# CS225 Homework 1



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#### 1. Our Solution:

We suppose the list L has members: length denoting the length of the list, or number of elements in the list; data[i] denoting the i-th element of the list. Assuming the index starts from 1.

Therefore, just cut down the length of l to disable elements after the i-th in the list and w obtain L.length := L.length - k, so the elements  $data[i+1, i+2, \cdots, length]$  will be "ignored", or deleted.

Since this only requires one instruction thus the complexity has nothing to do with k, the answer should be  $\Theta(1)$ .

## 2. (a) Our Solution:

When function  $g: T' \times T' \to T'$  satisfies a rule similar to "Law of Association". Denoting a list as t, of which the i-th element is  $t_i$ , the sublist containing a-th to b-th element is  $t_{a..b}$ . The condition is that for every  $k_1, k_2$  satisfying  $a < k_1, k_2 < b$ , we have  $g(t_{a..k_1}, t_{k_1+1..b}) = g(t_{a..k_2}, t_{k_2+1..b})$ .

The reason for this requirement is, any list l with more than three elements can be divided into two lists in n-1 ways, where n is the length of the list l. Assuming  $g(t_{a..k_1},t_{k_1+1..b}) \neq g(t_{a..k_2},t_{k_2+1..b})$ , we find if the division happens at the k-th element, i.e. dividing the list into  $t_{a..k}$  and  $t_{k+1..b}$ , the result depends on the value of k, which is against definity.

## (b) Our Solution:

Algorithm 1: Get list length

```
if list[id] reaches EndOfList then
2
3
          if id = 0 then
              return zero length
4
          else
5
              return 1
7
          end
8
          return getLength (list, id +1)
9
      end
10 end
```

**Length of the list** For the first operation, we iterate every element until reaching the end of the list. Since the algorithm just iterate from the first element to the last, the complexity is  $\Theta(n)$ .

**Perform a function to all element** For the second operation, assuming the function f accepts an element x in l. For our structural recursion, refer to Algorithm 2.

Same as above, since the algorithm iterate from the first to the last, the complexity should be  $\Theta(n)$ .

**Find sublists** For the structural recursion, time consuming (time complexity) is  $\Theta(1)$  for one loop. And it will recursive for n times which means the time complexity will be  $\Theta(n)$ . Refer to Algorithm 3

#### (c) Our Solution:

Complexity for all operations are  $\Theta(n)$ , because they all iterate from the first element to the last, each element costing a constant time.

#### 3. Our Solution:

Please refer to Figure 1. The left half is denoted as Figure I, and right Figure II.

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# Algorithm 2: Do a Function for All Elements

```
input: list, the id of currently processing element, the array of result [] containing return values for all
               element before the id-th
   Output: result [] containing return values for all elements
2 begin Function
        \quad \textbf{if} \ \mathsf{length} = 0 \ \textbf{then} \\
            Return the value for an empty list, and exit
        end
5
6
        if id = length - 1 then
            Return in result [id] the function value
8
        end
        if id < length then</pre>
            Compute the function value
10
             \mathsf{result}[\mathsf{id}] \leftarrow \mathsf{the} \; \mathsf{function} \; \mathsf{value}
11
            Call Function (list, id + 1, result[])
12
        end
13
14 end
```

## Algorithm 3: Find Sublists

```
input: A list list, an index id
   output: The sublist of elements in list satisfying condition \phi
1 begin findSublist
       if id == 0 then
2
           Exit the call and return to caller with an empty sublist
3
       end
4
       if \; \mathsf{id} > \mathtt{length}(\mathsf{list}) \; then \;
5
          Exit this call
       if list[id] satisfies condition φ then
8
           Append (list [id], sublist)
10
       end
       findSublist(list, id + 1)
11
12 end
```

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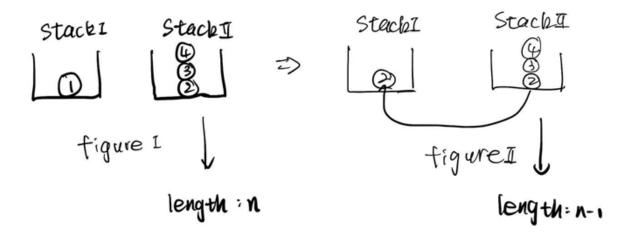


Figure 1: Figure for exercise 3.

- As mentioned in figure I, when we have two stacks, we can store the first data in the stack I and then we should store other data in stack II (FI: FIRST INPUT)
- When we need data, we will fetch the first data in the stack I (FO: FIRST OUTPUT) and then move it.
- Then we will use pointer to read the second data (we can read and copy any data in the stack no matter where it is) and copy it to the stack I, which means we can read the second data (FIFO). Then delete the data in the stack I and copy the third one into the stack I and repeat the steps. By this means, we can read and use the data in order. (As mentioned in the Figure I to Figure II)
- Each time we move one data from stack II to stack 1, we minus the length of the stack II by one (If the original length of the stack II is n, when we move the second data from stack II to stack 1, its length becomes n-1, when we move the third data from stack II to stack I, the length of the stack becomes n-2). By this means, Each FIFO operation takes amortised constant time. (As mentioned in the length indication of the figure I and figure II)

## 4. Our Solution:

Please refer to the code bundle.

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