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ECE 459

COMMUNICATIONS SYSTEMS

Final Project (Fall 2023)

PERFORMANCE ANALYSIS OF AMPLITUDE AND FREQUENCY MODULATION IN NOISE

Group 5

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Abstract

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Contents

1 Introduction

1.1 The Background

The history of modulation techniques dates back to the early days of radio communication when Amplitude Modulation emerged as the pioneering method. Over time, Frequency Modulation gained prominence due to its resilience against noise and superior audio quality, particularly in broadcasting and mobile communication [1, p. 152].

Amplitude Modulation (AM) is a communication technique that transmits messages by modulating the amplitude of a radio frequency (RF) wave. This modulation is achieved through the combination of the message signal with a high-frequency carrier wave. The resulting modulated waves can be demodulated using either coherent detectors or envelope detectors.

Frequency Modulation (FM), classified as a form of Angle Modulation, involves integrating the message into the phase of an RF signal. Demodulation of the FM signal can be accomplished through the utilization of differentiators or slope circuits.

Both AM and FM present distinct advantages and trade-offs, necessitating a comprehensive performance analysis. Such an analysis is crucial for a thorough understanding of their strengths and limitations within contemporary communication systems.

1.2 Objectives and Purposes

This project is designed to conduct a comprehensive analysis of the performance of Frequency Modulation (FM) and Amplitude Modulation (AM) communication systems in the presence of noise. The methodology involves constructing an envelope-modulated AM and narrow-band FM communication system, with the subsequent application of Additive White Gaussian Noise (AWGN) to the system. Specifically, the demodulation of AM signals is to be carried out using envelope detectors.

The team is tasked with simulating the modulation and demodulation processes for both systems and subsequently comparing the spectra and waveforms of the message signals and demodulated signals. The chosen message signals encompass both a multi-tone message and a Text-to-Speech (TTS)-generated voice recording. Theoretical and experimental pre- and post-detection signal-to-noise ratios (SNRs) are to be obtained to facilitate a comprehensive performance analysis.

Furthermore, the team is required to meticulously observe disparities between input and output signals, as well as their spectra, in order to conclude the distinctive characteristics of AM and FM modulation. A comparative analysis of anti-noise performance is also imperative, involving the measurement of the signal-to-noise ratio (SNR). The evaluation of simulation performance itself is to be conducted by comparing theoretical and experimental pre- and post-detection SNRs.

This project aims to equip the team with an in-depth understanding of both the modulation and demodulation processes, enabling a nuanced comprehension of the intricacies involved in implementing communication systems using Python. Specifically, the team is expected to demonstrate proficiency in performing Fourier Transform and Hilbert Transform, as well as implementing filters and envelope detectors.

1.3 Literature Review

The textbook by Haykin and Moher [1, Sec. 3.1] presents an intuitive method of envelope modulation. In this approach, the modulated signal is derived by combining a carrier wave with an amplified

and DC-shifted message signal. For the demodulation process, the team references Haykin's work, particularly [1, Fig. 9.8]. Ulrich [2] introduces an alternative method of envelope detection utilizing Hilbert Transformation. This technique, when employed in conjunction with the `scipy.signal` package, streamlines the implementation of envelope detector design.

The Direct Method of Frequency Modulation (FM) signal generation, as illustrated in [1, Fig. 4.7], involves components such as an integrator, a phase modulator, and a local oscillator. The demodulation process for FM is also elucidated in the same textbook, specifically in [1, Fig. 9.13].

The realization of ideal filters poses challenges due to the discontinuous frequency response. However, the Butterworth filter offers a practical solution for simulating real-world filters, as discussed in the works of Storr [3] and Khetarpal et al. [4]. Implementation of the Butterworth filter can be achieved using the `scipy.signal` package.

2 Methodology

This chapter presents the methodology employed in the project using Python 3. The simulations were executed within the Jupyter Notebook environment, leveraging essential packages for numerical computation, signal analysis, and plotting, namely `numpy`, `scipy`, and `matplotlib`.

2.1 Choice of Message Signal

Two distinct message signals were selected for thorough investigation in this project:

1. The multi-tone sinusoidal signal $m_1(t) = A_1 \cos(2\pi f_1 t + \phi_1) + A_2 \cos(2\pi f_2 t + \phi_2)$.
2. The TTS-generated male voice recording.

The first signal, a multi-tone sinusoidal waveform, was chosen for its simplicity as a periodic function and its unique attributes as a linear combination of two sinusoidal functions. This particular choice facilitates the observation of distortion induced by noise, given the relatively straightforward frequency spectra of sinusoidal functions. On the other hand, the utilization of a TTS-generated male voice recording introduces a more realistic scenario, allowing the team to experiment with the designed communication system in a practical context.

2.2 AM Simulation

2.3 Envelope Modulation

The modulation of a message signal, denoted as $m(t)$, can be achieved through envelope modulation, represented by the equation:

$$s(t) = A_c[1 + k_a m(t)] \cos(2\pi f_c t) \tag{2.1}$$

In this expression, k_a denotes the modulation sensitivity, A_c corresponds to the amplitude of the carrier wave, and f_c represents the frequency of the carrier wave. It is imperative to ensure that the carrier wave frequency f_c significantly surpasses the highest frequency component, denoted as W, of the message signal $m(t)$ to prevent aliasing. This condition can be expressed as $f_c \gg W$. Moreover, the choice of the modulation sensitivity, k_a, needs to adhere to the constraint:

$$|k_a m(t)| < 1, \quad \text{for all } t \tag{2.2}$$

This condition is crucial to prevent envelope distortion, as outlined by Haykin and Moher [1, pp. 101-102].

The implementation of amplitude modulation (AM) can be illustrated through the block diagram depicted in Figure 2.1. For practical implementation in Python, the AM modulation process can be realized using the following code snippet:

```
1 am_signal = Ac*(1 + ka*data) * np.cos(2*np.pi*fc*t)
```

Here, `data` refers to the array containing samples of the message signal, and `ka` denotes the modulation sensitivity.

2.3.1 Envelope Detection

2.3.2 SNR Calculation and Measurement

2.4 FM Simulation

2.4.1 Narrow-Band FM Modulation

2.4.2 Narrow-Band FM Demodulation

2.4.3 SNR Calculation and Measurement

2.5 Filter Design

2.5.1 Ideal Filters

2.5.2 Butterworth Filter in Python

Both Amplitude Modulation (AM) and Frequency Modulation (FM) communication systems necessitate the incorporation of filters. In practical scenarios, however, the realization of ideal filters poses inherent challenges. Nevertheless, the Butterworth Filter exhibits characteristics closely approximating those of an ideal filter. Figures 2.2 and 2.3 depict the frequency responses of Butterworth Low Pass Filter (LPF) and Band Pass Filter (BPF) with varying orders, illustrating that an increased order (n) results in a more pronounced roll-off slope. As expounded by [3], [5], a Butterworth Low Pass Filter manifests a maximally flat frequency response within its passband, swiftly attenuating beyond the cut-off frequency. This advantageous attribute empowers the design of filters with minimal distortion, albeit at the expense of an indeterminate phase delay induced by the inherent properties of Infinite Impulse Response (IIR) filters.

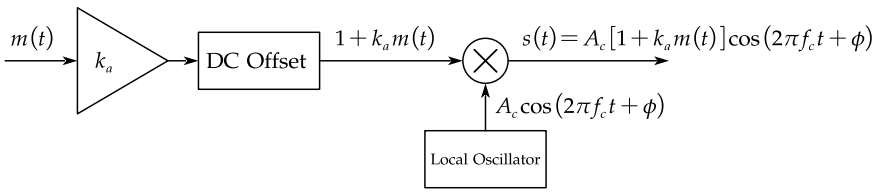

Figure 2.1 Block diagram illustrating the process of envelope modulation.

In the digital realm, Python facilitates the implementation of filters as digital IIR/FIR filters, with each filter in the z-domain expressed as the quotient of two polynomials:

$$H_{\text{filter}}(z) = \frac{\sum_{n=0}^{\infty} a_n z^{-n}}{\sum_{m=0}^{\infty} b_m z^{-m}} \tag{2.3}$$

The response of the filter is uniquely determined by coefficients a_i and b_j ($0 \leq i, j \leq n$), where these coefficients can be computed using the `scipy.signal.butter()` function, as detailed by [6]–[8]. A practical instantiation of an IIR filter is exemplified below:

```
# Generate an 8-order 40 Hz to 80 Hz IIR BPF, sample rate = fs
b, a = butter(N=8, [40, 80], btype='band', fs=fs)
# Apply the filter to the message signal
filtered_signal = filtfilt(b, a, message)
```

Figures 2.2 and 2.3 showcase the frequency response of a Butterworth LPF and BPF, respectively, each featuring a cut-off frequency of $\omega_c = 100\,\text{rad/s}$. The black dashed line denotes the $-3\,\text{dB}$ amplitude.

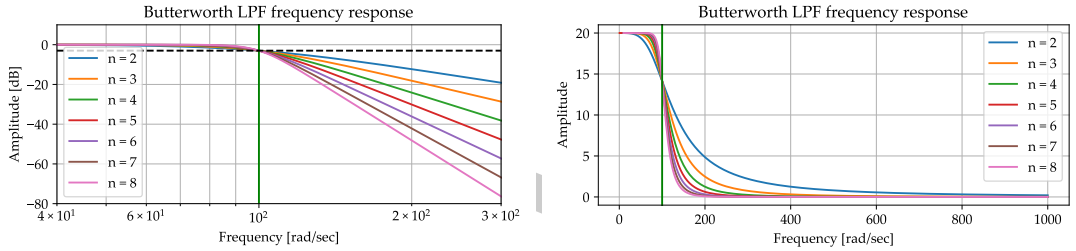

Figure 2.2 The frequency response of a Butterworth LPF with cut-off frequency $\omega_c = 100\,\text{rad/s}$. The black dash line shows the $-3\,\text{dB}$ amplitude.

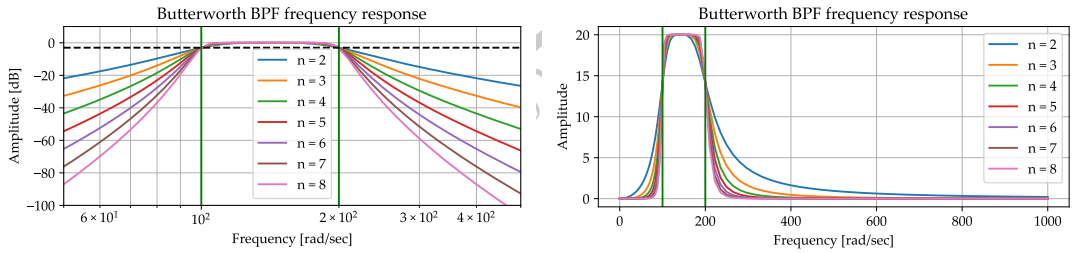

Figure 2.3 The frequency response of a Butterworth BPF with pass-band from 100 Hz to 200 Hz. The black dash line shows the $-3\,\text{dB}$ amplitude.

2.6 Additive White Gaussian Noise

3 Results and Discussion

4 Conclusion

Statement of Contribution

Appendix A Python Scripts of This Project

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