

INF5390 oblig 2

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Task 1

Domain:

Constants:

The domain does not have any known constants.

Functions:

The domain has the following functions:

- $\text{canfool}(X, Y)$ - Returns the set of times when X can fool Y

Relations:

The domain has the following relations:

- $\text{Man}(X)$ - (X) exists if X is a man
- $\text{Woman}(X)$ - (X) exists if X is a woman
- $\text{Vegetarian}(X)$ - (X) exists if X is a vegetarian
- $\text{Smart}(X)$ - (X) exists if X is smart
- $\text{Politician}(X)$ - (X) exists if X is a politician
- $\text{Barber}(X)$ - (X) exists if X is a barber
- $\text{Hate}(X, Y)$ - (X, Y) exists if X hate Y
- $\text{Like}(X, Y)$ - (X, Y) exists if X like Y
- $\text{Shaves}(X, Y)$ - (X, Y) exists if X shaves Y

All relations and functions has a fixed arity, but we use the paranthesis to define arguments as it is easier to read.

a.

$$\forall X \forall Y ((Vegetarian(Y) \wedge Hates(X, Y)) \Rightarrow Smart(X))$$

b.

$$\forall X \forall Y (Smart(X) \wedge Vegetarian(X) \Rightarrow (\neg Like(Y, X)))$$

c.

$$\exists X \forall Y ((Woman(X) \wedge (Man(Y) \wedge Vegetarian(Y)) \Rightarrow Like(X, Y))$$

d.

$$\exists X \forall Y ((Barber(X) \wedge Man(Y) \wedge \neg Shaves(Y, Y)) \Rightarrow Shaves(X, Y))$$

e.

$$\forall X (Politician(X) \Rightarrow ((\exists Y \forall T (T \in canfool(X, Y)) \vee \forall Y \exists T (T \in canfool(X, Y))) \wedge \exists Y \exists T (T \notin canfool(X, Y))))$$

Task 2

$$\forall X \forall Y \exists T ((Sock(X) \wedge Sock(Y) \wedge Pair(X, Y)) \Rightarrow (Before(Now, T) \wedge (Lost(X, T) \vee Lost(Y, T))))$$