);
||
    A := Remove_First(Q);
||
    B := Remove_First(Q);
end block;
// At this point, either A == 1 and B == 2
// or A == 2 and B == 1.
```

In this example, we use a locking module Queue and use locked and queued operations from three separate threads to concurrently add elements to the queue and remove them, without danger of unsynchronized simultaneous access to the underlying queuing data structures.

10.2 Concurrent Evaluation

Two expressions that are inputs to an operation call (see 6.3) or a binary operator (see 4.2.1) are evaluated in parallel in ParaSail, as are the expressions that appear on the right hand side of an assignment and those within the object_name of the left hand side (see 5.2). In addition, the separate statement_threads of a statement_thread_group (see 5.1) are performed in parallel. Finally, the iterations of a concurrent loop (see 5.6) are performed in parallel.

Two object_names that can be part of expressions or statements that are evaluated concurrently must not denote overlapping parts of a single sequential object, if at least one of the names is the left-hand side of an assignment or the actual parameter for a 'var' parameter of an operation call. Distinctly named components of an object are non-overlapping. Elements of a container associated with distinct indices are non-overlapping (see 8.1).

Examples:

```
\begin{array}{llll} & \text{func Bump}(\text{var } A : \text{Int}) \to \text{Int}\,; \\ X := 3 & || & X := 5 & // & illegal \\ X := 3 & || & Y := X & // & illegal \\ A := X & || & B := X & // & legal \\ A[I] := 2 & || & A[J] := 3 & // & illegal & if & I & can & equal & J \\ Bump(X) & + & X & // & illegal \\ X := & Bump(X) & // & legal &
```

ParaSail Source Files and Standard Library

11.1 ParaSail Source Files

Each ParaSail source file is made up of a sequence of standalone module or operation definitions. Import clauses can be used to restrict which other modules or operations are visible when defining a given standalone module or operation.

```
source_file ::=
  [ program_unit_list ] { import_clause_list program_unit_list }

program_unit_list ::= standalone_program_unit { standalone_program_unit }

import_clause_list ::= import_clause { import_clause }

standalone_program_unit ::=
  interface_declaration | class_definition | operation_definition
```

11.2 Import Clause

The import_clause may be used to control which other standalone program units are visible within a given program_unit_list.

```
import_clause ::=
   'import' imported_module_specification { ',' imported_module_specification }

imported_module_specification ::= module_identifier [ '::' '*' ] | '*'

Examples:
   import Acme:: Utilities:: Graphics
   import Acme:: Killer_App::*
```

An import_clause without an * allows the specified program unit to be referenced within the following program_unit_list, using either its full name or its simple name. An import_clause with a * allows any program unit whose full name has the given prefix to be referenced, and also provides direct visibility to

the simple names of the units immediately within the module identified by the given prefix. Hence, the above example allows reference to the program unit Acme::Utilities::Graphics, and to all program units with names of the form Acme::Killer_App::.... In addition, the simple name Graphics may be used to refer to Acme::Utilities::Graphics, and if there is a Acme::Killer_App::Driver program unit and a Acme::Killer_App::GUI program unit, then the simple names Driver and GUI, respectively, may be used to refer to these units.

Standalone program units that appear in a source file before any explicit import_clauses, are provided with a default import clause. If the name of the standalone unit is of the form A::B::C then the default import clause is:

```
import A::B::*
```

If the name of the standalone unit is a simple name (such as A), then the default import clause is:

```
import *
```

The net effect of the default import clause is to make the names of the the *sibling* program units directly visible.

After an import_clause_list appears in a source file, these imports apply until the next import_clause_list, or the end of the source file, whichever comes first. That is, an import_clause_list applies only to the immediately following program_unit_list.

Two additional import clauses apply to all ParaSail source code:

```
import PSL::Core::*
import PSL::Containers::*
```

This makes the names of the standard library modules in the Core and Containers subsystems directly visible to all ParaSail code.

11.3 ParaSail Syntax Shorthands

ParaSail syntax is not as rigid as implied by the BNF given in this reference manual. In particular, semicolons at the end of a statement or declaration may be omitted. In addition, ParaSail allows the end XXX indications to be omitted, by adopting a *Python*-like convention of using ':' instead of is, then, loop, and of, and relying on indentation to indicate where the corresponding construct ends.

For example, the following is a legal use of these shorthands:

```
func Fib (N : Integer) -> Integer:
    // Recursive fibonacci but with linear time

func Fib_Helper(M : Integer)
    -> (Prev_Result : Integer; Result : Integer):
    // Recursive "helper" routine which
    // returns the pair ( Fib(M-1), Fib(M) )
    if M <= 1:
        // Simple case
        return (Prev_Result => M-1, Result => M)
    else:
        // Recursive case
        const Prior_Pair := Fib_Helper(M-1)

        // Compute next fibonacci pair in terms of prior pair
        return with
        (Prev_Result => Prior_Pair.Result,
```

```
Result => Prior_Pair.Prev_Result + Prior_Pair.Result)

end func Fib_Helper // This is optional because used ':'

// Just pass the buck to the recursive helper function
return Fib_Helper(N).Result
```

11.4 ParaSail Standard Library

ParaSail includes a number of language-provided modules, with names of the form PSL::Core::* and PSL::Containers::*. These are all defined in the source file "aaa.psi", and that file should be used as a reference for use of these standard modules.

Several of these modules are parameterless, and act as the predefined types of the language:

Univ_Integer<> arbitrary length integers

Univ_Real <> ratio of two Univ_Integers, with plus/minus zero and plus/minus infinity

Univ_Character<> 31-bit ISO-10646 (Unicode) characters

Univ_String<> vector of Univ_Characters

Univ_Enumeration<> all values of the form # identifier

Boolean<> an enumeration type with two values #false and #true

Ordering<> an enumeration type with four values #less, #equal, #greater, and #unordered

The other language-provided modules include:

abstract interface Any<> all types implement Any<>implicitly

abstract interface Assignable <> provides ":=", "<==", and "<=>" operations; all but concurrent types and reference types implement Assignable <> implicitly

abstract interface Comparable <> provides "=?" operator

abstract interface Hashable<> implements Assignable<>, Comparable<>; provides Hash operation

abstract interface Countable <> implements Hashable <>; provides "+" and "-" operators to add or subtract Univ_Integers to progress through the values of the type

interface Vector<Element_Type is Assignable<>> an extensible array indexed by Univ_Integer starting at 1

interface ZVector<Element_Type is Assignable<>> an extensible array indexed by Univ_Integer starting at 0

interface Enum<Values: Vector<Univ_Enumeration>> implements Countable<>; used to define a new enumeration type given the enumeration literals

interface ZString<> very similar to Univ_String, except that indexing starts at 0 rather than 1

interface Interval<Bound_Type is Countable<>> intervals are constructed using the "..", "..<", "<..", and "<..<" operators with a low and high bound specified by values of the Bound_Type

interface Integer < Range : Interval < Univ_Integer >:= Default_Range > implements Countable <> , Imageable <> ; provides the usual operators

- $\label{eq:continuous} \textbf{interface Float} < \textbf{Digits}: \ \textbf{Univ_Integer} := \textbf{Default_Digits} > \ \textbf{implements Hashable} <> , \ \textbf{Imageable} <> ; \\ \textbf{provides the usual operators}$
- interface Array<Element_Type is Assignable<>; Indexed_By is Countable<>> a fixed-size array of Element_Type, indexed by a specified countable type
- $\mathbf{interface} \ \mathbf{Set} \ \boldsymbol{<} \mathbf{Element_Type} \ \mathbf{is} \ \mathbf{Hashable} \boldsymbol{<} \boldsymbol{>} \boldsymbol{>} \ \mathbf{a} \ \mathbf{set} \ \mathbf{of} \ \mathbf{Element_Type}$
- interface Map <Key_Type is Hashable<>; Element_Type is Assignable<>> a map from Key_Type to Element_Type

Consult "lib/aaa.psi" for further details on the ParaSail Standard Library.

Appendix: Using the ParaSail Interpreter and Virtual Machine

The ParaSail interpreter and virtual machine is invoked with the following command:

The psli command invokes the interpreter on the specified ParaSail source files. If -command is specified, then after compiling the ParaSail source to ParaSail Virtual Machine (PSVM) instructions, it executes the specified ParaSail func with the given arguments, if any. If -command is not specified, a prompt is presented once processing is successful, allowing the user to enter a command to the virtual machine in the form "func arg1 arg2 ...".

At the interactive prompt, the quit command may be used to exit the virtual machine. The "debug on" command may be used to turn on virtual machine debugging. The "debug off" command may be used to turn it back off. The "servers <number>" command may be used to specify the total number of server threads to use for work stealing, henceforth.

The number of servers can also be specified on the command line via "-servers <number>". The default is six. That is, there is effectively an implicit "-servers 6" on the command line if no explicit "-servers nnn" is specified. At the interactive prompt, "servers nnn" is only effective to increase the number of servers, because once a server is activated there is no mechanism to deactivate it.

The first source file to be interpreted should *always* be the ParaSail standard library, with name "../lib/aaa.psi". This file contains the definitions for the standard modules such as Univ_Integer, Set, Vector, etc.

If the ParaSail interpreter detects an error during parsing, semantic analysis, or PSVM code generation, it gives error messages on the standard error output stream, as well as creating a file "errors.err," which may be viewed using the "vim" text editor giving it the "-q" flag. When "errors.err" is viewed using "vim -q", it will automatically position the text window at the line in a source file with a compilation error. The vim commands:cn and:cp may be used to go to the next and the previous error.

In addition to producing error messages, the ParaSail interpreter also produces listing files, with names of the form "file1.psl.lst". These include a line-numbered listing of the source file, an *unparsing* of each top-level compilation unit, and the ParaSail Virtual Machine instructions generated for each operation. These listing files are produced whether or not an error is detected. The ParaSail Virtual Machine instructions are only produced if the ParaSail compiler's semantic analysis of the source code succeeds. By default, a listing is only produced when there is no "-command" specified. This default can be overridden with the "-listing on/off" option on the command line. Giving "-listing off" will turn off listings in all cases. Giving "-listing on" will produce a listing in any case.

Note that the error recovery of this ParaSail interpreter is not perfect, so it may be necessary to fix the first few errors and then rerun psli to avoid being mislead by cascading errors.

12.1 ParaSail LLVM-based Compiler

There is now also a true *compiler* for ParaSail, written in ParaSail itself. It converts the PSVM instructions into LLVM instructions, and then invokes the LLVM compiler/assembler (llc/clang) to produce object code. The cshell-script which invokes the compiler is called "bin/pslc.csh" and you can run it with no arguments to learn how to invoke it. The first time you use it, you will need to compile the ParaSail standard library (lib/aaa.psi) and the compiler itself. This is done with the command bin/pslc.csh -b3 where -b3 requests a full bootstrap of the compiler.

An important thing to know about the compiler is that a compiled program needs a *main* routine in which to start execution. By convention, this needs to be called main and have one parameter of type Basic_Array<Univ_String>. The compiler can automatically generate such a routine, if you have an existing routine with a different name. The compiler generates a simple *wrapper* routine called main which calls the user-specified routine, if you give it the "-m <name>" command-line flag. Here is a description of some of the command line switches of pslc.csh:

Run pslc.csh with no parameters to get the full list of command-line switches.

12.2 Example of using ParaSail Interpreter

Examples of using the ParaSail interpreter:

```
% psli ../lib/aaa.psi qsort.psl
ParaSail Interpreter and Virtual Machine beta 1.0 Revision: 6.2
Copyright (C) 2011-2014, AdaCore, New York NY, USA
This program is provided "as is" with no warranty.
Parsing ../lib/aaa.psi
Parsing qsort.psl
---- Beginning semantic analysis ----
Starting up thread servers
162 trees in library.
Done with First pass.
Done with Second pass.
Done with Pre codegen pass.
Done with Code gen.
Filling in cur-inst-param info in op tables.
Evaluating global constants.
Finishing type descriptors.
Command to execute: Test_Sort 10
Before sort, Vec =
70, 43, 1, 92, 65, 26, 40, 98, 48, 67
After sort, Vec =
```

```
1, 26, 40, 43, 48, 65, 67, 70, 92, 98
After 2nd sort, Vec2 =
1, 26, 40, 43, 48, 65, 67, 70, 92, 98
Command to execute: quit
Shutting down thread servers
Stg_Rgn Statistics:
New allocations by owner:
                                3312 = 55%
Re-allocations by owner:
                                1892 = 31%
Total allocations by owner:
                                 5204 = 87%
New allocations by non-owner:
                                 317 = 5%
                                 440 = 7%
 Re-allocations by non-owner:
Total allocations by non-owner: 757 = 12%
Total allocations:
                                 5961
Threading Statistics:
Num_Initial_Thread_Servers : 1 + 1
Num_Dynamically_Allocated_Thread_Servers : 4
Max_Waiting_Shared_Threads (on all servers' queues): 1
 Average waiting shared threads: 0.00
Max_Waiting_Unshared_Threads (on any one server's queue): 1
 Average waiting unshared threads: 0.00
Max_Active (threads): 6
 Average active threads: 2.20
Max_Active_Masters : 6
Max_Subthreads_Per_Master : 3
Max_Waiting_For_Subthreads : 3
Num_Thread_Steals : 570 out of 1 + 570 (U+S) thread initiations = 99%
% psli ../lib/aaa.psi qsort.psl -command Test_Sort 10
Before sort, Vec =
70, 43, 1, 92, 65, 26, 40, 98, 48, 67
After sort, Vec =
1, 26, 40, 43, 48, 65, 67, 70, 92, 98
After 2nd sort, Vec2 =
1, 26, 40, 43, 48, 65, 67, 70, 92, 98
% psli ../lib/aaa.psi error_test.psl
Parsing aaa.psi
Parsing error_test.psl
error_test.psl:90:8: Error: Use ":=" rather than "=" in ParaSail
error_test.psl:92:8: Error: Use "!=" rather than "/=" in ParaSail
error_test.psl:94:7: Error: Use "elsif" rather than "elseif"
error_test.psl:94:11: Error: Use "==" rather than "=" in ParaSail
error_test.psl:239:17: Error: Use "==" rather than "=" in ParaSail
error_test.psl:263:42: Error: "for-each" iterator uses "of" rather than "in"
```

error_test.psl:274:5: Error: Use "end if" rather than "endif"

% vim $\neg q$ [interactive correction of errors identified in errors.err]